

# Robot-Assisted FBG-based Sensorized Needle Calibration

Paper Presentation

Team 6: Kefan Song

Mentors: Iulian Iordachita, Dimitri Lezcano, Jin Seob Kim

# Project Summary

- **Objective:** to calibrate flexible needles with FBG-based shape-sensing capabilities
- **Current problem:** manual needle calibration is very time-consuming and prone to human error
- **Project aim:** to develop an automatic needle calibration process that can be both precise and efficient

# Paper Selection

## Improved FBG-Based Shape Sensing Methods for Vascular Catheterization Treatment

Omar Al-Ahmad, Mouloud Ourak, Jan Van Roosbroeck, Johan Vlekken, and Emmanuel Vander Poorten

# Summary

This paper mainly discusses the methods for fiber integration within catheters to improve shape estimation accuracy and repeatability. It also introduces a two-step calibration process for intrinsic twist compensation and a practical method for fiber parameter identification. An example calibration setup was then demonstrated and validated.

# Overall Structure

- Section I: Introduction
- Section II: Basic Principles
- Section III: Contributors to Shape Accuracy
- Section IV: Experimental Setup
- Section V: Results
- Section VI: Conclusion

# Section I: Introduction

- History and advantages of Fiber Optic Shape Sensing (FOSS)
- Fiber Bragg Gratings (FBGs) vs. Rayleigh scattering
- Optical Frequency Domain Reflectometry (OFDR) vs. Wavelength Division Multiplexing (WDM)
- Basis for Reconstruction methods
  - Frenet-Serret frames
  - Parallel transport frames
  - Constant curvature segmentation
  - Helical geometry

TABLE I  
SHAPE SENSING EXAMPLES FROM PREVIOUS LITERATURE (ALL DIMENSIONS ARE IN MILLIMETRE)

Authors	Interrogation	Fibers & Cores	Conf.	Model	Length	#Grts	Spacing	Validation	Error	$R_{min}$
Abayazid <i>et al.</i> [11]	FBG / WDM	3 outer / no central	Straight	Constant curvature	90	4	30	2D / 3D	$2.10 \pm 1.10$ (mean)	375
Henken <i>et al.</i> [12]	FBG / WDM	3 outer / no central	Straight	Frenet-Serret	70	2	70	2D	$1.32 \pm 0.48$ (mean)	NA
Yi <i>et al.</i> [23]	FBG / WDM	4 outer / no central	Straight	Frenet-Serret	400	5	100	2D / 3D	4.10 (mean)	NA
Elayaperumal <i>et al.</i> [24]	FBG / WDM	3 outer / no central	Straight	Other	85	2	85	2D	4.20 (rms)	NA
Gander <i>et al.</i> [25]	FBG / WDM	4 (MCF) / no central	Straight	Other	NA	NA	NA	2D	2.00 (max)	20
Van de Berg <i>et al.</i> [13]	FBG / WDM	3 outer / no central	Straight	Frenet-Serret	120	4	40	3D	$2.60 \pm 1.10$ (mean)	71.4
Parent <i>et al.</i> [26]	OFDR	3 outer / no central	Straight	Other	NA	NA	NA	2D	$\approx 1.00$ (rms)	17.5
Sefati <i>et al.</i> [14]	FBG / WDM	3 outer / no central	Straight	Constant curvature	NA	NA	NA	3D	0.62 (max)	101.6
Ryu <i>et al.</i> [17]	FBG / WDM	3 outer / no central	Straight	Other	NA	NA	NA	2D	$0.84 \pm 0.62$ (mean)	NA
Leyendecker <i>et al.</i> [27]	FBG / WDM	3 (MCF) / central	Straight	Constant curvature	250	6	50	2D / 3D	15.40 (max)	NA
Lally <i>et al.</i> [28]	OFDR	3 (MCF) / central	Helical	Other	30000	NA	NA	3D	210 (max)	NA
Klute <i>et al.</i> [1]	OFDR	3 outer / no central	Straight	Constant curvature	2000	NA	NA	3D	42.9 (max)	14
Duncan <i>et al.</i> [10]	OFDR	3 (MCF) / no central	Straight	NA	1100	110	10	2D	$22.50 \pm 0.5$ (max)	667
Khan <i>et al.</i> [29]	FBG / WDM	4 (MCF) / no central	Straight	Frenet-Serret	108	6	18	2D / 3D	1.05 (max)	NA
Roesthuis <i>et al.</i> [18]	FBG / WDM	3 outer / no central	Straight	Frenet-Serret	90	4	3	2D	1.14 (mean)	30
Kim <i>et al.</i> [15]	FBG / WDM	3 outer / no central	Straight	Constant curvature	150	NA	NA	3D	0.53 (max)	NA
Wang <i>et al.</i> [30]	FBG / WDM	4 outer / no central	Straight	Frenet-Serret	200	5	50	3D	15.00 (mean)	NA
Moore <i>et al.</i> [2]	FBG / OFDR	3 (MCF) / no central	Straight	Frenet-Serret	1100	111	10	3D	31.06 (max)	14.3
Roesthuis <i>et al.</i> [4]	FBG / WDM	3 outer / no central	Straight	Constant curvature	90	4	30	2D / 3D	1.66 (max)	15

# Section I: Introduction

- Major factors on reconstruction accuracy
- Contributions in this paper
  - Fiber integration approach into a catheter
  - Two-step calibration method for intrinsic twist
  - Approach for spatial curve reconstruction
  - Parameter identification method
  - Validation process of all the methods

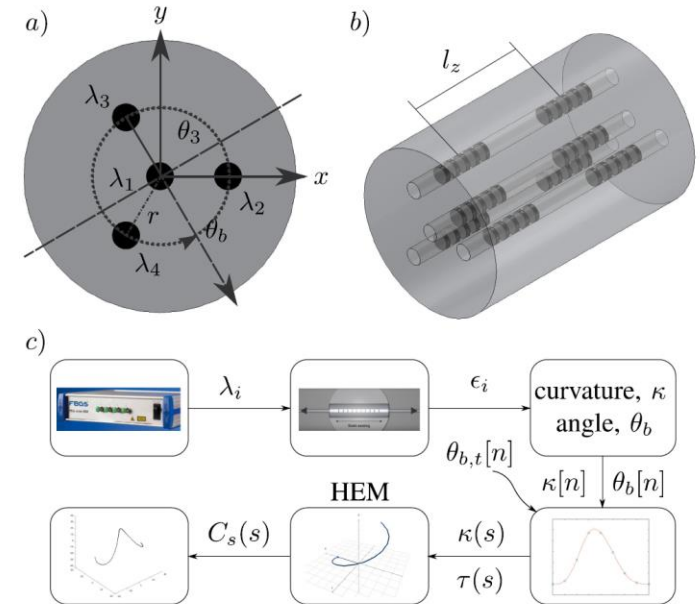
# Section II: Basic Principles

## 1. Principles behind FBG sensors

$$\epsilon = -\kappa y$$

$$\frac{\lambda_B - \lambda_{B_0}}{\lambda_{B_0}} = \frac{\Delta\lambda_B}{\lambda_{B_0}} = S_\epsilon \Delta\epsilon + S_T \Delta T$$

$$\Delta\epsilon_i = \frac{\Delta\lambda_{B,i}}{S_\epsilon \lambda_{B_0,i}} - \frac{\Delta\lambda_{B,1}}{S_\epsilon \lambda_{B_0,1}}$$





# Section II: Basic Principles

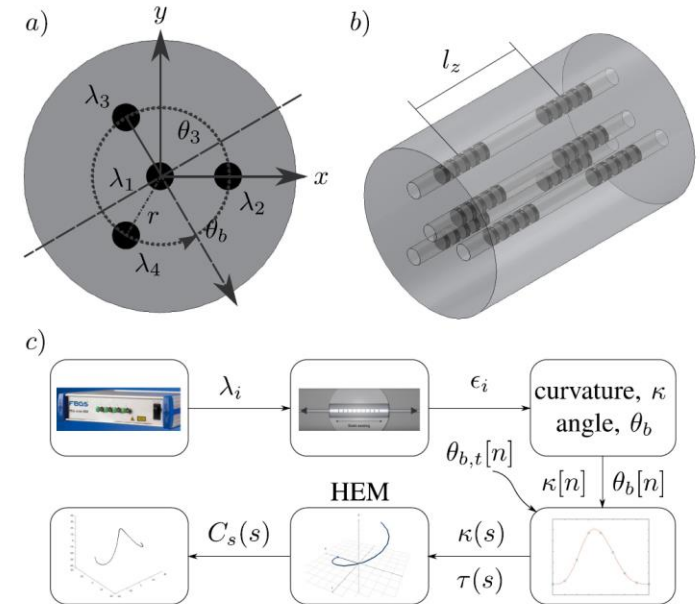
## 2. Strain, curvature and Bend Angle

$$\epsilon_i = -\kappa r \sin(\theta_b - 3\pi/2 - \theta_i)$$

$$\mathbf{\kappa}_{app} = -\sum_{i=1}^N \frac{\epsilon_i}{r} \cos \theta_i \hat{\mathbf{i}} - \sum_{i=1}^N \frac{\epsilon_i}{r} \sin \theta_i \hat{\mathbf{j}}$$

$$\kappa = \frac{2|\mathbf{\kappa}_{app}|}{N},$$

$$\theta_b = \angle \mathbf{\kappa}_{app},$$



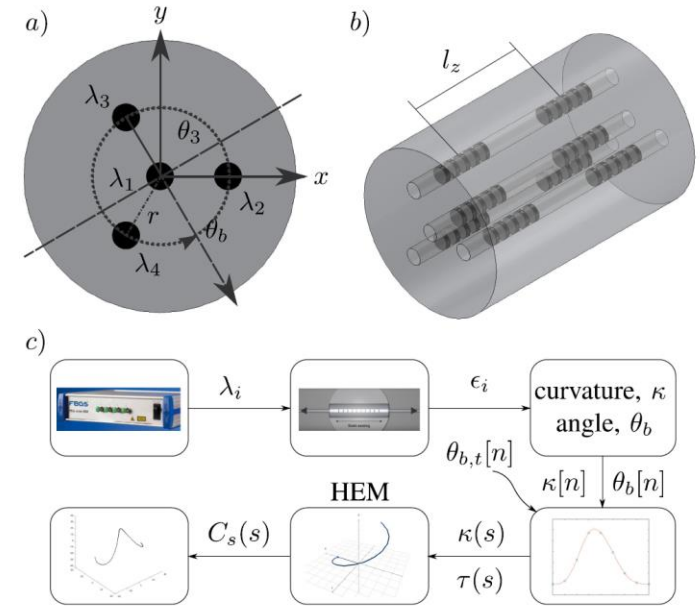
# Section II: Basic Principles

## 3. Shape Reconstruction

- Frenet-Serret formula

$$\begin{aligned}\frac{d\mathbf{T}}{ds} &= \kappa\mathbf{N}, \\ \frac{d\mathbf{N}}{ds} &= -\kappa\mathbf{T} + \tau\mathbf{B}, \\ \frac{d\mathbf{B}}{ds} &= -\tau\mathbf{N},\end{aligned}$$

$$C_s(s) = C_{s,0} + \int_0^l \mathbf{T}(s) ds$$



# Section III: Contributors to Shape Accuracy

- interrogation method
- fiber integration method
- presence of twist compensation
- calibration for twist compensation
- parameter identification
- reconstruction algorithm

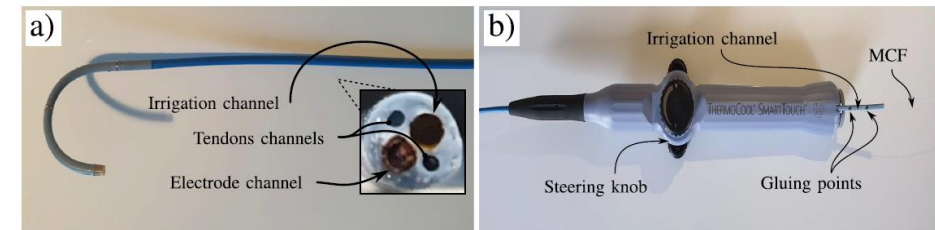
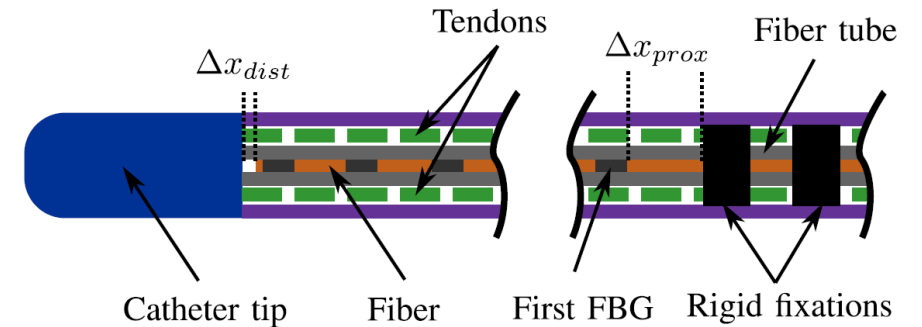
# Section III: Contributors to Shape Accuracy

- **interrogation method: WDM vs. OFDR**

	<b>WDM</b>	<b>OFDR</b>
Spatial resolution	Lower (~1mm)	Extremely high (~10 $\mu$ m)
Refresh rate	High	Not as high
SNR	High	Not as high
Cost	Cheaper	More expensive
Wavelength measurement accuracy	More accurate	Less accurate

# Section III: Contributors to Shape Accuracy

- **fiber integration method**
- 3 guidelines:
  - reducing the spacing between the multiple-core fiber (MCF) and the inner lumen of the catheter
  - including one or two rigid fixations at the base of the MCF with distance  $\Delta x_{prox}$  to the closest FBG grating
  - attaching the MCF at a location where its tip is at distance  $\Delta x_{dist}$  away from the tip of the catheter



# Section III: Contributors to Shape Accuracy

- **presence of twist compensation**
- Fiber is more sensitive in sensing the strain caused by the twist
- Intrinsic twist is present in FBG fibers even when they are not externally loaded. Mechanical design is necessary to reduce the twist.

# Section III: Contributors to Shape Accuracy

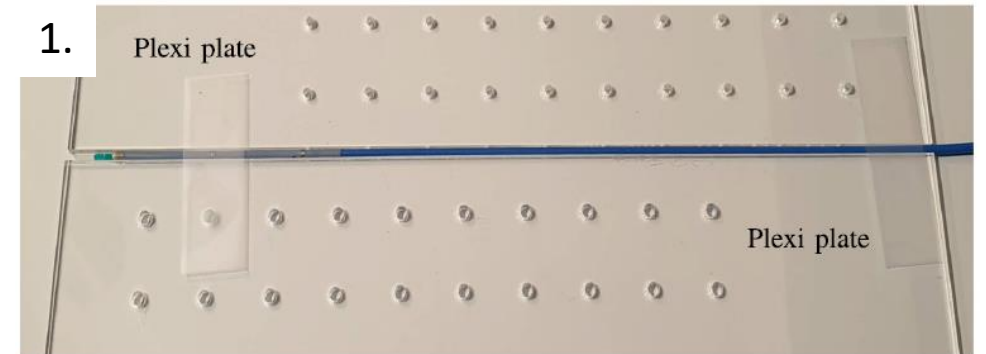
- **calibration for twist compensation**
- 2-step procedure proposed

$$\Delta\epsilon_i = \frac{\Delta\lambda_{B,i}}{S_\epsilon\lambda_{B_0,i}} - \frac{\Delta\lambda_{B,1}}{S_\epsilon\lambda_{B_0,1}}$$

$$\mathbf{\kappa}_{app} = -\sum_{i=1}^N \frac{\epsilon_i}{r} \cos\theta_i \hat{\mathbf{i}} - \sum_{i=1}^N \frac{\epsilon_i}{r} \sin\theta_i \hat{\mathbf{j}}$$

$$\kappa = \frac{2|\mathbf{\kappa}_{app}|}{N},$$

$$\theta_b = \angle\mathbf{\kappa}_{app},$$



# Section III: Contributors to Shape Accuracy

- **parameter identification**
- Procedure proposed
  1. Position in various ground-truth scenarios

2. Minimize the cost function: 
$$C(\Theta) = \sum_{i=1}^k \max(\mathbf{d}(C_{s,gr}(s, k) - C_{s,rc}(s, k, \Theta)))$$

for  $\Theta$  subject to

$$\left\{ \begin{array}{l} \Theta = [\Delta\theta, r, S_\epsilon], \\ \Delta\theta_{\min} \leq \Delta\theta \leq \Delta\theta_{\max}, \\ r_{\min} \leq r \leq r_{\max}, \\ S_{\epsilon, \min} \leq S_\epsilon \leq S_{\epsilon, \max}, \end{array} \right.$$

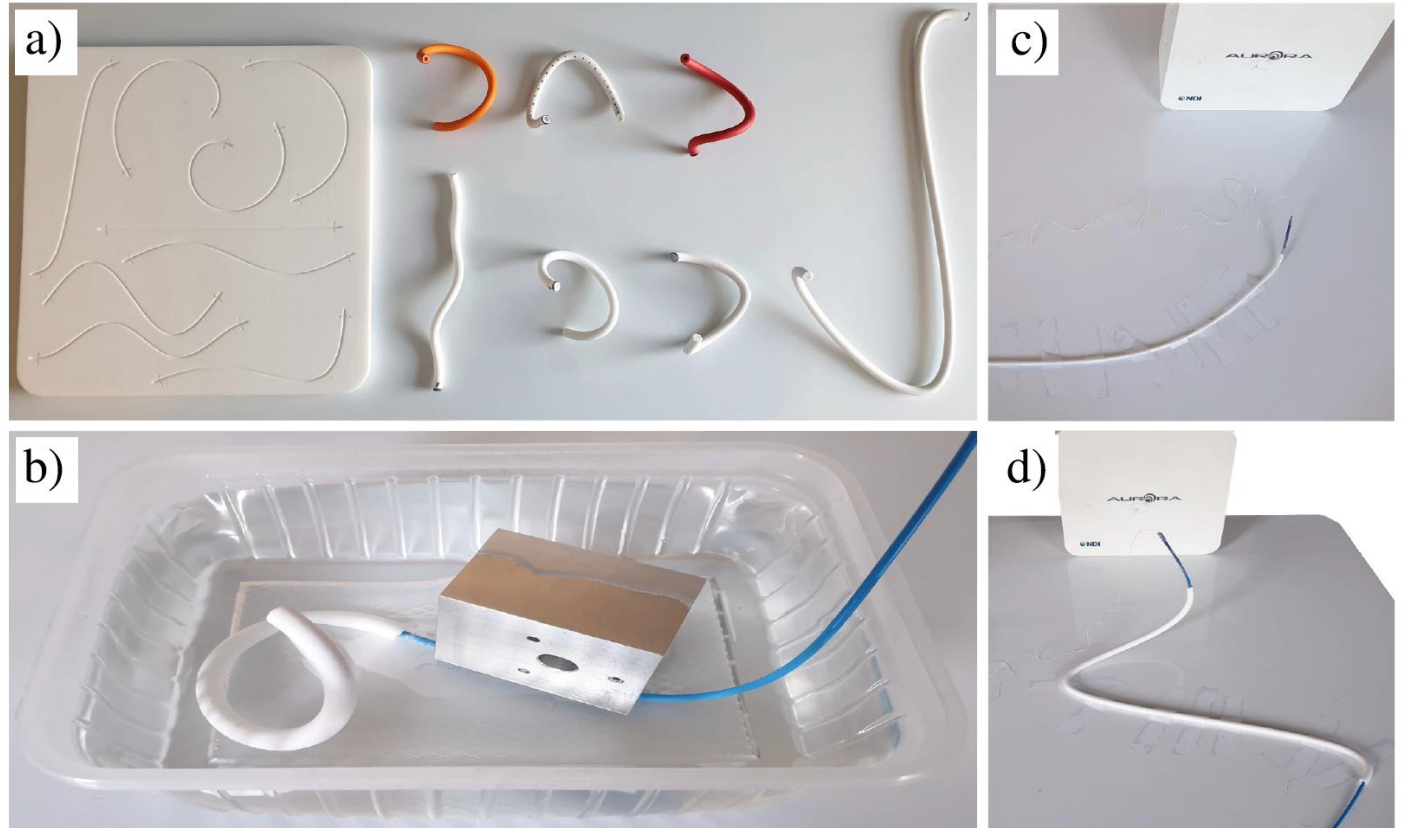


# Section III: Contributors to Shape Accuracy

- **reconstruction algorithm**
- 3 modifications:
  - code for twist compensation
  - construct the spatial curve using the Helical Extension Method
  - compare different interpolation techniques and employ one with the best performance

# Section IV: Experimental Setup

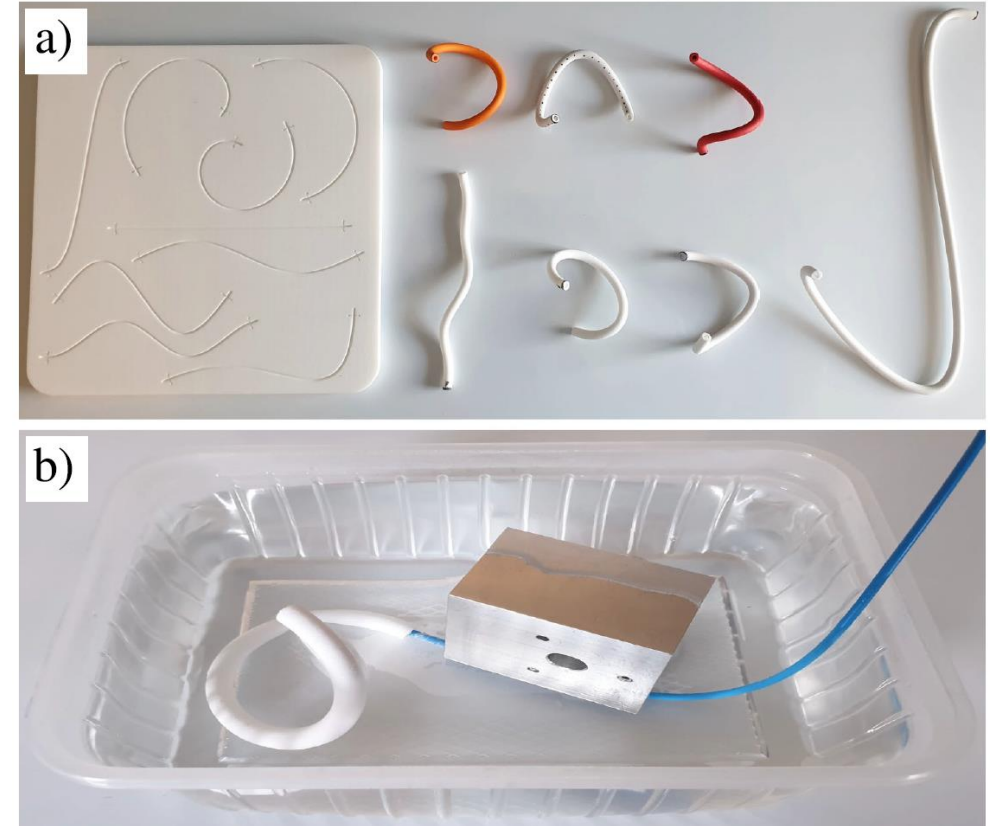
- Static tests (left)
- Dynamic tests(right)



# Section IV: Experimental Setup

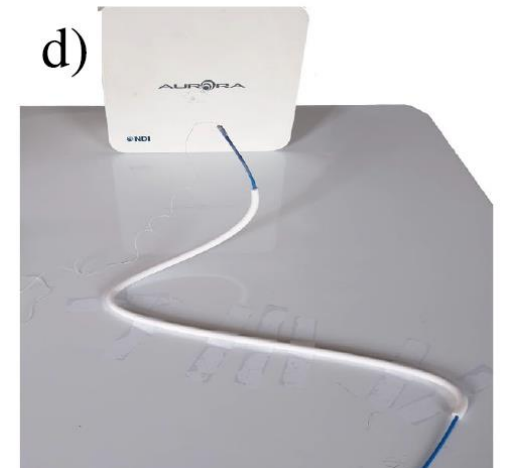
- **Static tests**

1. Parameter optimization  
12 shapes x 5 insertions each  
Half for optimization, half for validation
2. Temperature variation  
Submerge catheter in hot water bath



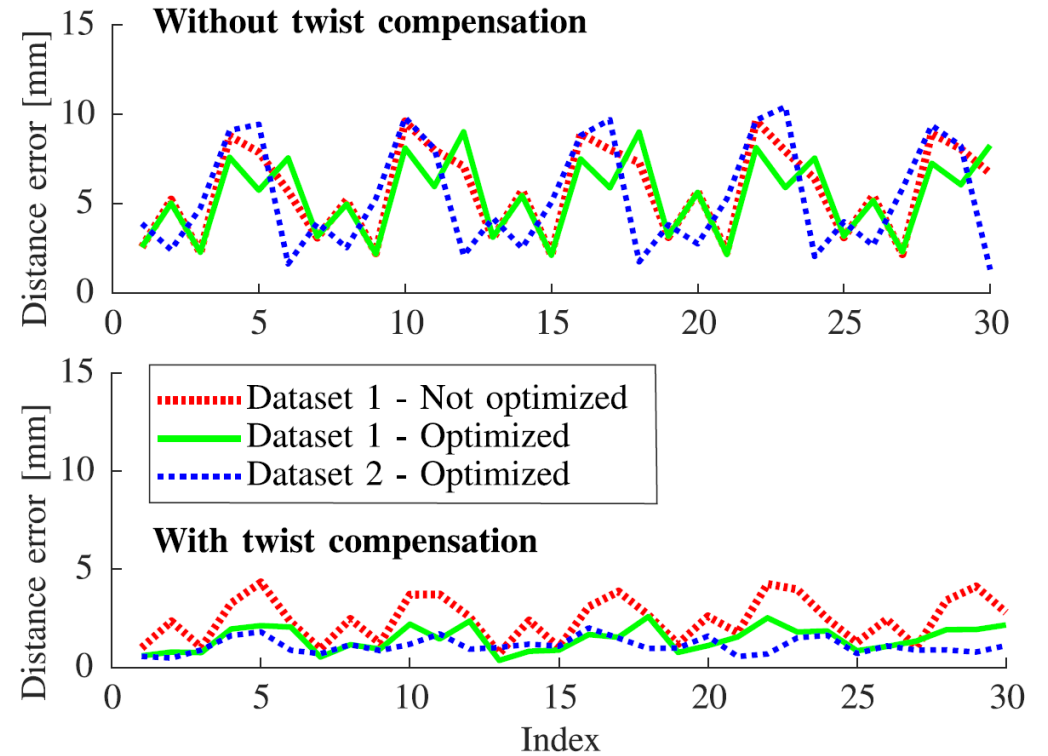
# Section IV: Experimental Setup

- **Dynamic tests**
- EM sensor fixed at the tip
- 4 effects to be tested
  - Longitudinal catheter rotation
  - Repeatability
  - Tendon actuation
  - Dynamic catheter movement



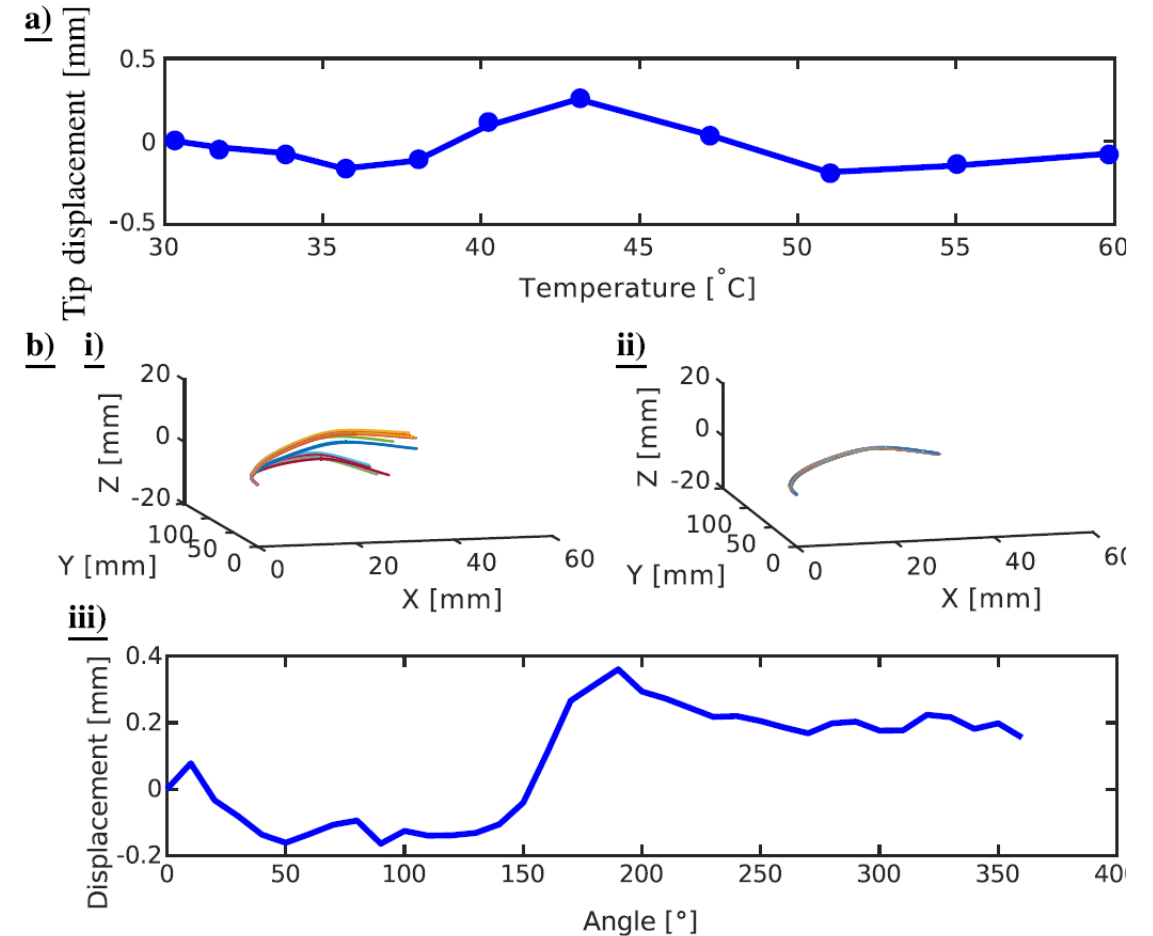
# Section V: Results

- Parameter optimization improves accuracy
- Twist compensation improves accuracy
- Optimized parameters perform well for shapes excluded from optimization (data2)



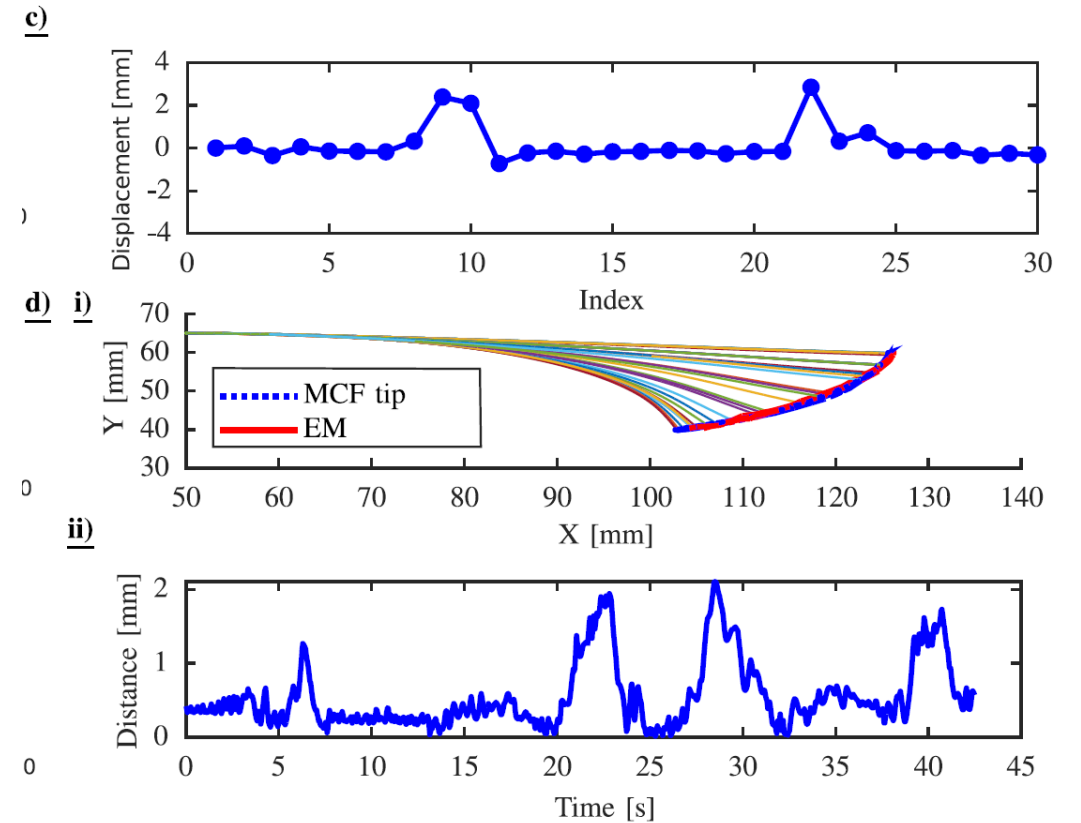
# Section V: Results

- variation caused by temperature is mostly uniform and are almost negligible
- rotation induces negligible twist and has no major effect on shape accuracy



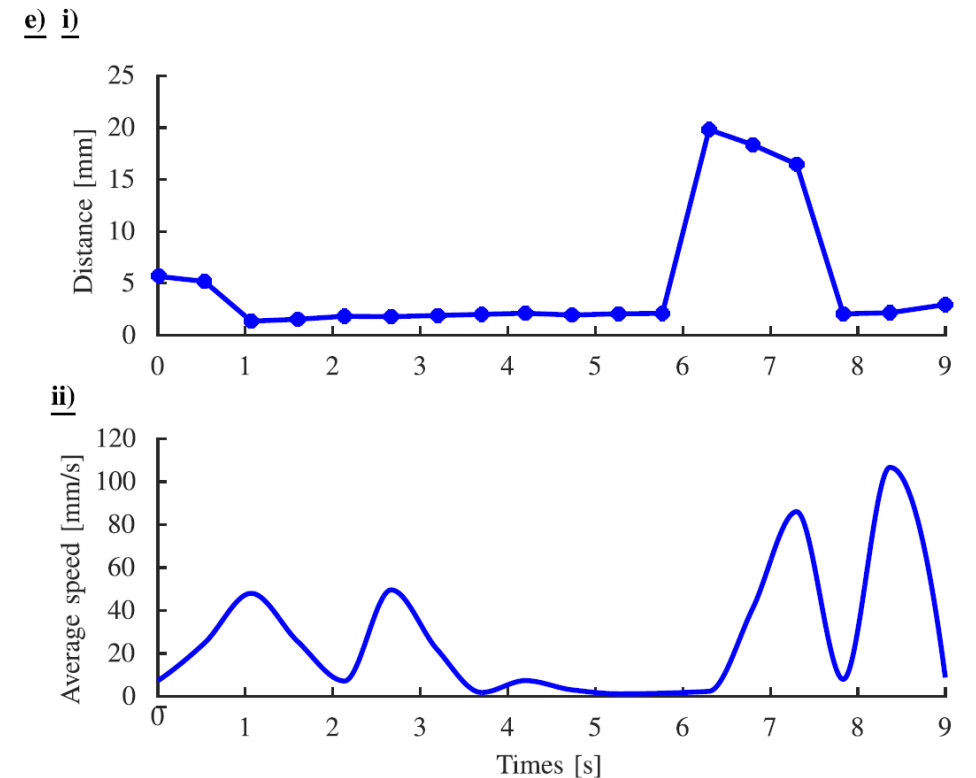
# Section V: Results

- excellent repeatability, result will likely improve in real-life settings
- shape reconstruction is not affected by tendon actuation



# Section V: Results

- distance error increases when there's sharp bends
- could be mitigated by applying lubrication in the sheath, and to use larger FBG spacing to avoid wavelength overlap in the spectrum





# Section VI: Conclusion

- This paper explored the effect of multiple factors on the accuracy of shape reconstruction of an FBG-based catheter. It also proposed several different algorithms to mitigate the possible errors. Through experiment, it shows that when applying these calibration algorithms, the FBG-based catheter is able to reconstruct the shape pretty accurately.

# Critiques

## Pros:

- Easy to follow
- Well structured
- Equations are clear
- Detailed explanation of the experiment

## Cons

- No classification of good and bad FBG sensors

# Takeaways

- Good general guidance
- Principles are applicable
- Good reference experiment

# References

- Seifabadi, R., Iordachita, I., & Fichtinger, G. (2012, June). Design of a teleoperated needle steering system for MRI-guided prostate interventions. In 2012 4th IEEE Ras & Embs International Conference on Biomedical Robotics And Biomechatronics (Biorob) (pp. 793-798). IEEE.
- Al-Ahmad, O., Ourak, M., Van Roosbroeck, J., Vlekken, J., & Vander Poorten, E. (2020). Improved FBG-Based Shape Sensing Methods for Vascular Catheterization Treatment. IEEE Robotics and Automation Letters, 5(3), 4687-4694.