## Source and Detector Transformation matrices in TREK FluoroSimulator module.

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## 1. Source Transform

The purpose of source transform is to define source position in world coordinate. The transform is composed of three components: orientation, orbital rotation, and angular rotation. Therefore, the transformation could be defined as:

$$
T_{S}=O R_{a}(\alpha) R_{o}(\omega)
$$

where O represents an orientation, $R_{o}$ represents orbital rotation, and $R_{a}$ represents angular rotation. Under an assumption that original source position lies on an x-axis, $R_{o}$ rotates the source about y -axis for an angle $\omega$, and $R_{a}$ rotates the position about an axis $\mathrm{z}^{\prime}$, which is a rotated z-axis, for an angle $\alpha$. Figure 1 describes a view in a direction of a $y$-axis. In figure 2 , axis $z$ ' is defined as a line passing origin and a point $(\mathrm{x}, \mathrm{y}, \mathrm{z})=(\sin \omega, 0, \cos \omega)$, where $\omega$ is an orbital position of C -arm.


Figure 1. Schematic for a rotated z -axis
$R_{a}$ and $R_{o}$ are therefore rotation matrix with angle $\alpha$ and $\omega$ about the axis $(0,1,0)$ and $(\sin \omega, 0, \cos \omega)$. These rotations, however, are valid only if the original source position lies on the x -z plane. To compensate this, there is an orientation matrix $O$ that rotates these transformations to align the transformation with respect to a plane with zero angular position.

## 2. Detector Transformation

Detector transformation is similar to the source transformation. On an X-ray C-arm, detector and source has a fixed source-to-detector distance (SDD) and positioned at the opposite side. Therefore, the detector transformation rotates could be described as a source transformation with additional $\pi / 2$ rotation in either angular or orbital direction. On our system, additional $\pi / 2$ is added in angular position to define the source position. Therefore, source transform TD is:

$$
T_{D}=O R_{a}\left(\alpha+\frac{\pi}{2}\right) R_{o}(\omega)
$$

