

# Prior Models on Coronary Arteries to Support Coronary Artery Detection



Checkpoint Presentation

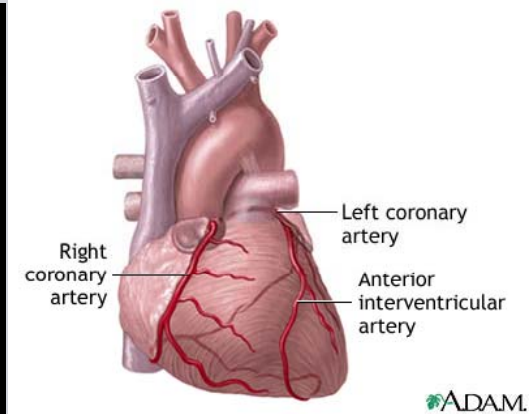
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Mentor: Gareth Funka-Lea, Princeton

## Project Overview

### Coronary Artery Disease

- 53% of cardiovascular diseases. Leading cause of death in the United States!
- Coronary detection in CTA is important for diagnosis, treatment and monitoring.



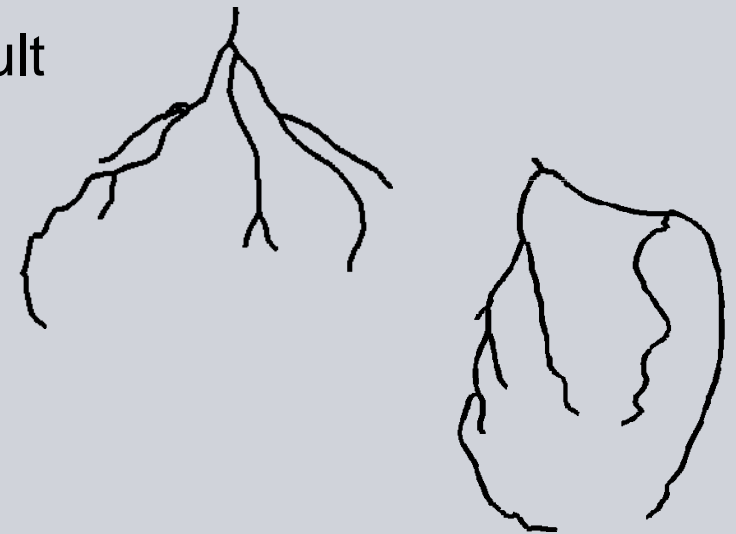
ADAM.  
nlm.nih.gov

Problem: Coronary detection from CTA is difficult due to

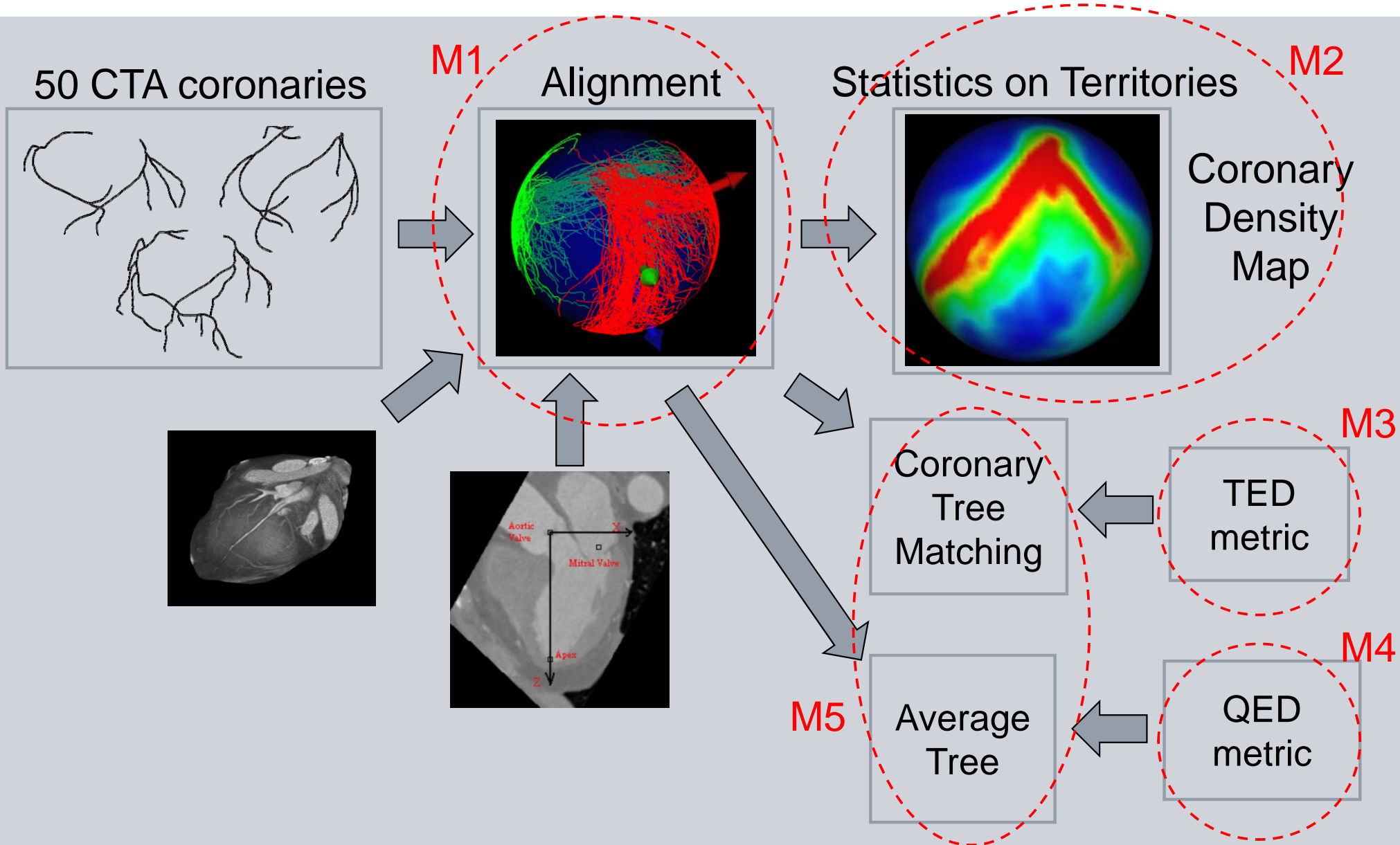
- their high anatomical variability
- pathologies and imaging artifacts

Project Goal: Build prior coronary models to

- improve detection
- allow for statistical analysis



# Technical Approach



## Milestones

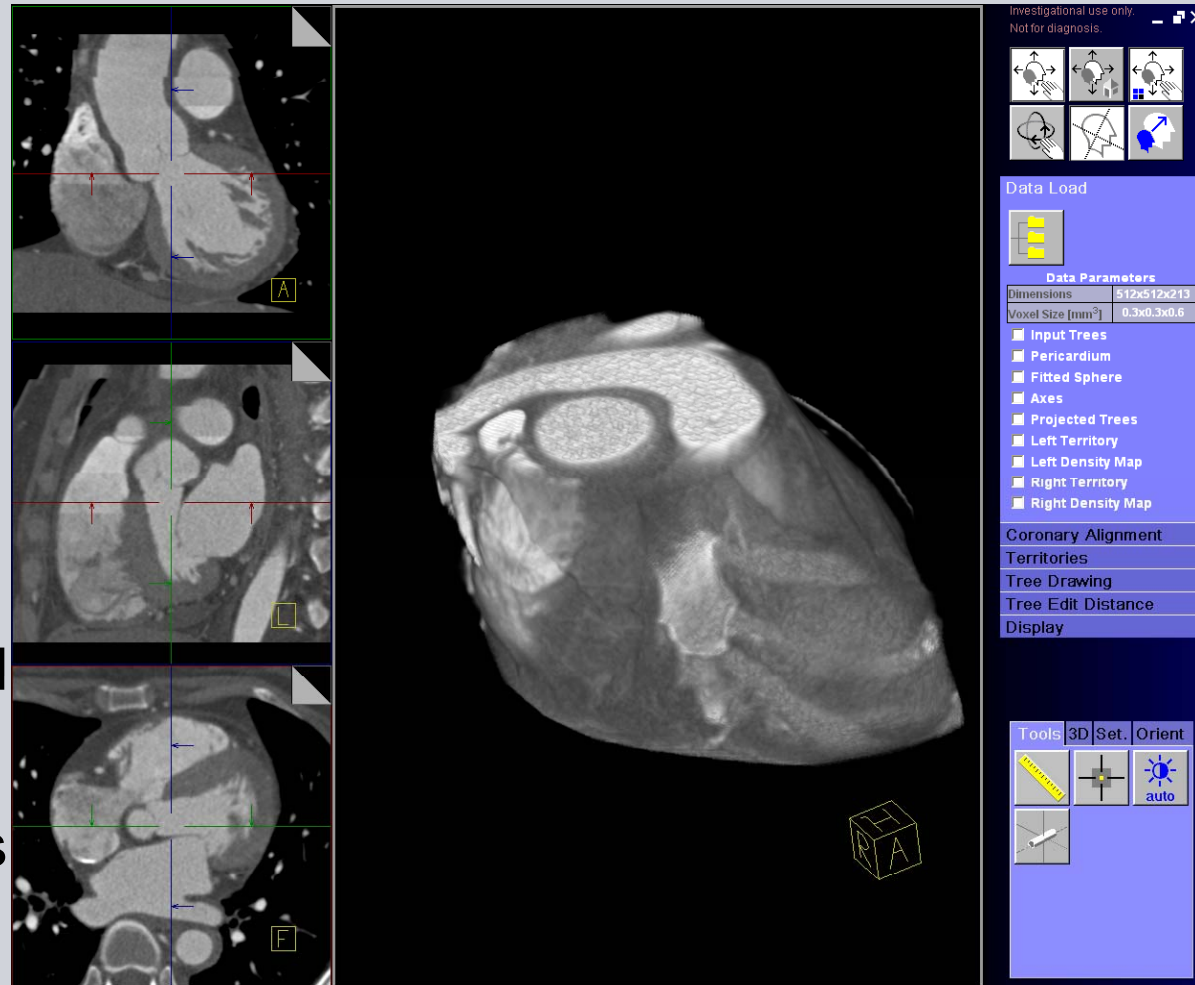
	Milestone	Planned	Achieved
1	Alignment of coronary centerlines (MINIMUM) ✓	Mar4	Mar2
2	Statistics on territories (MINIMUM) ✓	Mar11	Mar10
3	Geodesic with TED algorithm (EXPECTED) ✓	Apr8	Apr5
4	Geodesic with QED algorithm (EXPECTED) 50%	Apr29	-
5	Applications (MAXIMUM) Pending	May8	-

Milestone Validations	
1	Visualize coronary trees on the canonical surface ✓
2	Visualize both coronary trees and density map on the canonical surface ✓
3	Test on example trees with ground truth TED geodesic ✓

# Milestone 1 – Prototype setup

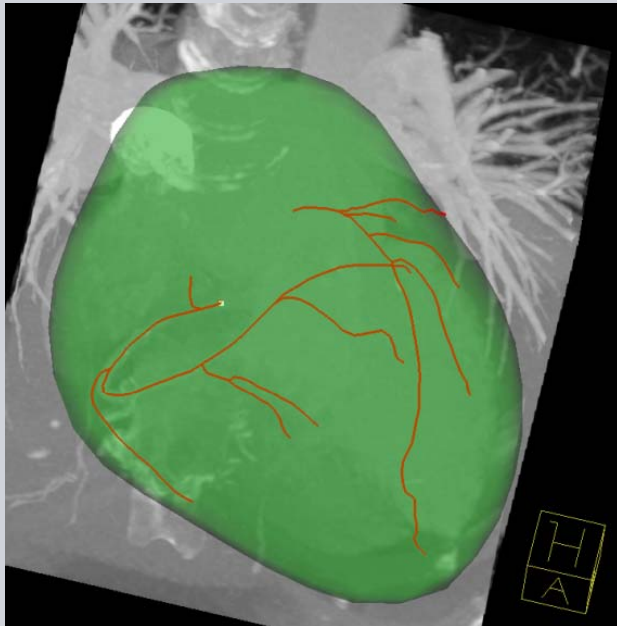
## Prototype software

- Built using Siemens' rapid prototyping platform XIP (extensible imaging platform)
- Loading and visualization of data
- Each milestone is implemented in a separate task card
- Features to validate milestones

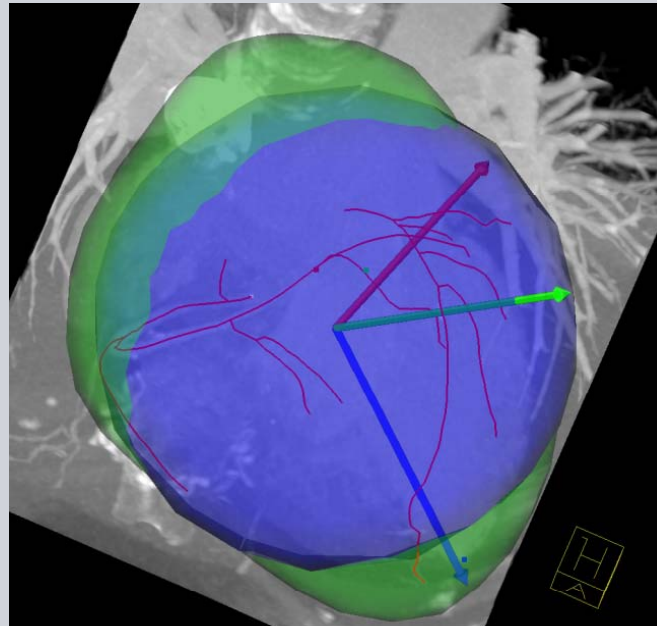


## Milestone 1 – Coordinate System

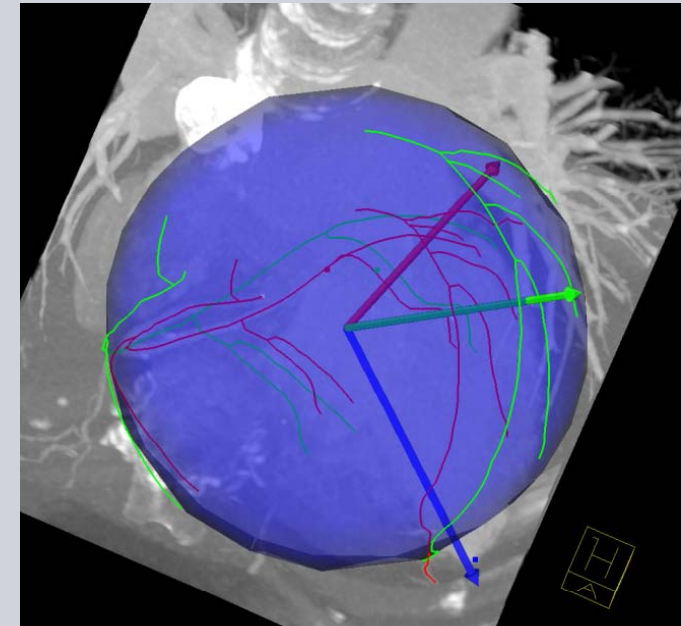
### Definition of the Canonical Coordinate System



Input Coronary Trees  
and Pericardium Mesh



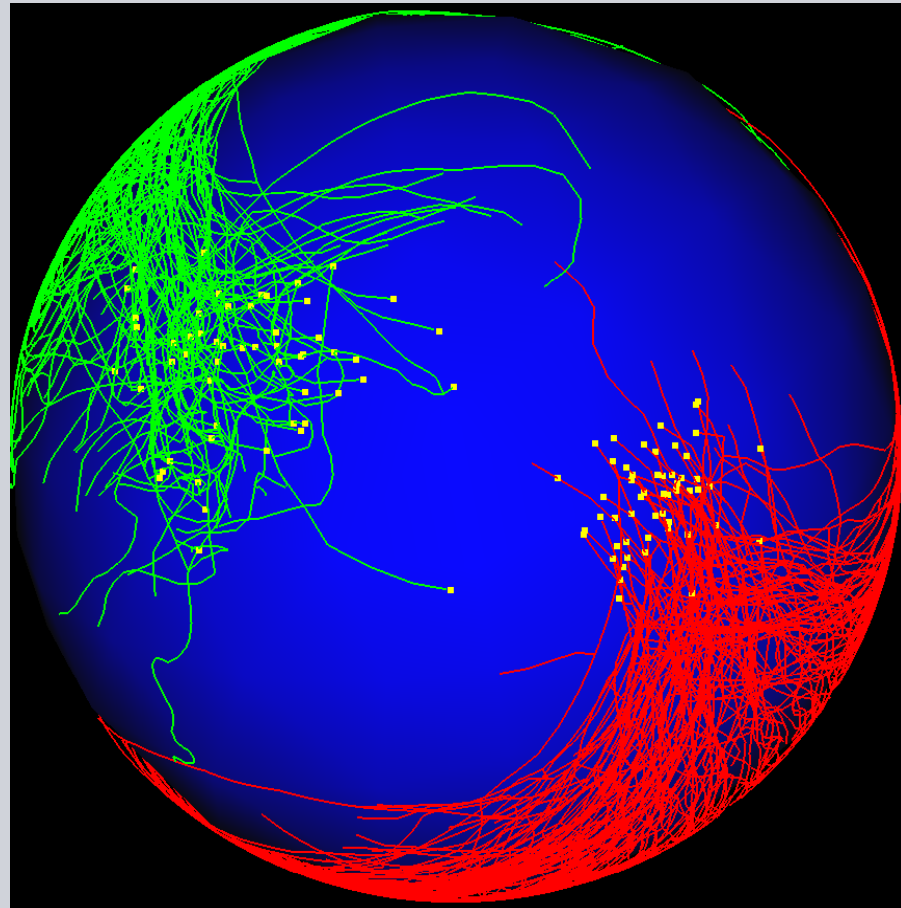
Fitted Spherical  
Model with Axes



Projected Trees



# Milestone 1 - Alignment



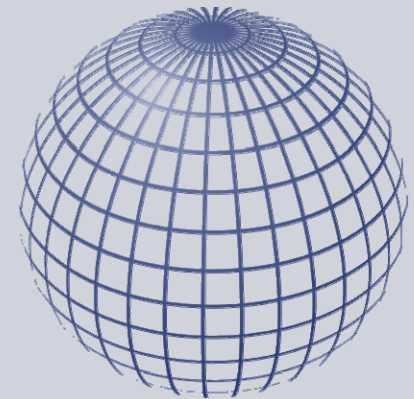
Ostia Distribution

## Milestone 2 – Coronary Distance Maps

Discretization of the spherical manifold

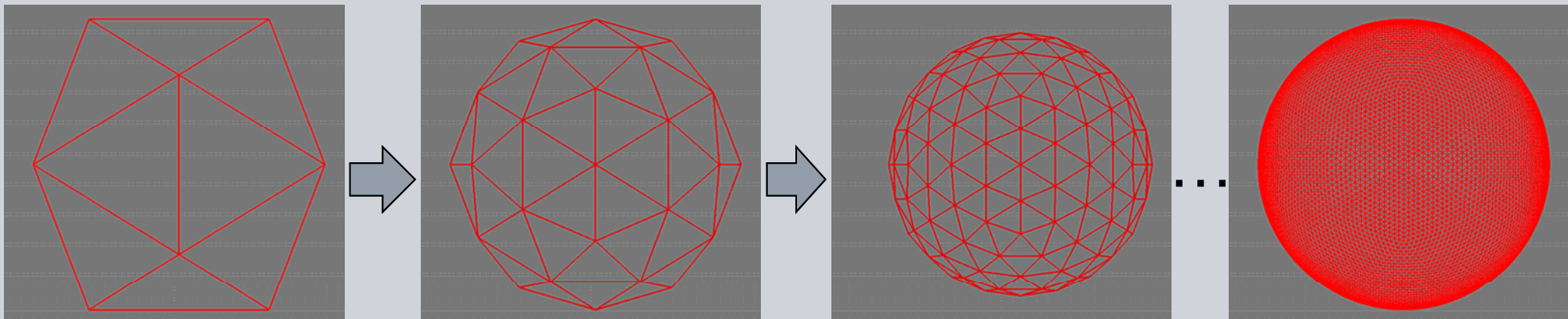
Spherical grid based on discrete polar coordinates

➤ Not uniform!



wikipedia.com

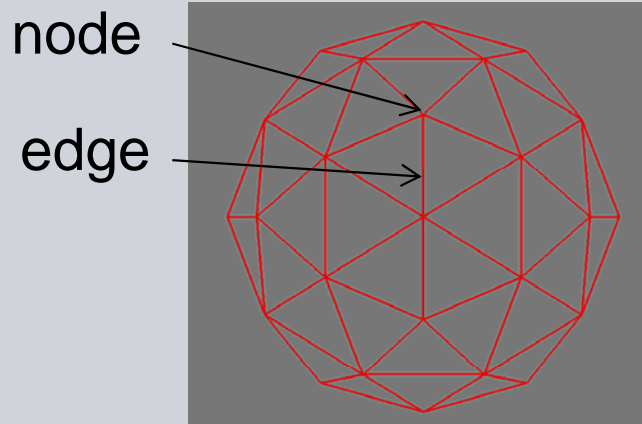
Solution: Recursive triangulation





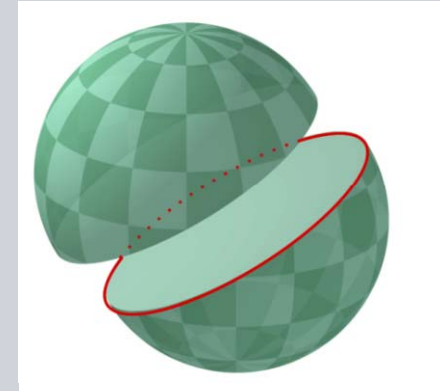
## Milestone 2 – Coronary Distance Maps

Construct a graph  $G = (\text{nodes}, \text{edges})$



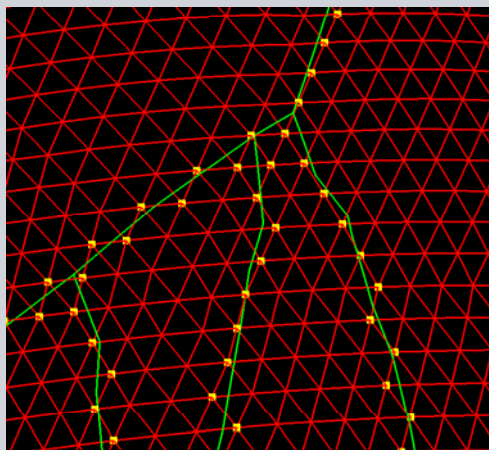
Cost of a graph edge:

- Great circle distance between the two neighboring nodes



wikipedia.com

### Distance Map Computation



- Initialize distance map with infinity
- For each centerline point
  - find the closest node and update its distance
- Run Dijkstra's algorithm

## Milestone 2 – Coronary Density Maps

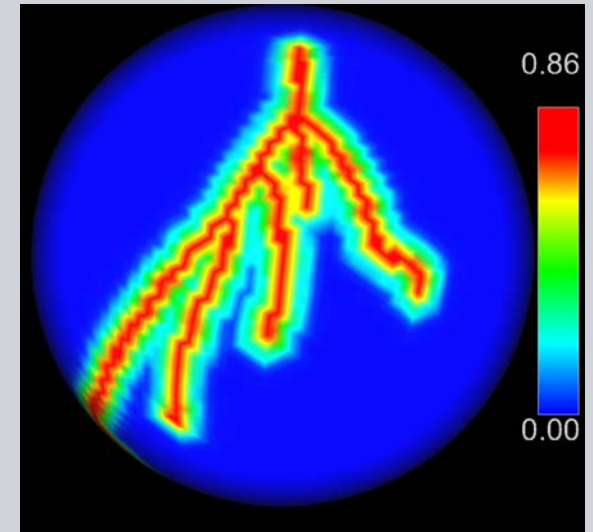
Computed from Gaussian weighting

density

$$\rho(\mathbf{x}) = e^{-\frac{D(\mathbf{x})^2}{\sigma^2}}$$

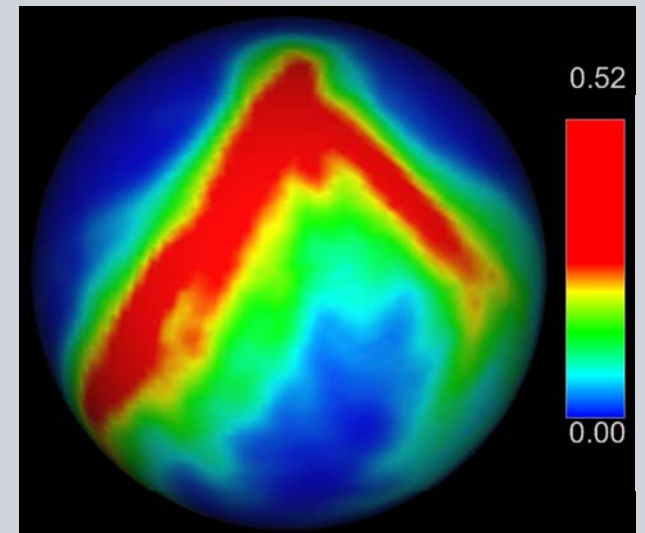
distance

standard deviation (~5 mm)

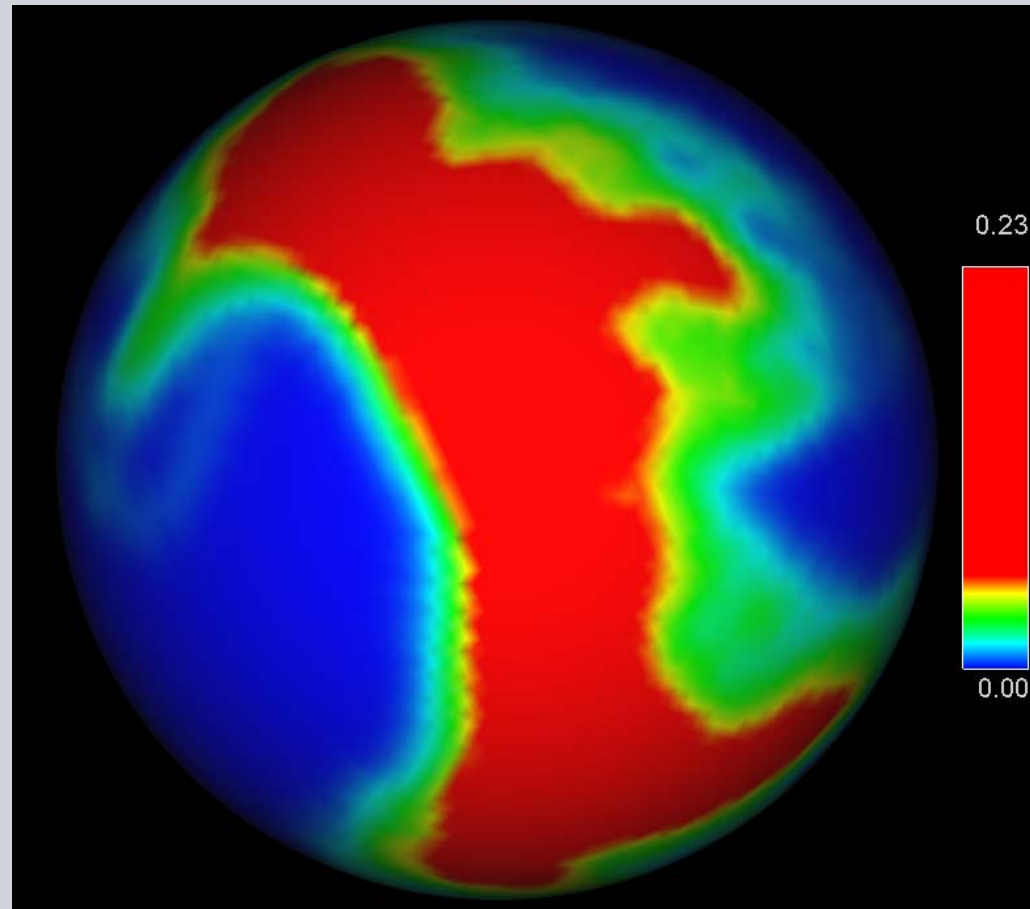


mean density

$$\bar{\rho}(\mathbf{x}) = \frac{1}{N} \sum_{i=1}^N \rho_i(\mathbf{x})$$

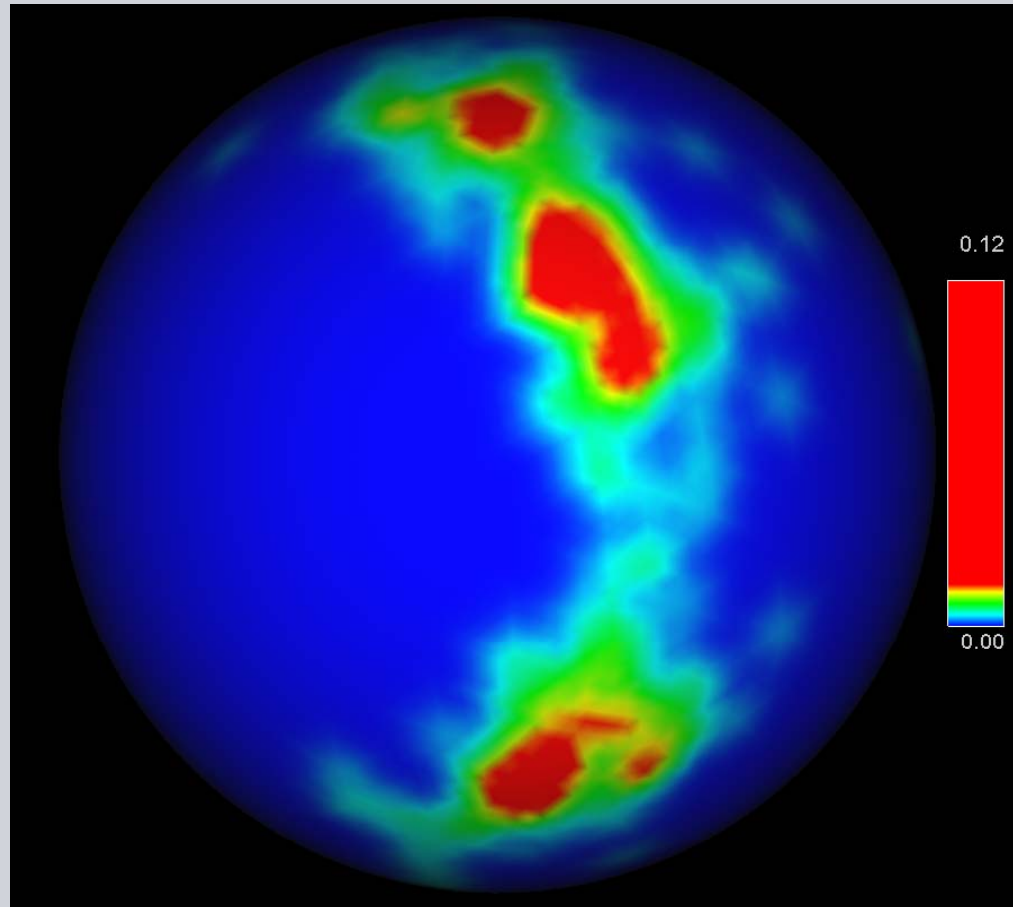


## Milestone 2



Right Coronary Density Map

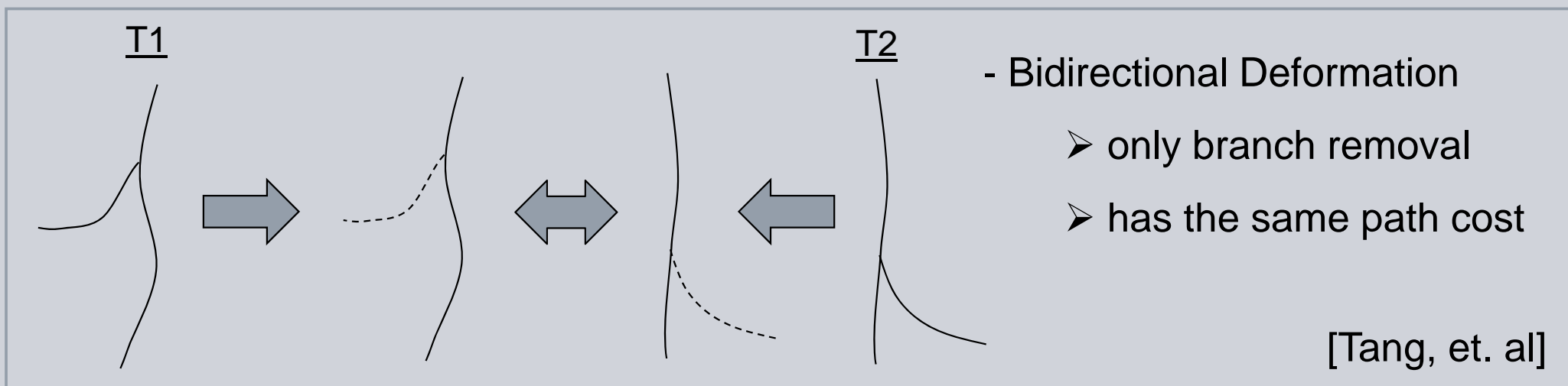
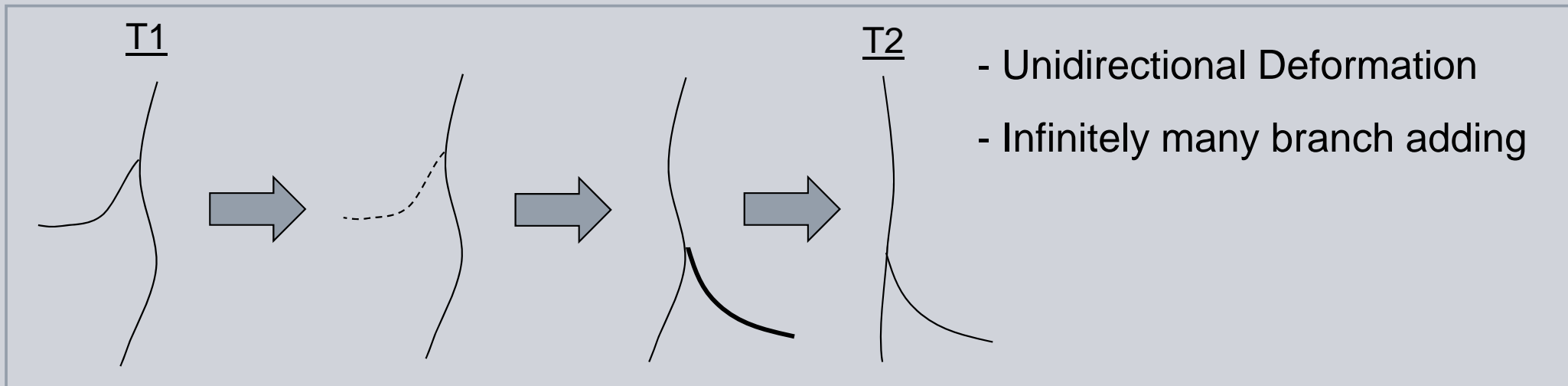
## Milestone 2



Right Bifurcation Density Map

## Milestone 3 – Tree Edit Distance

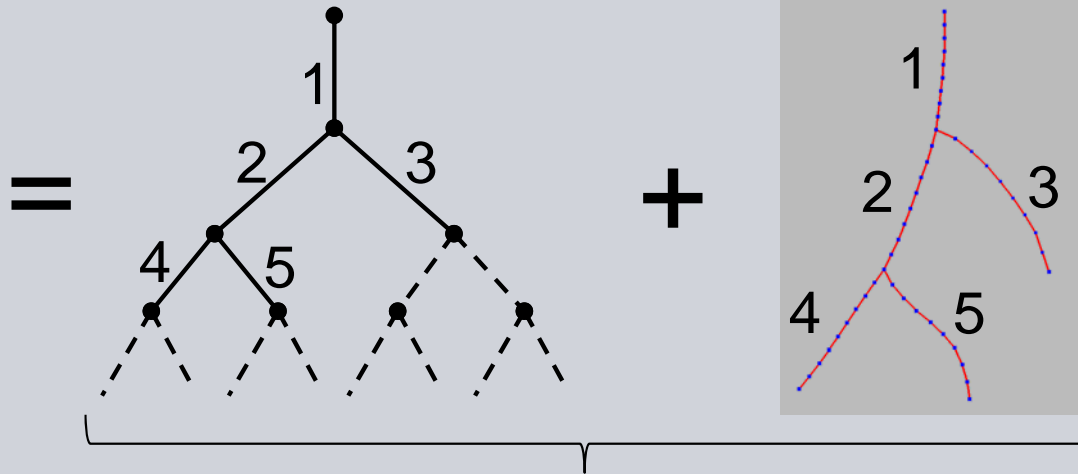
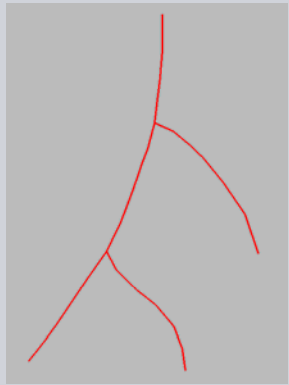
- Match one tree to another by adding, removing or deforming branches with minimal cost



[Tang, et. al]



# Milestone 3 – Tree Representation

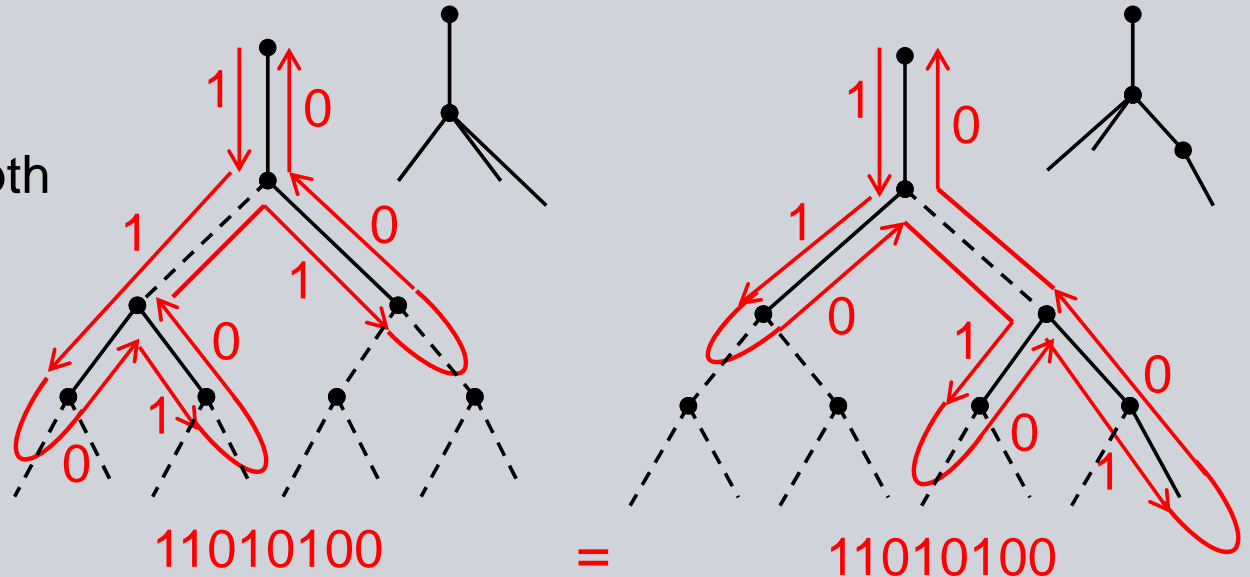


Geometric Tree

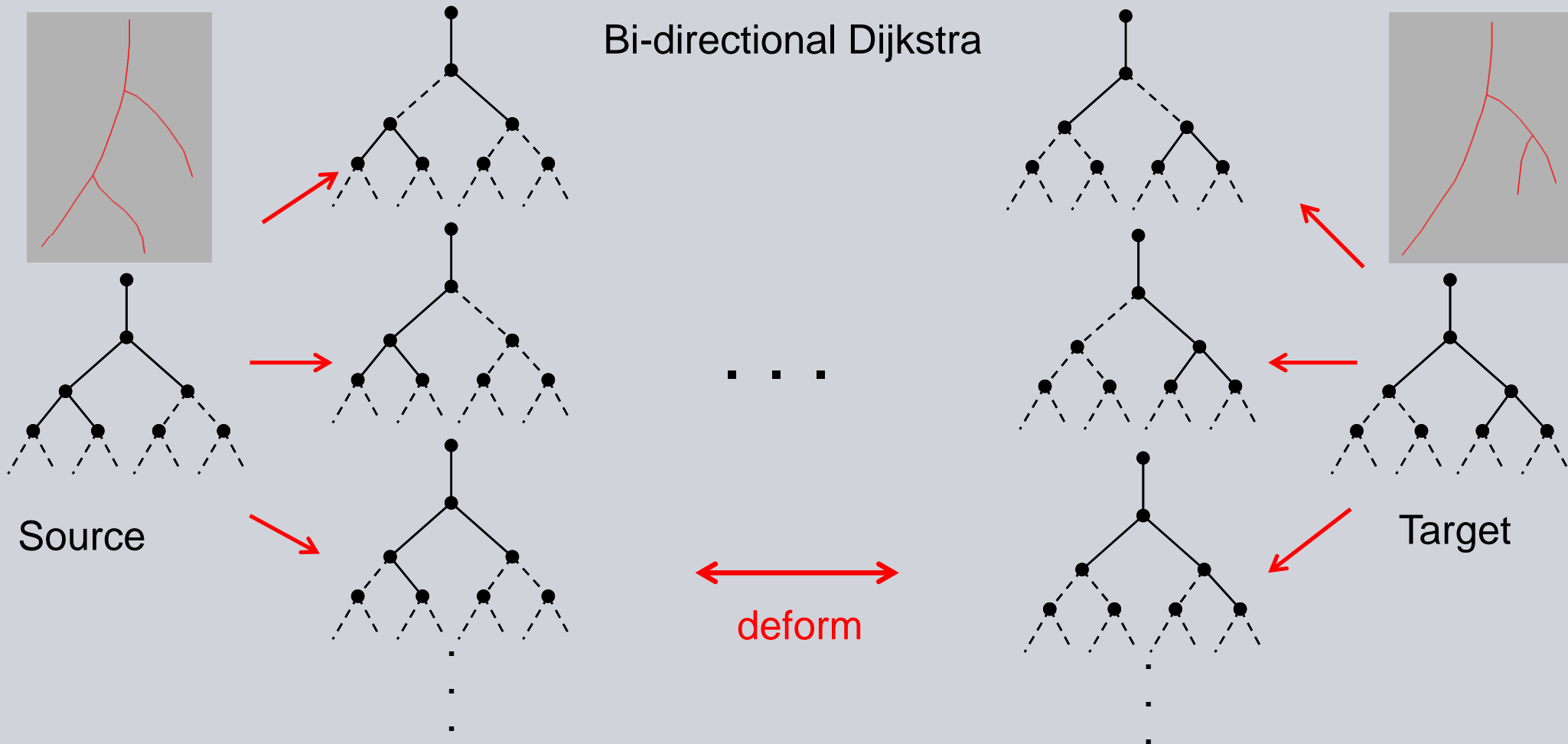
[Feragen, et. al]

## Topology matching

- Tree encoding based on Depth First Search (DFS) order



# Milestone 3 – Finding Least Cost Path



- Branch matching cost: Euclidean distance between landmarks
- Branch removal cost: matching it to a zero length branch

- Runtime 1-2 sec for depth 3 trees

## Deliverables

### Build a research prototype that can

#### Minimum

- align coronary trees in a population ✓
- compute mean coronary density map ✓

#### Expected



- compute TED geodesic between two ~~coronary~~ ordered depth-3 trees ✓
- compute QED geodesic between two ~~coronary~~ ordered depth-3 trees

#### Maximum



- match two coronary trees using TED
- compute average coronary tree in a population using QED
- assign a membership score to an unseen coronary tree using QED

## Dependencies

### Data

- 1 Coronary centerlines, pericardium models and anatomical landmarks 
- 2 Example trees with ground truth matching and geodesic path 

### Software

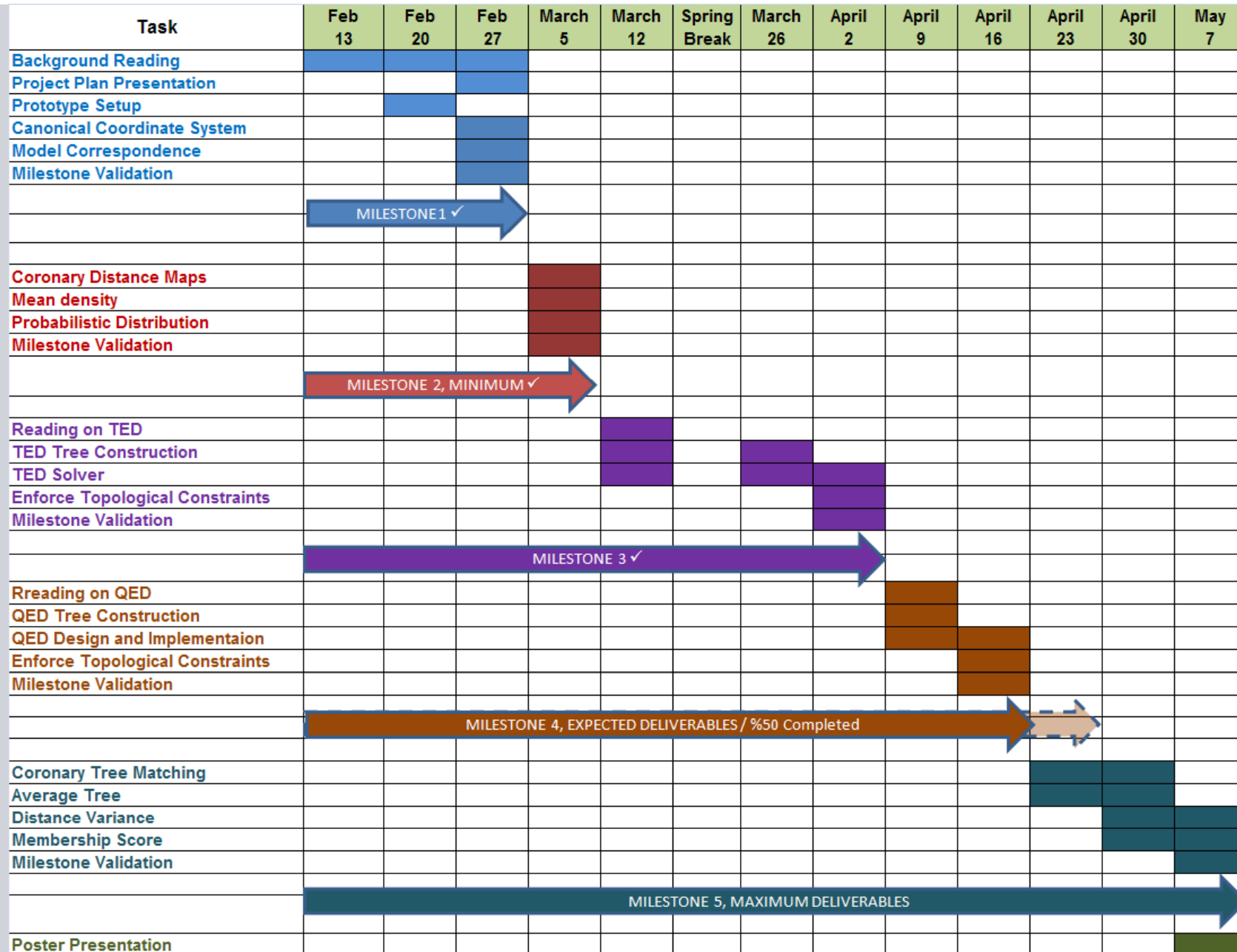
- 1 Prototype development framework → Live demo 
- 2 TED solver pseudo code → Implemented own algorithm 

## Management Plan

- 15 hours work per week.
- Weekly meetings with mentor located in Princeton, phone or in-person. **On schedule**



# Updated Project Timeline



## References

- [1] Donald Lloyd-Jones, Robert J Adams, Todd M Brown, Mercedes Carnethon, Shifan Dai, Giovanni De Simone, T Bruce Ferguson, Earl Ford, Karen Furie, Cathleen Gillespie, and et al. Executive summary: heart disease and stroke statistics–2010 update: a report from the american heart association. *Circulation*, 121(7):188–197, 2010.
- [2] Philip Bille. A survey on tree edit distance and related problems. *Theor. Comput. Sci.*, 337:217–239, June 2005.
- [3] A. Feragen, F. Lauze, and M. Nielsen. Fundamental geodesic deformations in spaces of treelike shapes. In *Pattern Recognition (ICPR), 2010 20th International Conference on*, pages 2089 –2093, aug. 2010.
- [4] Aasa Feragen, Francois Lauze, Pechin Lo, Marleen de Bruijne, and Mads Nielsen. Geometries on spaces of treelike shapes. In *Proceedings of the 10th Asian conference on Computer vision - Volume Part II, ACCV'10*, pages 160–173, Berlin, Heidelberg, 2011. Springer-Verlag.
- [5] Stephen R. Aylward, Julien Jomier, Christelle Vivert, Vincent LeDigarcher, and Elizabeth Bullitt. Spatial graphs for intra-cranial vascular network characterization, generation, and discrimination. In *MICCAI*, pages 59–66, 2005.
- [6] W H Tang and Albert C S Chung. Cerebral vascular tree matching of 3d-ra data based on tree edit distance. *Medical Imaging and Augmented Reality*, page 116123, 2006.
- [7] Aasa Feragen, Søren Hauberg, Mads Nielsen, and François Lauze. Means in spaces of tree-like shapes. In *ICCV*, pages 736–746, 2011.
- [8] Erik D. Demaine, Shay Mozes, Benjamin Rossman, and Oren Weimann. An optimal decomposition algorithm for tree edit distance. *ACM Transactions on Algorithms*, 6(1), 2009.
- [9] A. Feragen, P. Lo, V. Gorbunova, M. Nielsen, A. Dirksen, F. Lauze, and M. de Bruijne. An airway tree-shape model for geodesic airway branch labeling. In *Mathematical Foundations of Computational Anatomy*, 2011.