

Seminar on Statistical Anatomic Models,  
Registration, and Reconstruction  
2011/1/27

# GPU-accelerated Registration/Reconstruction Toolkit and its Application to 2D/3D registration

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# Acknowledgements

## Advisers

- Russell H. Taylor
- Mehran Armand
- Peter Kazanzides
- Jeffrey H. Siewerdsen

## Collaborators

### JHU/CISST

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- Wen Liu
- Ben X. Kang

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- Robert Armiger
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### Bayview

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- Stephen Belkoff

### I-STAR lab

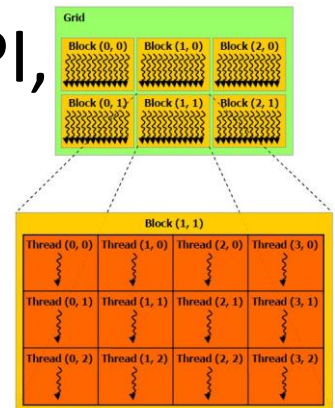
- J. Web Stayman
- Wojtek Zbijewski
- Sebastian Schafer
- Junghoon Lee
- Ali Uneri
- Sureerat Reaungamornrat
- Sajendra Nithiananthan
- Daniel Mirota

# Outline

1. Development of the GPU reg./recon. toolkit
  - Motivation
  - Purpose
  - Implementation detail
  - Example applications
  - Future work
2. An application of the toolkit: Intensity-based rigid 2D/3D registration
  - Implementation and experimental evaluation

# Motivations

- Many components of registration/reconstruction researches overlap and usually computationally intensive.
  - e.g. DRR generation (forward projection), back projection, resampling, etc.
- Why don't we implement those components on GPU with an unified interface?
- Matlab-friendliness is important for research
- Shared library, cross-platform, intuitive API, modular design, multi-GPU support are preferable...

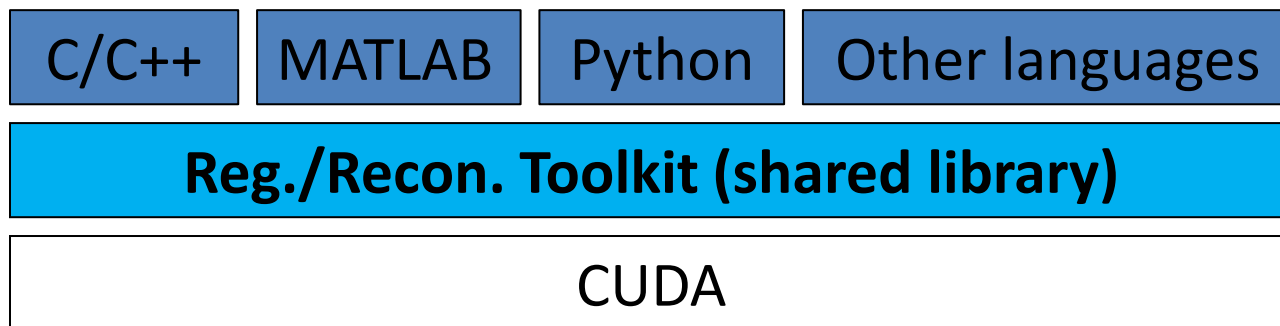


Cited from

NVIDIA CUDA Programming Guide

# Purpose

- To develop a cross-platform shared toolkit with GPU-acceleration, which helps registration/reconstruction researches.



Software architecture

# Overview of the Toolkit

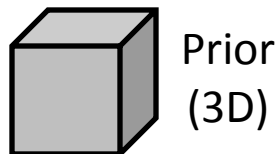
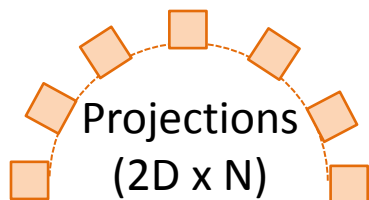
- One shared library (named “FBProjector.dll”)
- Almost all code in the library are implemented from scratch
  - Exceptions
    - FDK filtering – collaboration with Dr. Sebastian Schafer
    - MI computation on GPU – open source (written by Ramtin Shams)
- Source files and sample code
  - [https://svn.lcsr.jhu.edu/yotake2/C++/CUDA\\_Programs/FBProjectorDll](https://svn.lcsr.jhu.edu/yotake2/C++/CUDA_Programs/FBProjectorDll)
- Dependency
  - CUDA Toolkit ([http://developer.nvidia.com/object/cuda\\_3\\_2\\_toolkit\\_rc.html](http://developer.nvidia.com/object/cuda_3_2_toolkit_rc.html))
- Supported platform
  - Developed and tested mainly on Windows, but it should work on other platform, probably...
  - A little more details are on I-STAR wiki
    - <https://trac.lcsr.jhu.edu/istar/wiki/Projectors>

# Key components in the Toolkit

- Already implemented on the GPU
  - Forward projector (DRR generator)
  - Back projector (Voxel-driven & Ray-driven)
  - Resampler / Interpolator
  - Similarity measure computation (not optimized yet)
    - Mutual information (MI), Normalized mutual information (NMI), Gradient information (GI), Gradient correlation (GC), Normalized cross correlation (NCC), Mean square distance (MSD).
  - FDK filtering
- To be implemented... (currently Matlab is used)
  - Optimizer

# Application scenarios

## (1) 3D/2D Rigid Registration



## (2) 3D/3D Rigid Registration

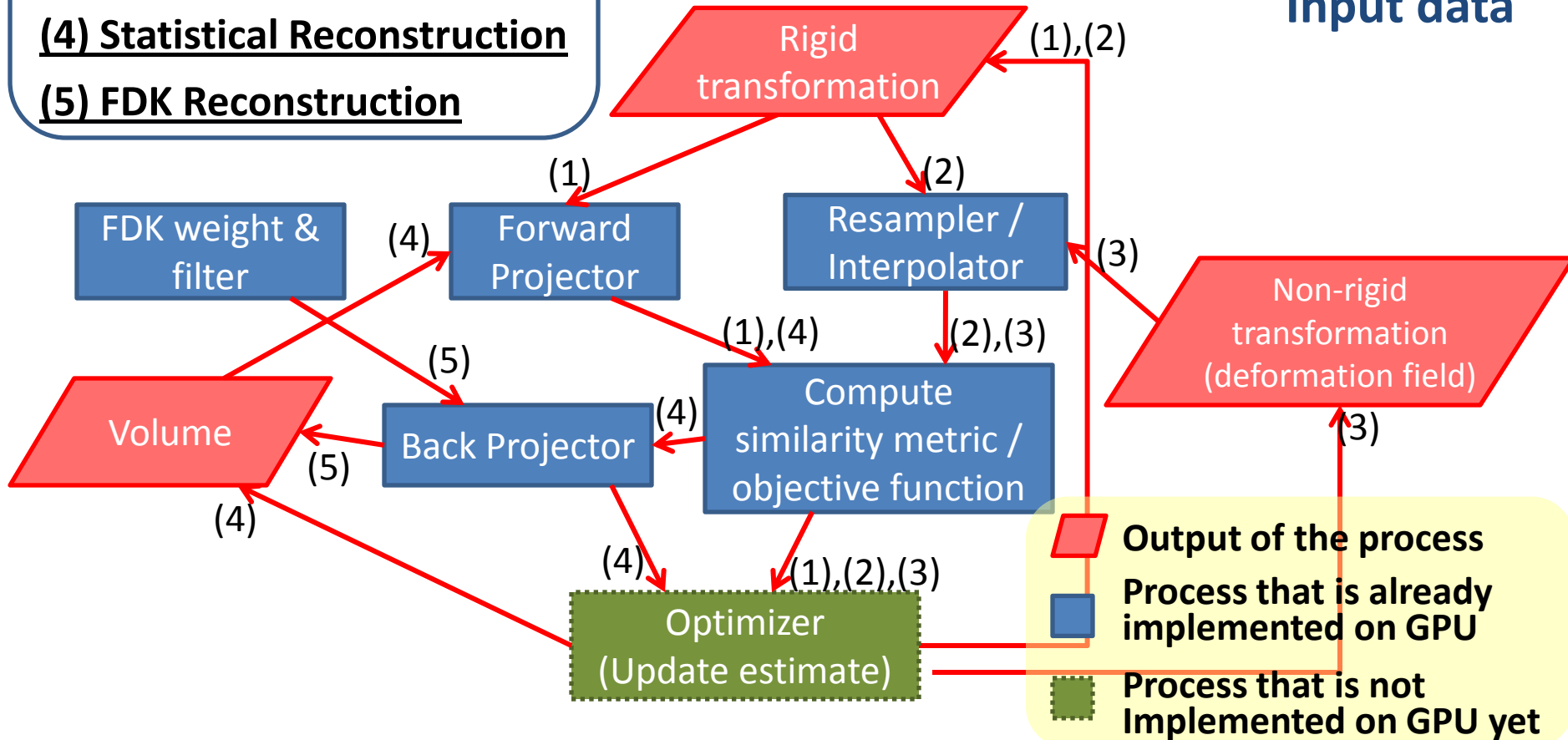
## (3) 3D/3D Non-Rigid Registration



**Input data**

## (4) Statistical Reconstruction

## (5) FDK Reconstruction





# Application scenarios

	2D/3D rigid reg.	3D/3D rigid reg.	3D/3D non-rigid reg.	Stat. recon.	FDK recon.
Input	2D x $N$ (fixed) + 3D (moving)	3D (fixed) + 3D (moving)	3D (fixed) + 3D (moving)	2D x $N$	2D x $N$
Optimization process	Forward project	Resample	Apply $D$ (resample)	Forward project	
	Compute similarity measure	Compute similarity measure	Compute gradient	Compute (curvature?)	FDK weighting & filtering
				Back project	Back project
	Update $T$	Update $T$	Update $D$	Update $V$	
Output	$T$	$T$	$D$	$V$	$V$

$N$ : Number of projection images

$T$ : Rigid transformation

$V$ : Volume (3D)

$D$ : Deformation field

# Example MATLAB interface

```
% Initialize dll instance
dllHandle = FBProjectorDll_wrapper( 'FBProjectorDll' );
dllHandle.CreateFBProjectorInstance(imageSize);
dllHandle.InitializeProjectorParameters(1, ... % intensity window
    0, ... % intensity level
    1.0, ... % step size (ignored in siddon mode)
    1) % 1: siddon mode, 0: trilinear interpolation mode
```

Initialization

```
% set volume data
dllHandle.InitializeInputData_CT( volume );
dllHandle.SetVolumeInfo(volumeSize, voxelSize);
```

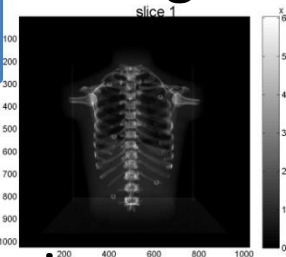
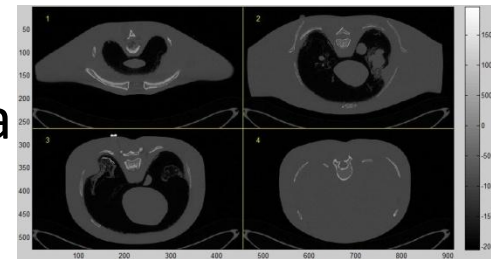
Volume data  
setting

```
% X-ray projection geometry setting
dllHandle.InitializeProjectionParametersArray(numProj);
for i=1:100
    projectionGeometry = struct('DetectorFrame', DetectorFrame(:,i), ...
        'SourcePosition', SourcePosition(:,i), ...
        'IsPerspective', 1, 'FOV', fov);
    dllHandle.SetProjectionParameter_objectOriented(i-1, projectionGeometry);
end
```

Geometry  
setting

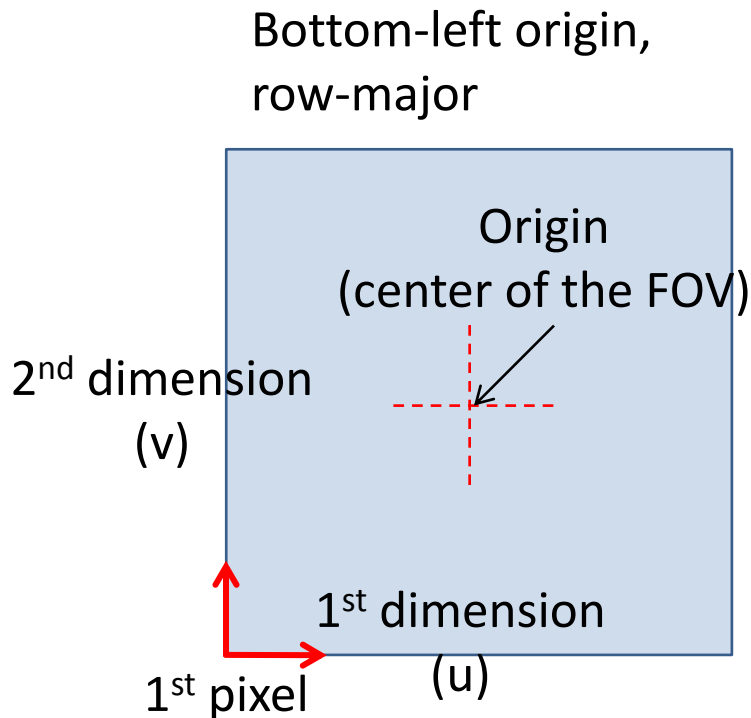
```
% Compute DRR
dllHandle.ForwardProjection( imageBufferPtr );
DRRs = reshape( get(imageBuffer.Data, 'value'), [imageSize numProj] );
```

DRR  
generation

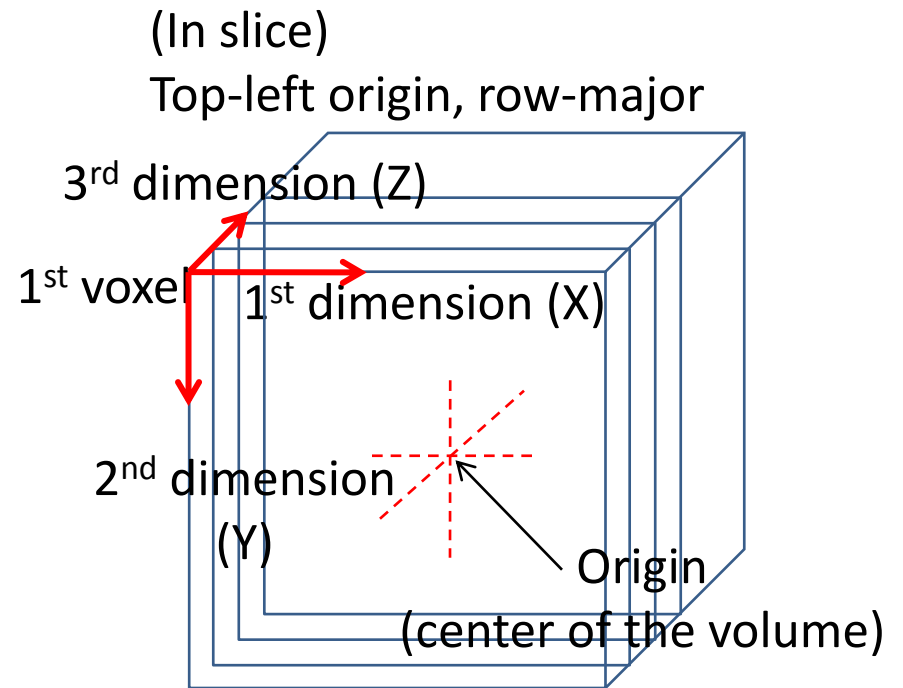


# Pixel/voxel order used in the library

For projection (2D)



For volume (3D)



# Example C/C++ interface

```
// Initialize dll instance
```

```
FBProjectorInstance fbProjector;
```

```
CreateFBProjectorInstance(&fbProjector, WIDTH, HEIGHT, false, err_str);
```

```
SetWindowLevel(fbProjector, WINDOW, LEVEL, err_str);
```

```
SetStepSize(fbProjector, 1.0, err_str);
```

```
SetIsSiddon(fbProjector, true, err_str);
```

} Initialization

```
// set volume data
```

```
float *volume; // see the previous slide for the voxel order
```

```
InitializeInputData_CT(fbProjector, volume, w, h, d, 1, err_str);
```

```
SetVolumeInfo(fbProjector, w, h, d, vox_w, vox_h, vox_d, err_str);
```

} Volume data setting

```
// X-ray projection geometry setting
```

```
InitializeProjectionParametersArray(fbProjector, NUM_PROJECTION, err_str);
```

```
ProjectionParameters_cameraOriented projectionGeometry;
```

```
for(int i=0;i<NUM_PROJECTION;i++){
```

```
    // Geometry setting on projectionGeometry
```

```
    SetProjectionParameter_cameraOriented(fbProjector, i, projectionGeometry, err_str);
```

```
}
```

} Geometry setting

```
// Compute DRR
```

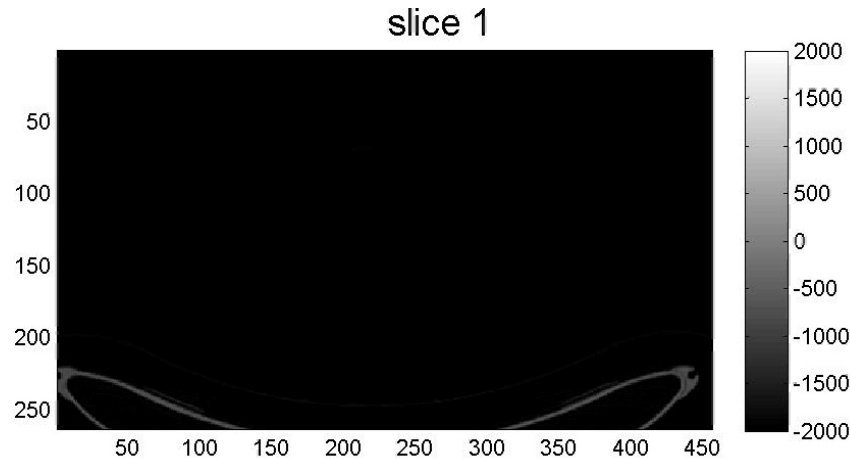
```
PackedDynamicFloatMatrix DRRs;
```

```
InitializePackedDynamicFloatMatrix(&DRRs);
```

```
ForwardProjection(fbProjector, &DRRs, err_str);
```

} DRR generation

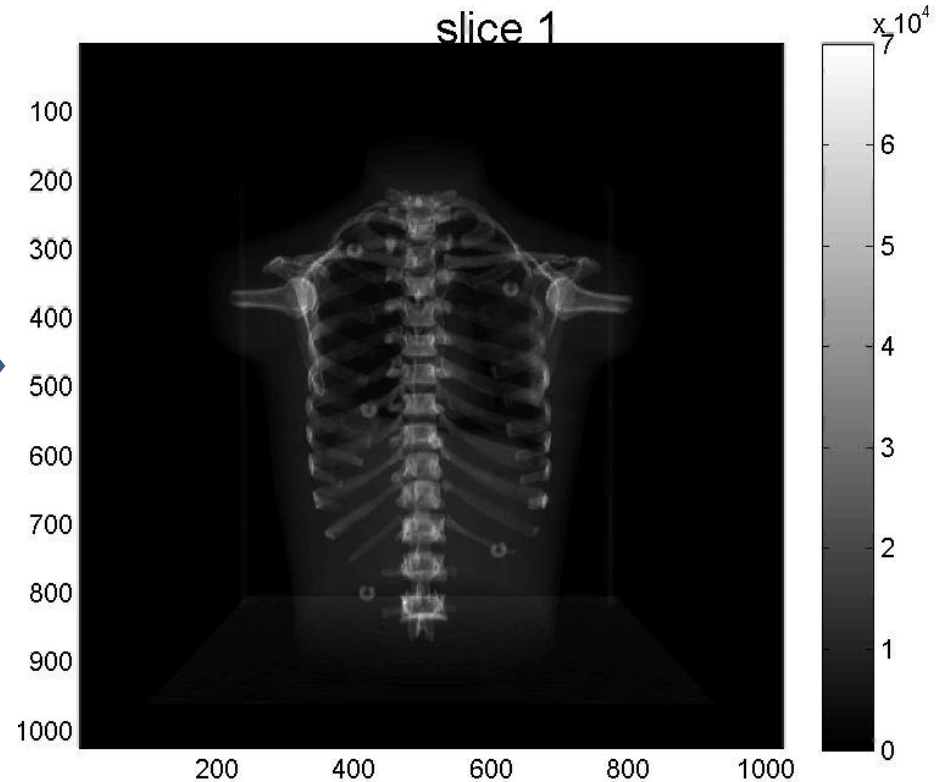
# Performance example



456×263×494 (1.0mm<sup>3</sup>)

## Hardware specifications

Operating System	Windows Vista 64 bit
Processor type	Intel® Core™ 2 Duo
CPU clock frequency (GHz)	2.66
Graphics card type	NVIDIA® Quadro® FX3700M
No. processors core	128
Memory bandwidth (GB/s)	51.2
Graphics memory (MB)	1024



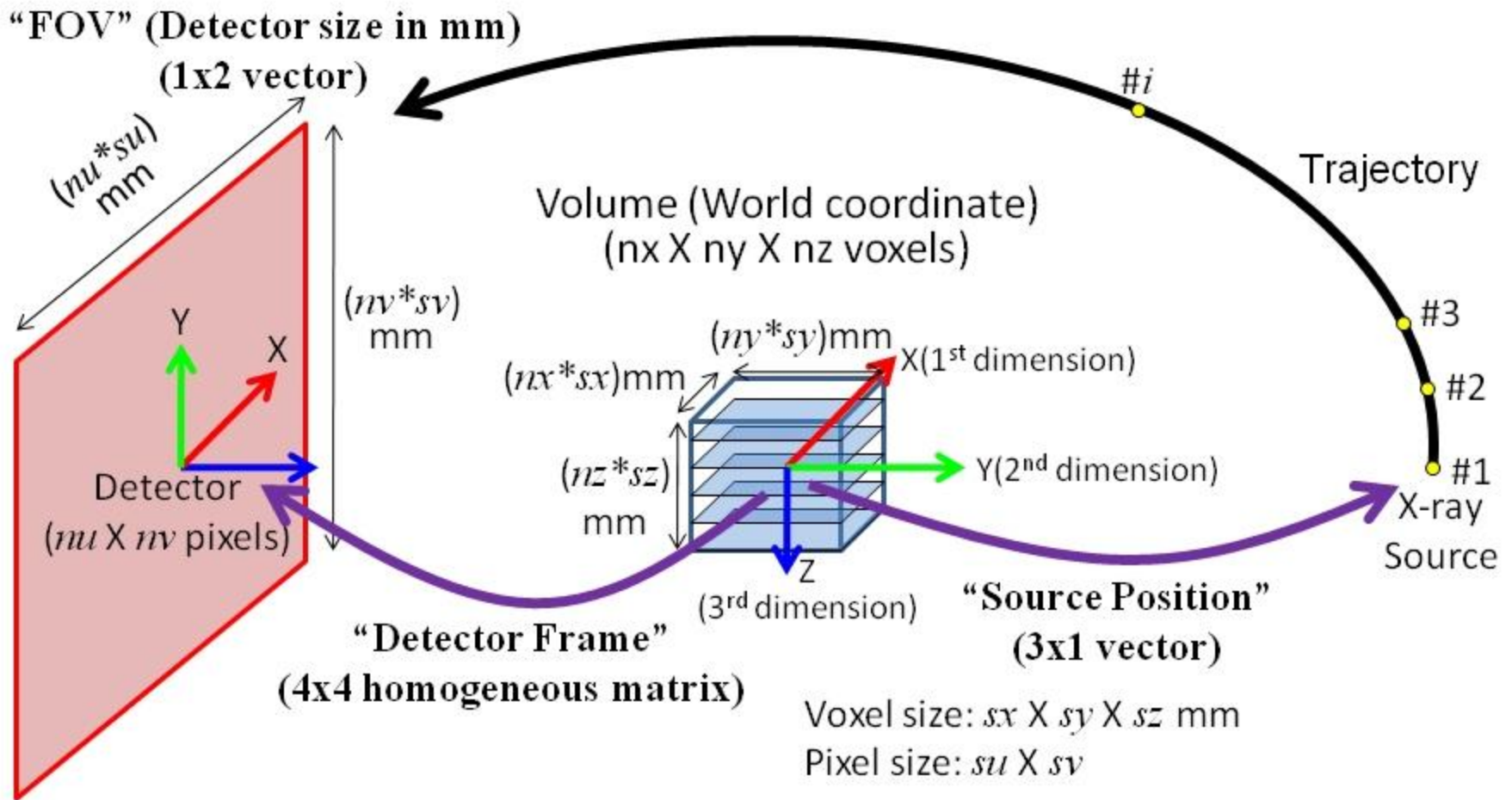
1024×1024×360

12.17 sec (~30fps)

(1.0mm step length, non-Siddon mode)

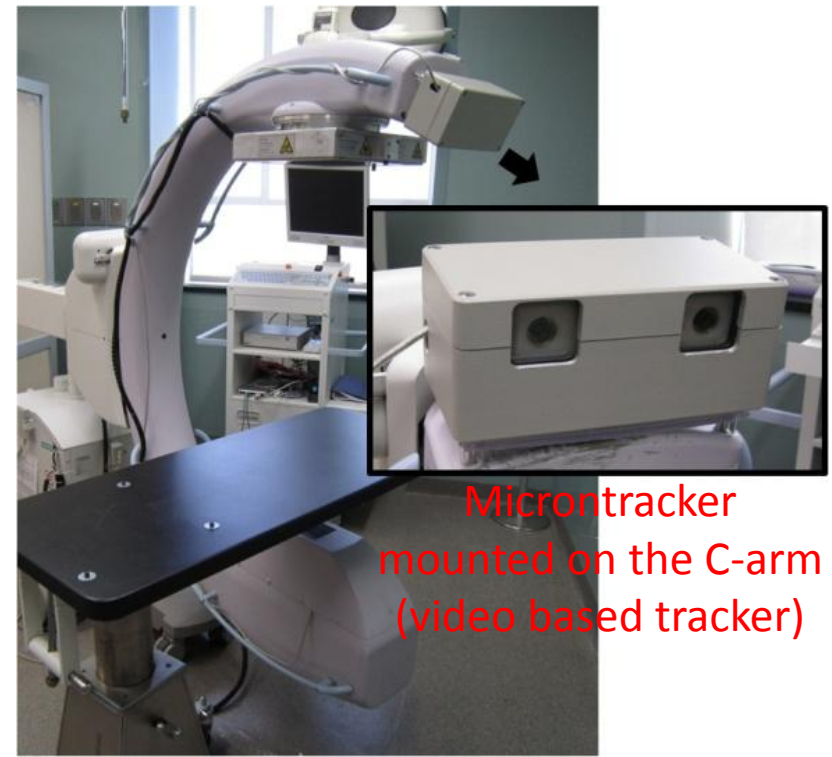
 Demo

# Definition of the coordinate systems



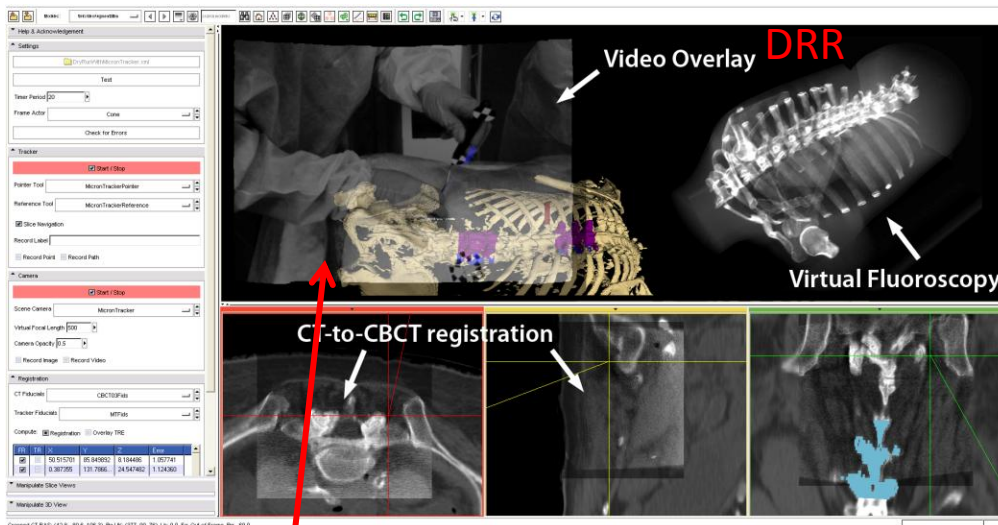
# Example application (1): DRR generation as an image-guidance tool

- Functions used
  - Forward projector
- Integrated into Slicer 3
- Real-time (~30fps)



Microntracker  
mounted on the C-arm  
(video based tracker)

Tracker-on-C

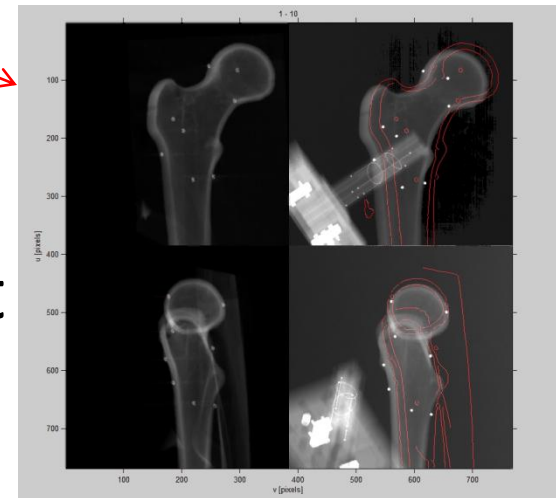


Video image captured by Microntracker

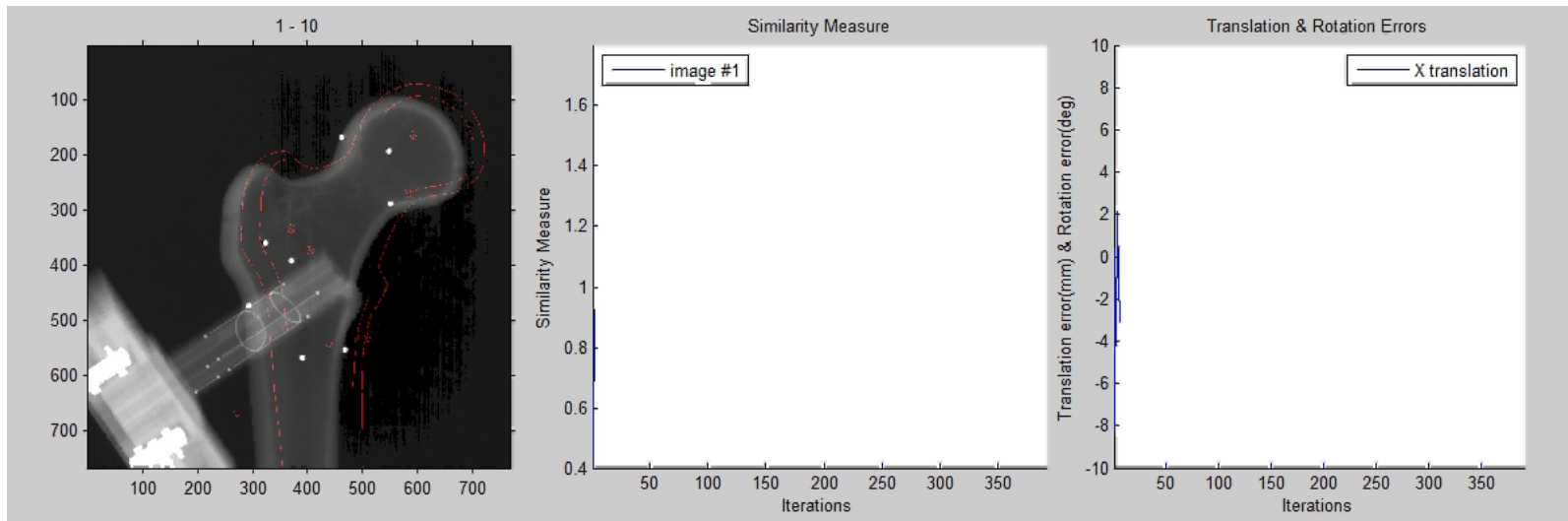
# Example application (2): Intensity-based 2D/3D rigid registration

- Functions used
  - Forward projector, similarity measure computation
- Function other than the toolkit
  - Optimizer (in Matlab): downhill simplex

Floating image



Fixed image with edges of the floating image



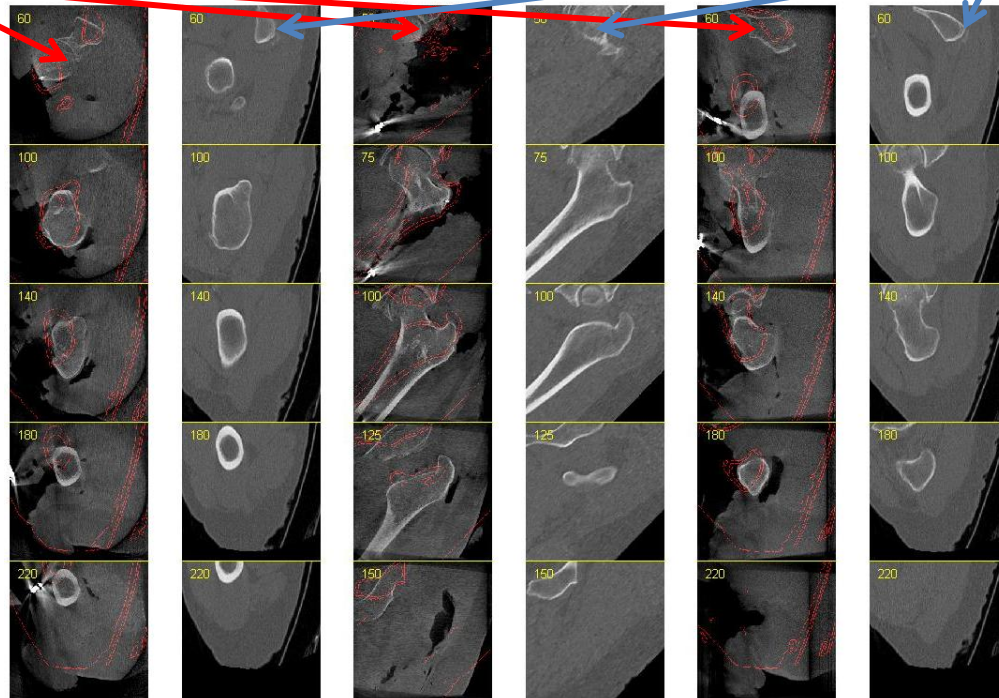


# Example application (3):

## Intensity-based 3D/3D rigid registration

- Functions used
  - Resampler, similarity measure computation (MI)
- Function other than the toolkit
  - Optimizer (in Matlab): downhill simplex

**Fixed volume** #1:(0.00, 10.00, 10.00, 0.00, 10.00, 0.00) cost: -0.066010 **Floating volume**



Axial slices

Coronal slices

Sagittal slices

# Example application (4): FDK reconstruction

- Functions used
  - FDK filtering, voxel-driven back projector
- Integrated into istar3D (cone-beam reconstruction platform developed in I-STAR lab)

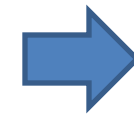
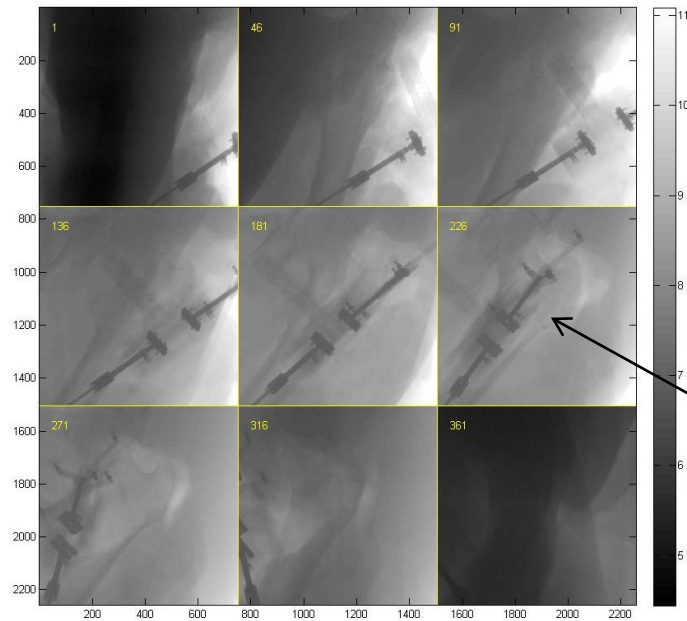
## Performance example

Input: 768x768, 360 projections

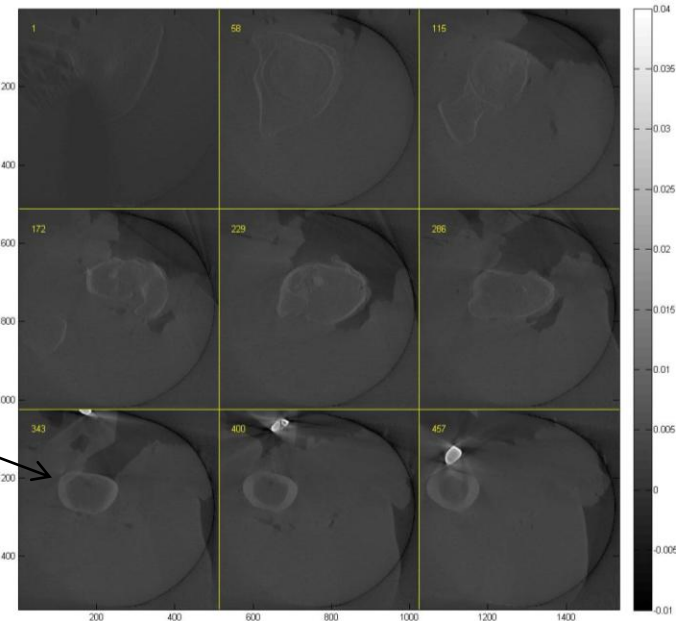
Output: 512x512x512 volume

GPU: nVidia Quadro FX3700

About 62 seconds



femur

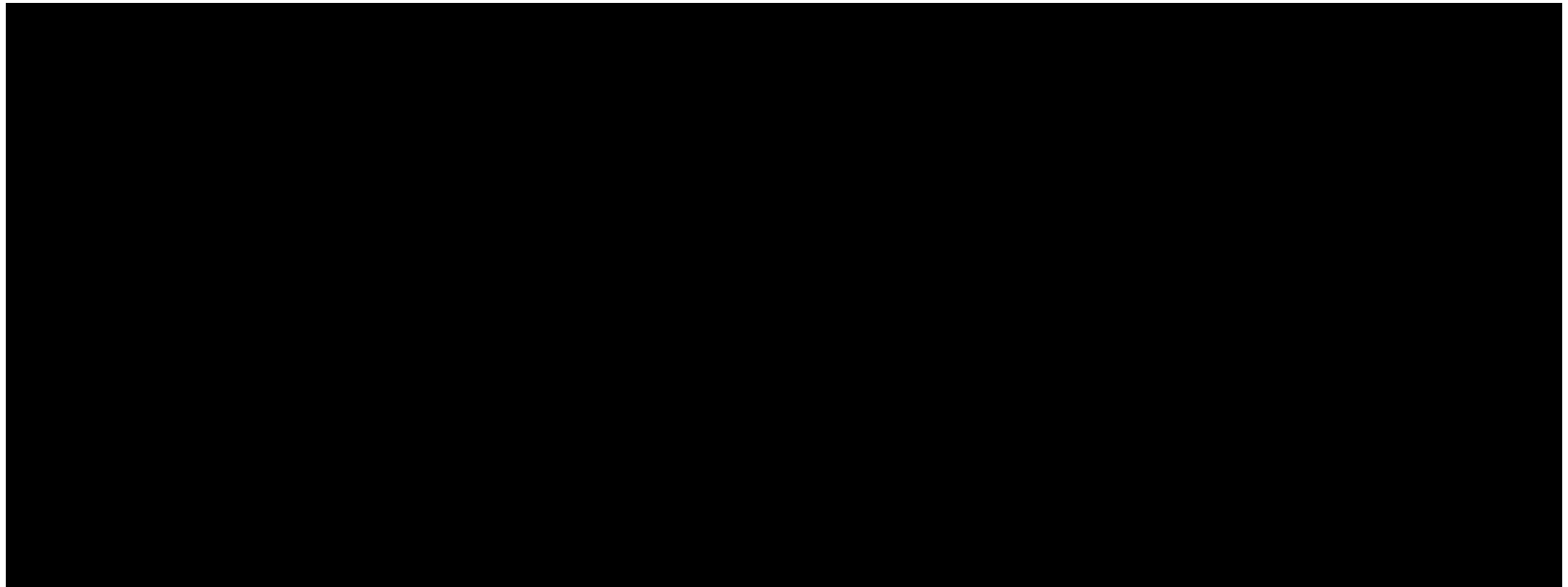


Output volume

Input X-ray projections (Log corrected)

# Example application (5): Statistical reconstruction

- Functions used
  - Siddon-based forward projector, ray-driven back projector
- Integrated into Matlab software (written by Dr. Stayman)



Input projection images (6 images)

Reconstructed volume

An example of sparse sample (6 samples) reconstruction

# Current status

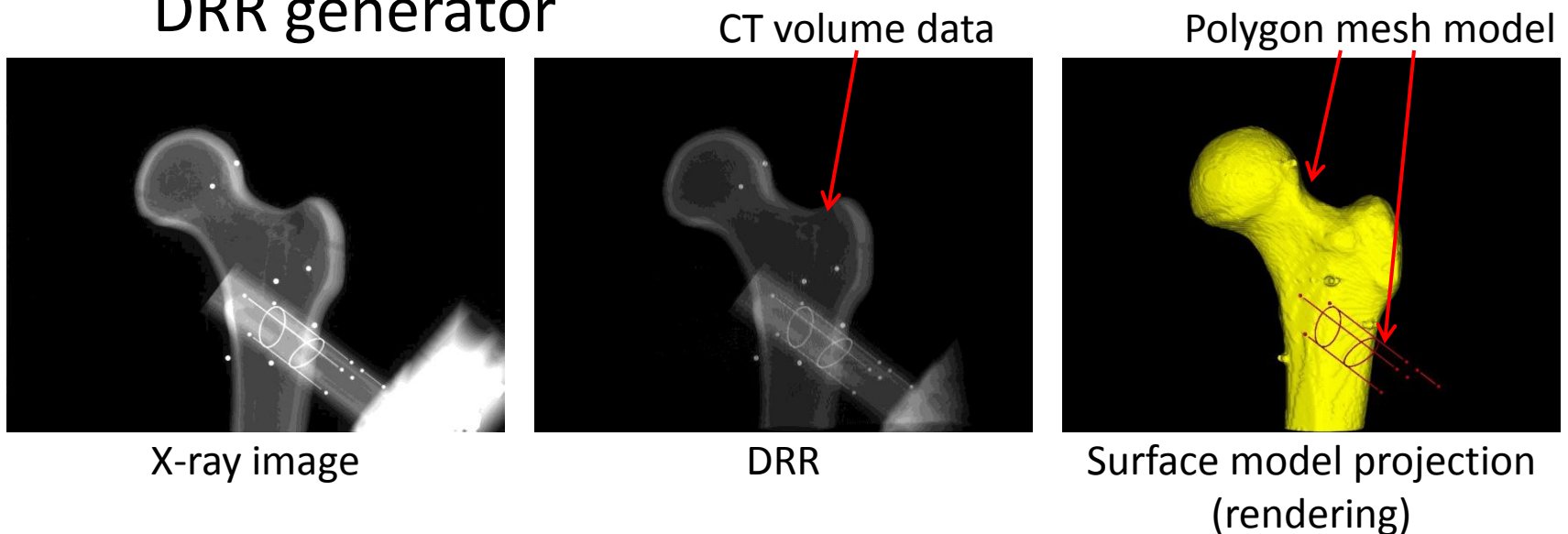
- Implementation of the basic functions has been completed and almost ready for “version 1.0” release.
- Some code are not clean and need to reorganize to make things consistent.
- Need to organize test datasets (ground truth reconstruction) to check the functionalities.

# Future works

- Unit test & debug
- Multi-GPU support
  - partly supported in the current version
- Re-organize (clean up) API
- New functions/applications
  - Polyenergetic projector ('segmented volume' projector)
  - Depth map computation for video/CT registration
  - Statistical atlas using voxel-based statistics with GPU-acceleration (fast instance generation, 2D/3D reg., etc.)
  - Connect the 'real-time' X-ray imaging with robot (da Vinci, ROBODOC)?
  - etc. (any suggestions are very welcomed.)

# Additional features of the toolkit

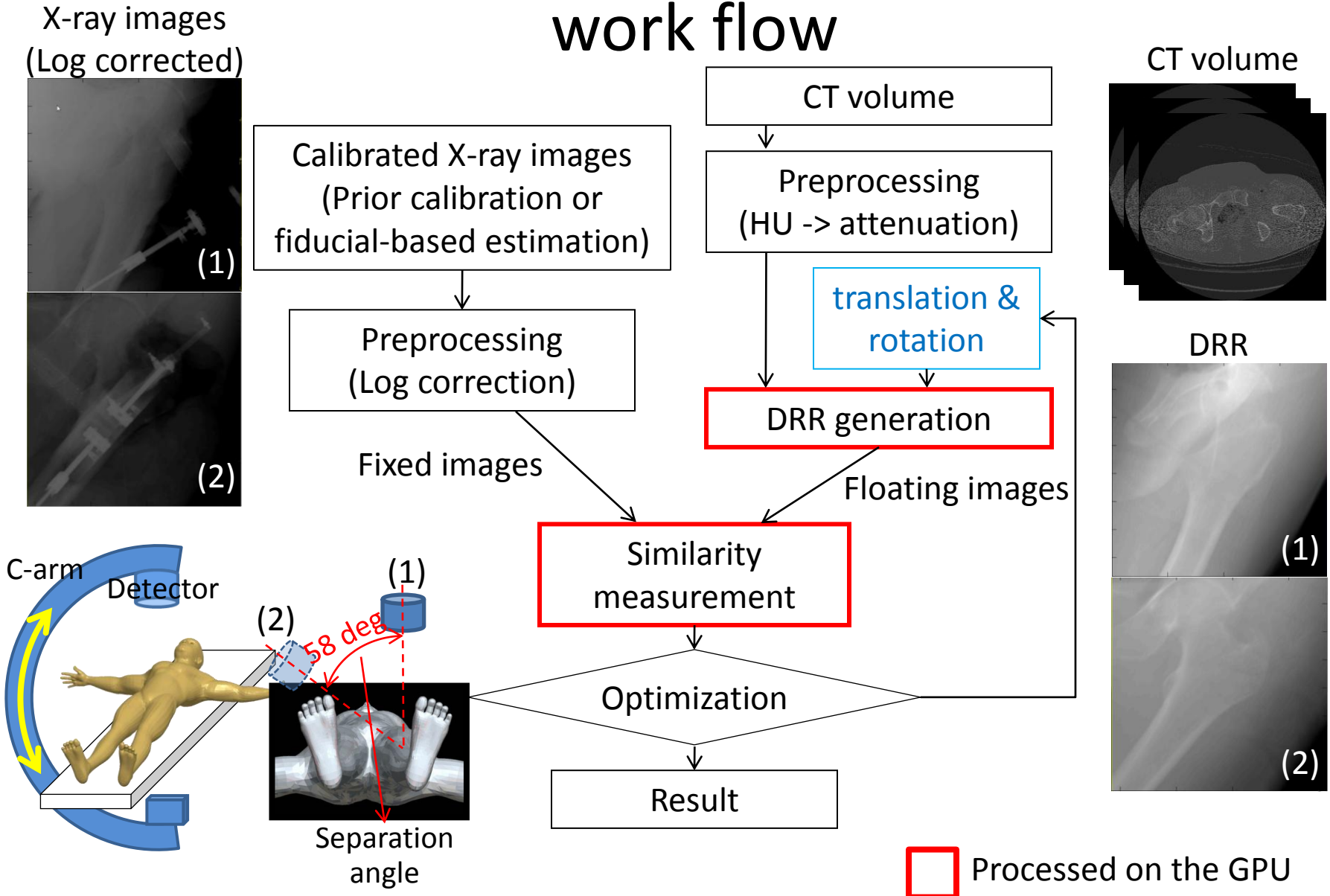
- Surface Projector
  - Generate projection images of surface (polygonal mesh) model using VTK
  - Generate multiple images at the same time
  - Can be used from MATLAB, C/C++, etc. along with DRR generator



# Implementation and experimental validation of an intensity-based rigid 2D/3D registration

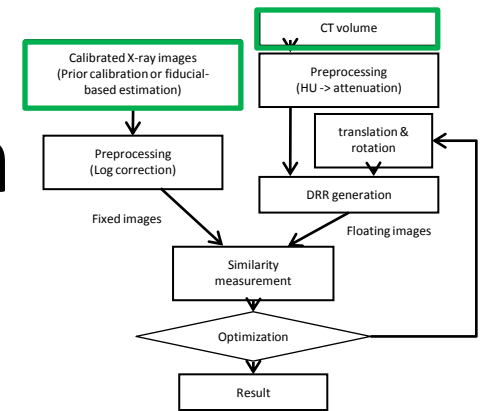
# Intensity-based rigid 2D/3D registration:

## work flow



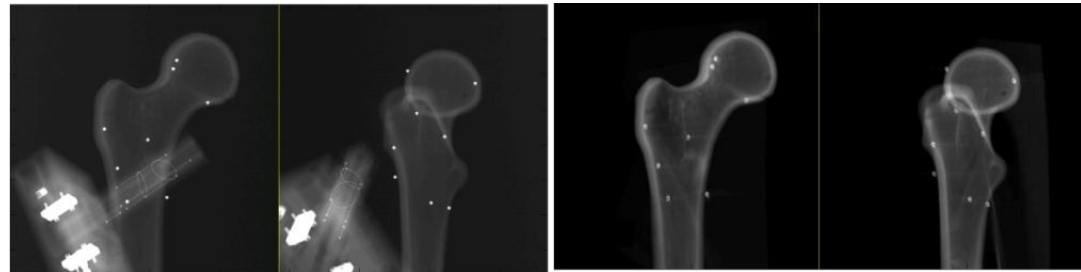


# Three Datasets for evaluation



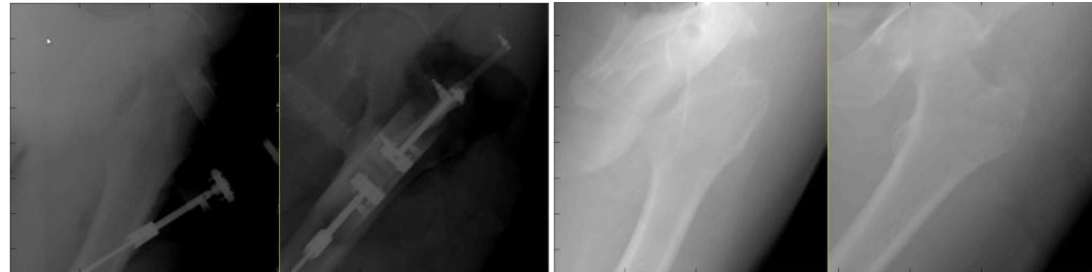
## 1. Sawbone

- Flat-panel
- without soft tissues



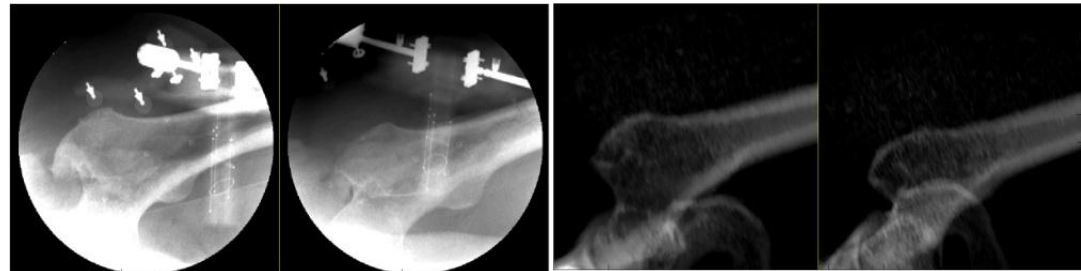
## 2. Cadaver #1

- Flat-panel C-arm
- with soft tissues



## 3. Cadaver #2

- Image intensifier
- with soft tissues

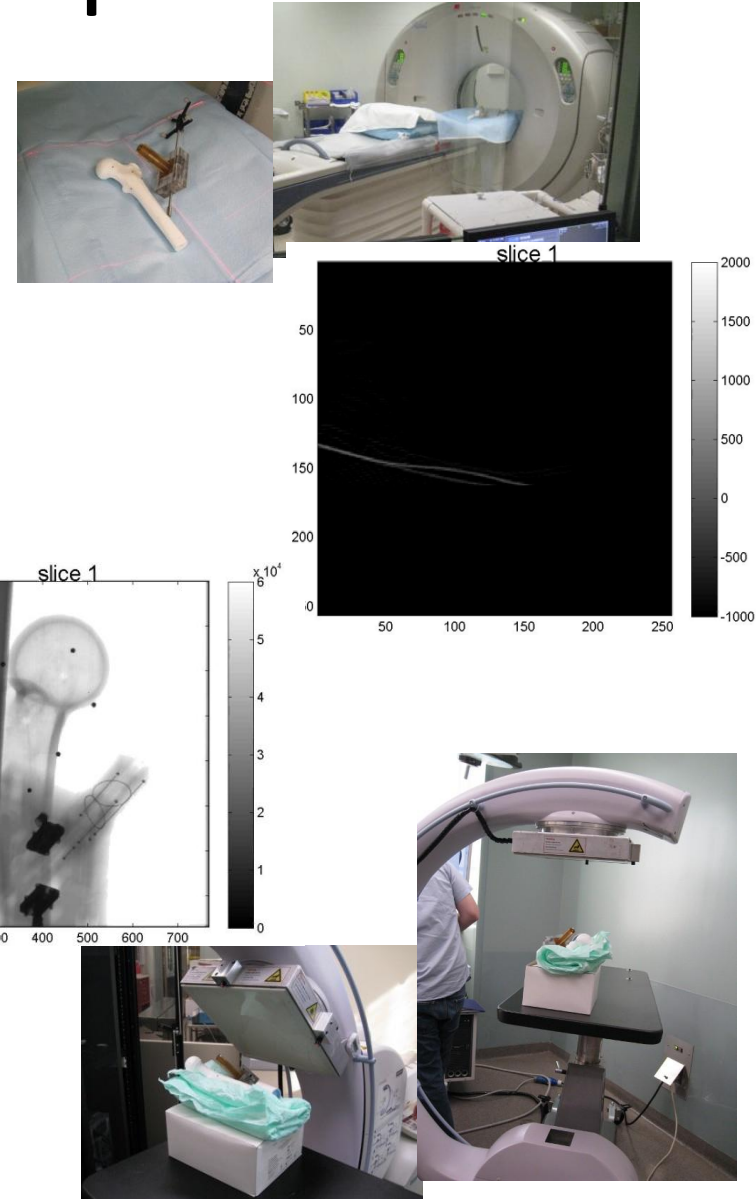


Fixed images (Log corrected)

Floating images

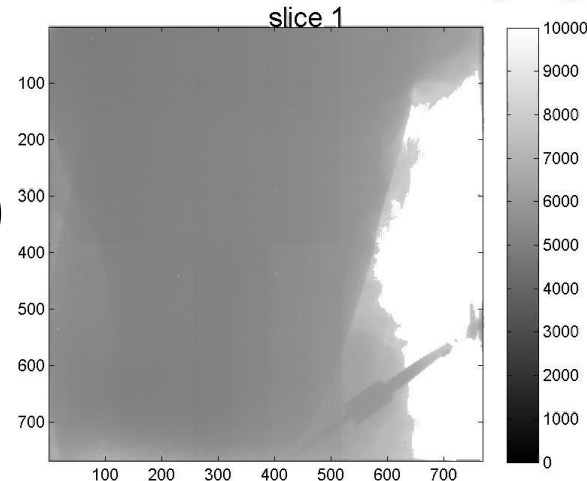
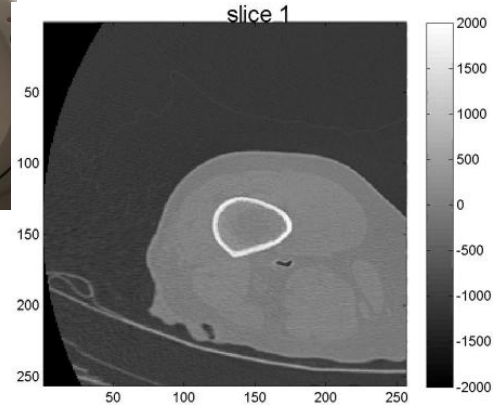
# Dataset 1: Sawbone phantom

- Preop CT
  - Diagnostic CT at Bayview Medical Center (2009/3/3)
  - 256x256x256 voxel (cropped)
  - 0.564x0.564x0.6 mm/voxel
  - 135 kVp, 250 mAs
- Intraop X-ray
  - C14 at MISTIC (2010/3/8)
  - 768x768 pixel
  - 0.388x0.388 mm/pixel
  - 100 kVp, 5.8 mA



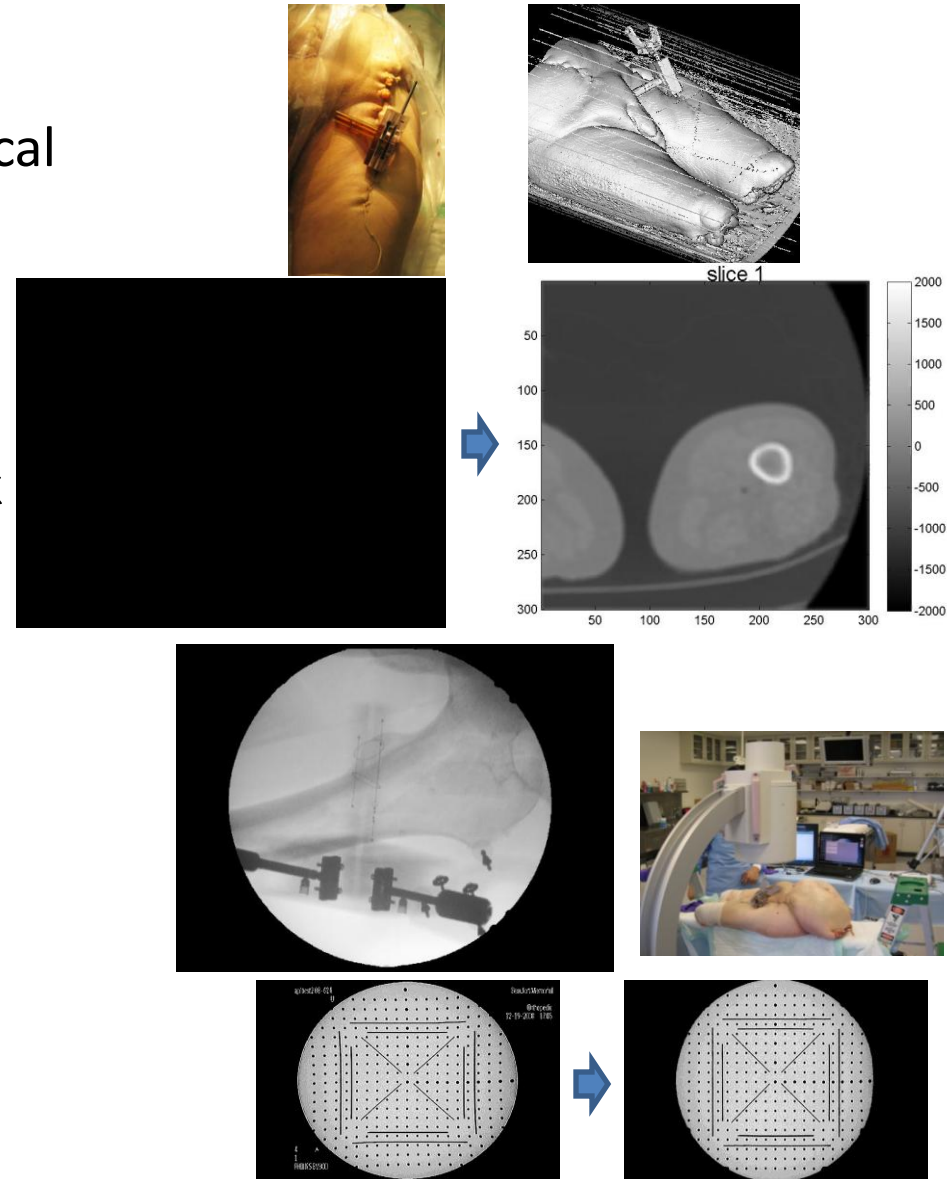
# Dataset 2: Cadaver #1

- Preop CT
  - Diagnostic CT at Bayview Medical Center (2010/4/29)
  - 256x256x256 voxel (cropped)
  - 0.782x0.782x2 mm/voxel
  - 135 kVp, 250 mAs
- Intraop X-ray
  - C14 at MISTIC (2010/4/30)
  - 768x768 pixel
  - 0.388x0.388 mm/pixel
  - 120 kVp, 5.2 mA
  - After cement injection



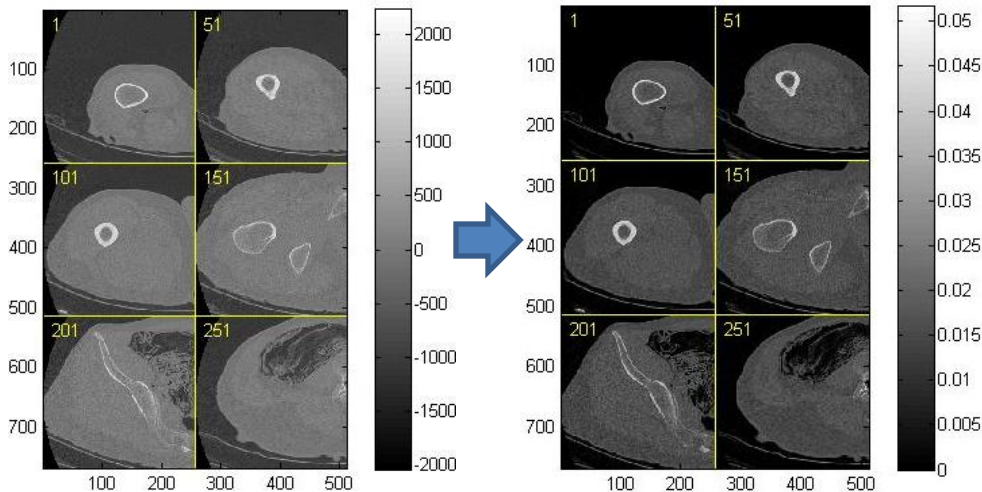
# Dataset 3: Cadaver #2

- Preop CT
  - Diagnostic CT at Bayview Medical Center (2009/8/7)
  - 300x300x700 voxel (cropped)
  - 0.835x0.835x0.602 mm/voxel
  - 135 kVp, 250 mAs
  - Gaussian filter to reduce streak artifact
- Intraop X-ray
  - Philips at Bayview (2009/8/10)
  - 480x480 pixel
  - 0.45x0.45 mm/pixel
  - Before cement injection
  - With distortion correction
  - Only 7 images with narrow separation angle



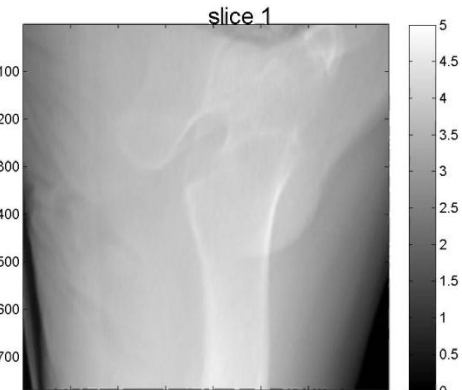
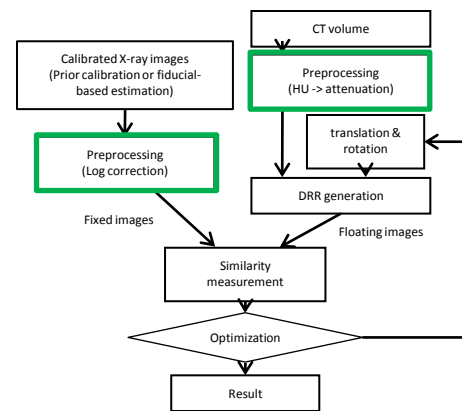
# Preprocessing of input images

Prior CT  
(135kVP,  
250mAs)



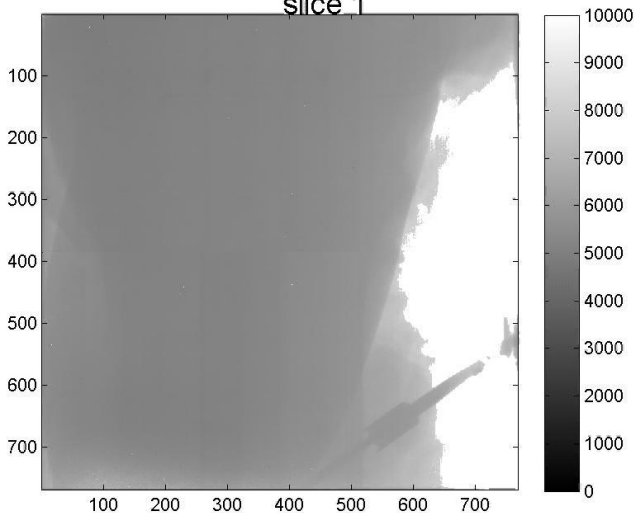
$$HU = 1000 \times \frac{\mu - \mu_{water}}{\mu_{water}}$$

$\mu$

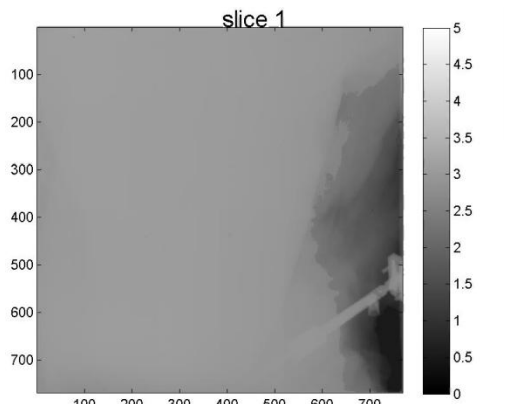


$$DRR = \int_0^d \mu(s; \bar{E}) ds$$

X-ray  
projections  
(120kVp,  
5.2mA)

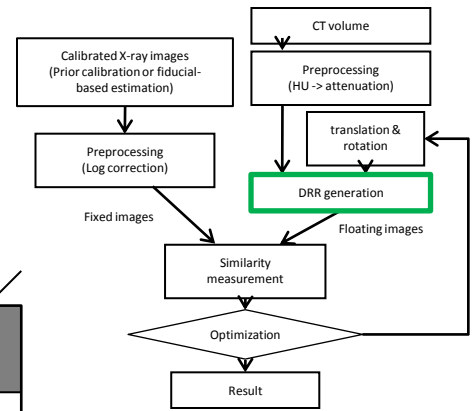
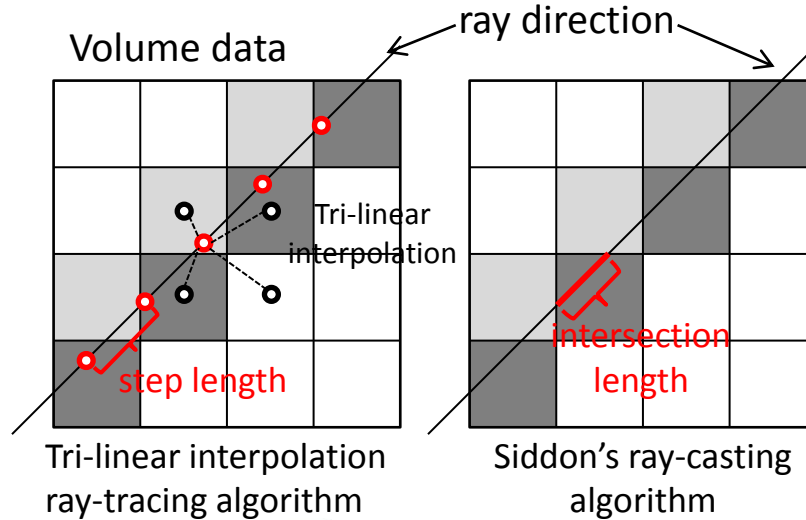
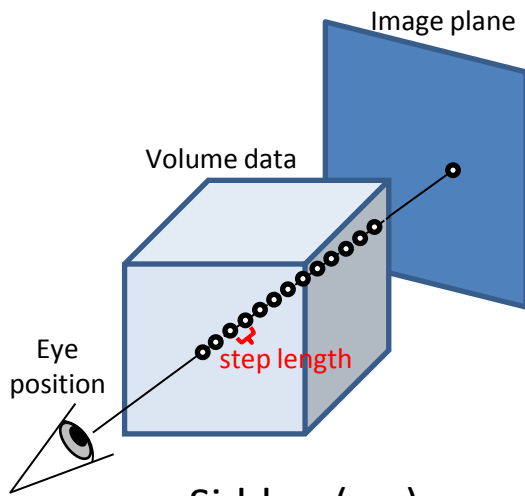


$$I_d = I_0 \exp \left[ - \int_0^d \mu(s; \bar{E}) ds \right]$$



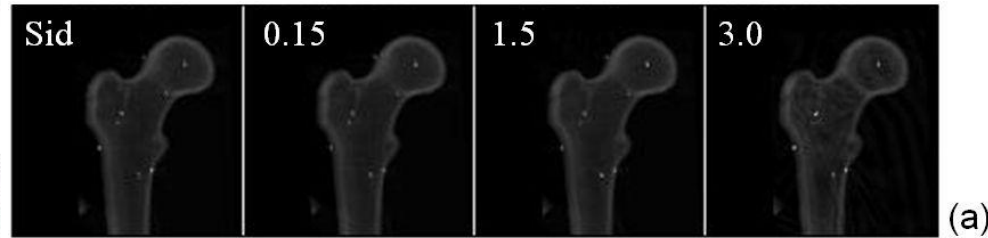
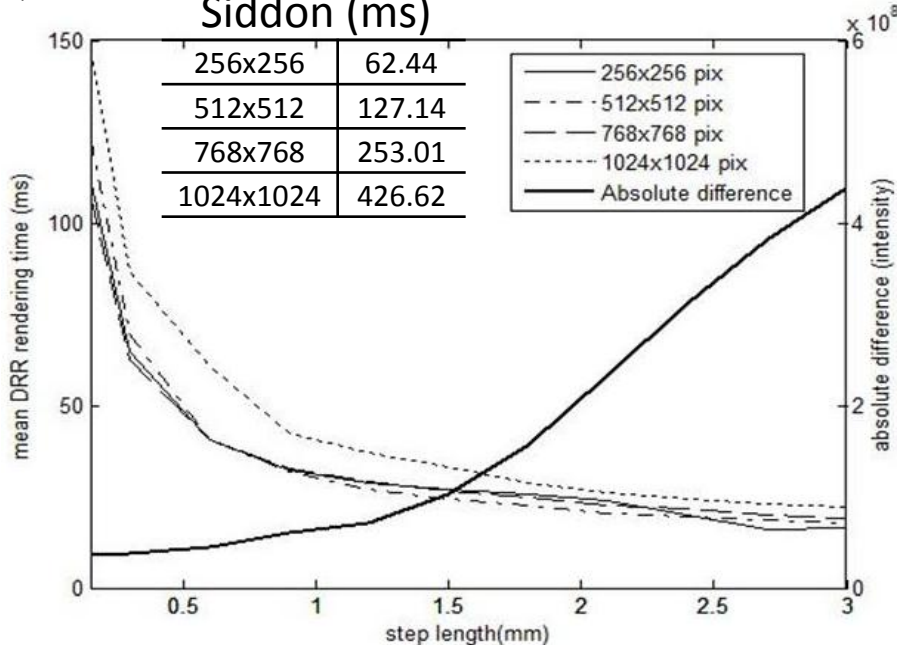
$$g_d = - \ln \left( \frac{I_d}{I_0} \right) = \int_0^d \mu(s; \bar{E}) ds$$

# DRR generation



Siddon RL, "Fast calculation of the exact radiological path for a three-dimensional CT array," Med.Phys. Mar-Apr 12(2), 252-255 (1985)

Siddon (ms)



512x512x512 volume (0.3mm<sup>3</sup>/voxel)

# Gradient Information (GI) Similarity Measure

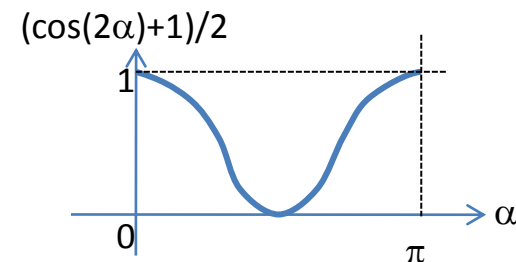
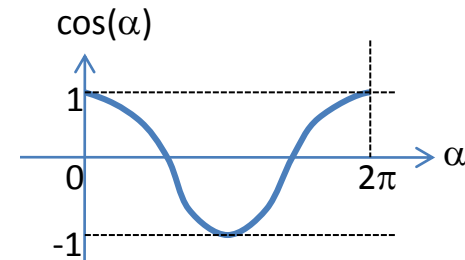
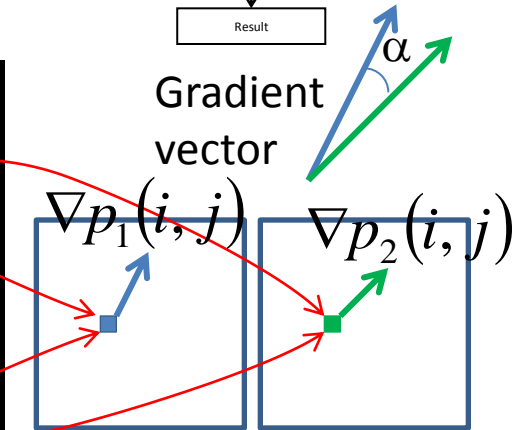
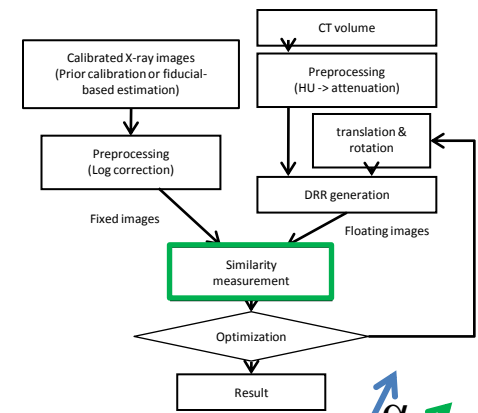
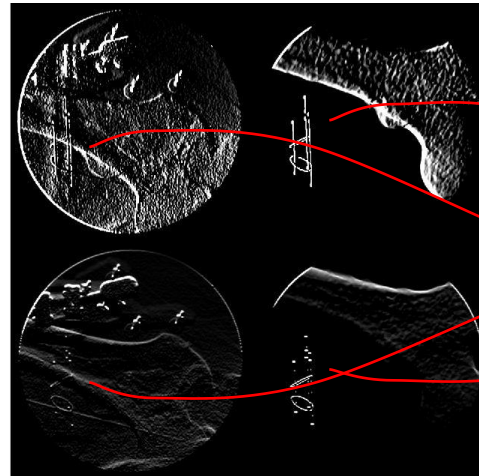
$$\alpha_{i,j} = \arccos \frac{\nabla p_1(i,j) \cdot \nabla p_2(i,j)}{\|\nabla p_1(i,j)\| \|\nabla p_2(i,j)\|}$$

(angle between two gradient vectors)

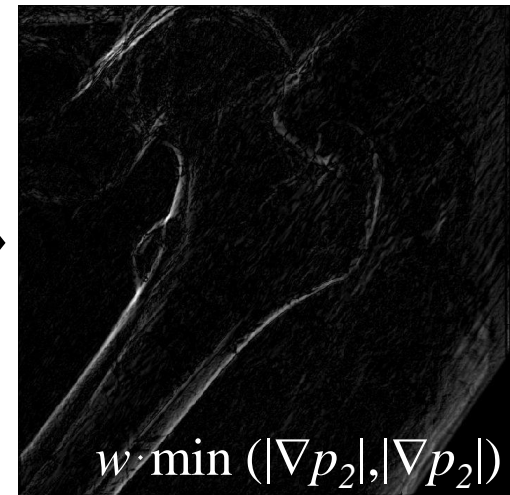
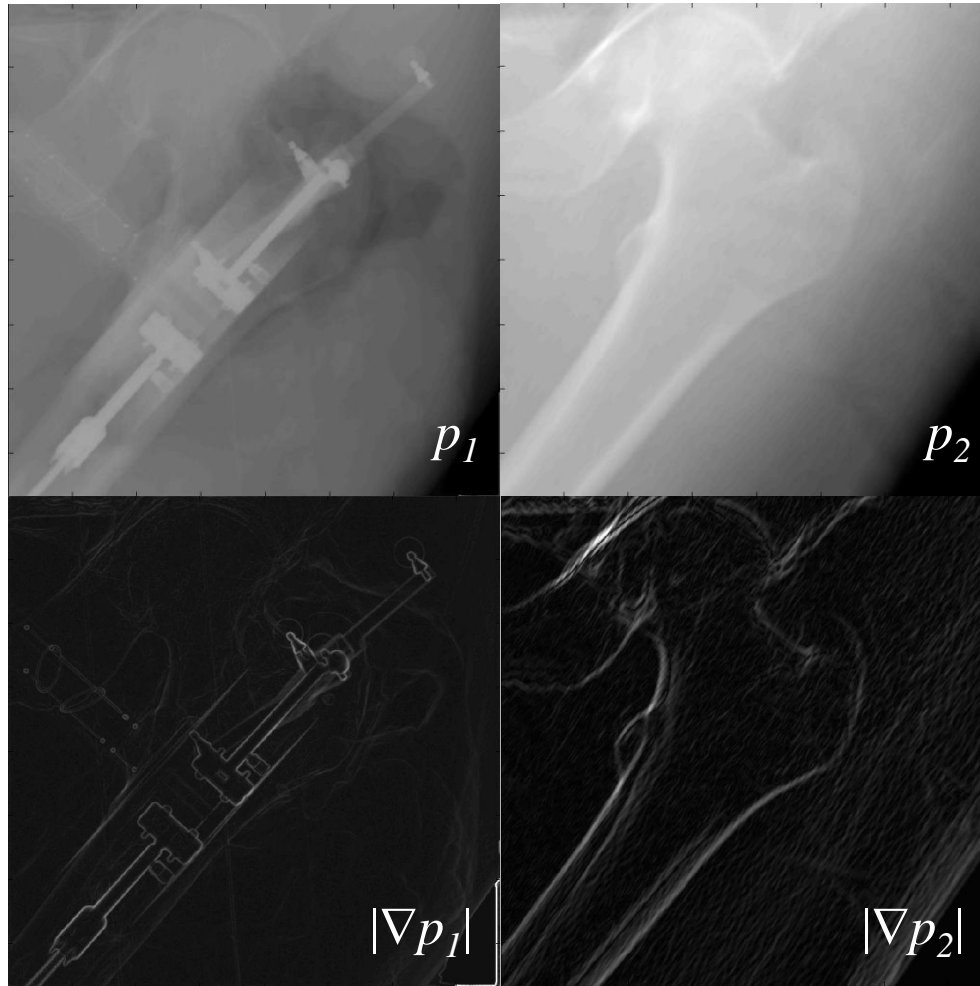
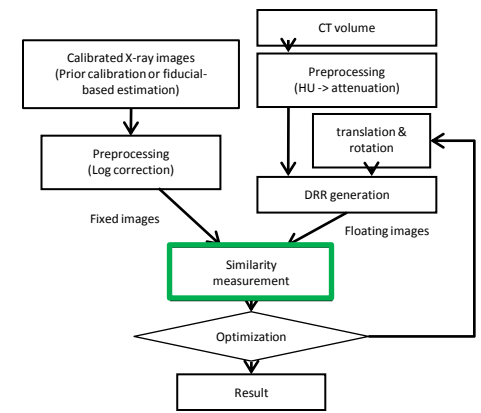
$$w(i,j) = \frac{\cos(2\alpha_{i,j}) + 1}{2}$$

$$G(p_1, p_2) = \sum_{i,j} w(i,j) \min(\|\nabla p_1(i,j)\|, \|\nabla p_2(i,j)\|)$$

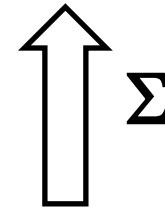
Pluim, J.P., Maintz, J.B. and Viergever, M.A., 2000. Image registration by maximization of combined mutual information and gradient information. IEEE Transactions on Medical Imaging, 19(8), 809-814.



# Gradient Information (GI) Similarity Measure



$$GI(p_1, p_2)$$





# Optimizer

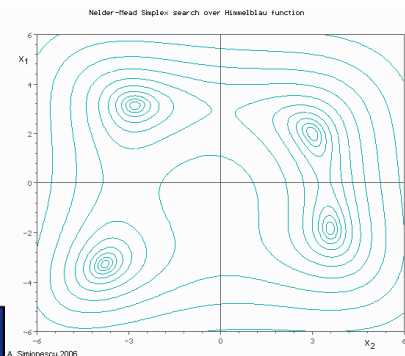
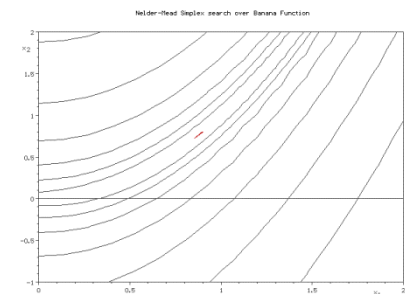
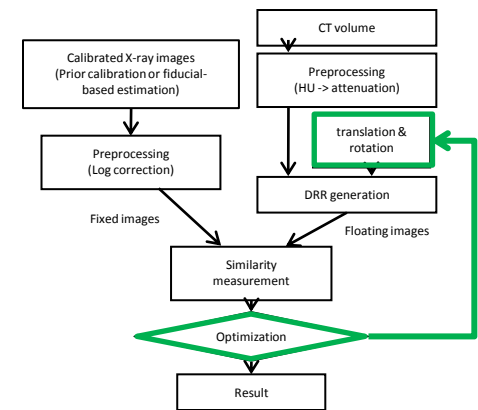
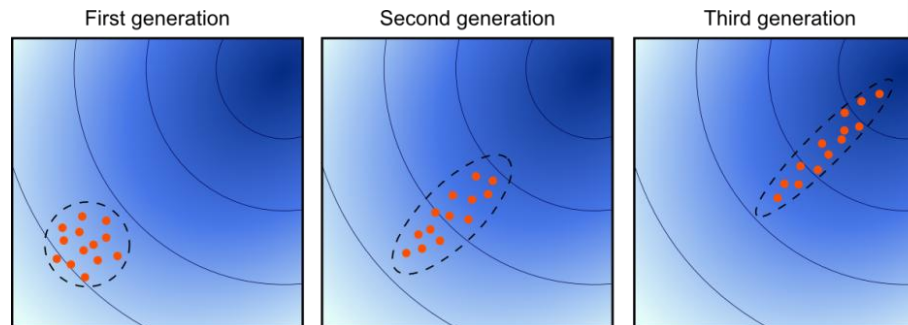
## 1. Nelder-Mead Downhill Simplex

- Heuristic optimization algorithm
- No derivative computation
- Matlab implementation - `fminsearch()`

## 2. CMA-ES (Covariance Matrix Adaptation Evolution Strategy)

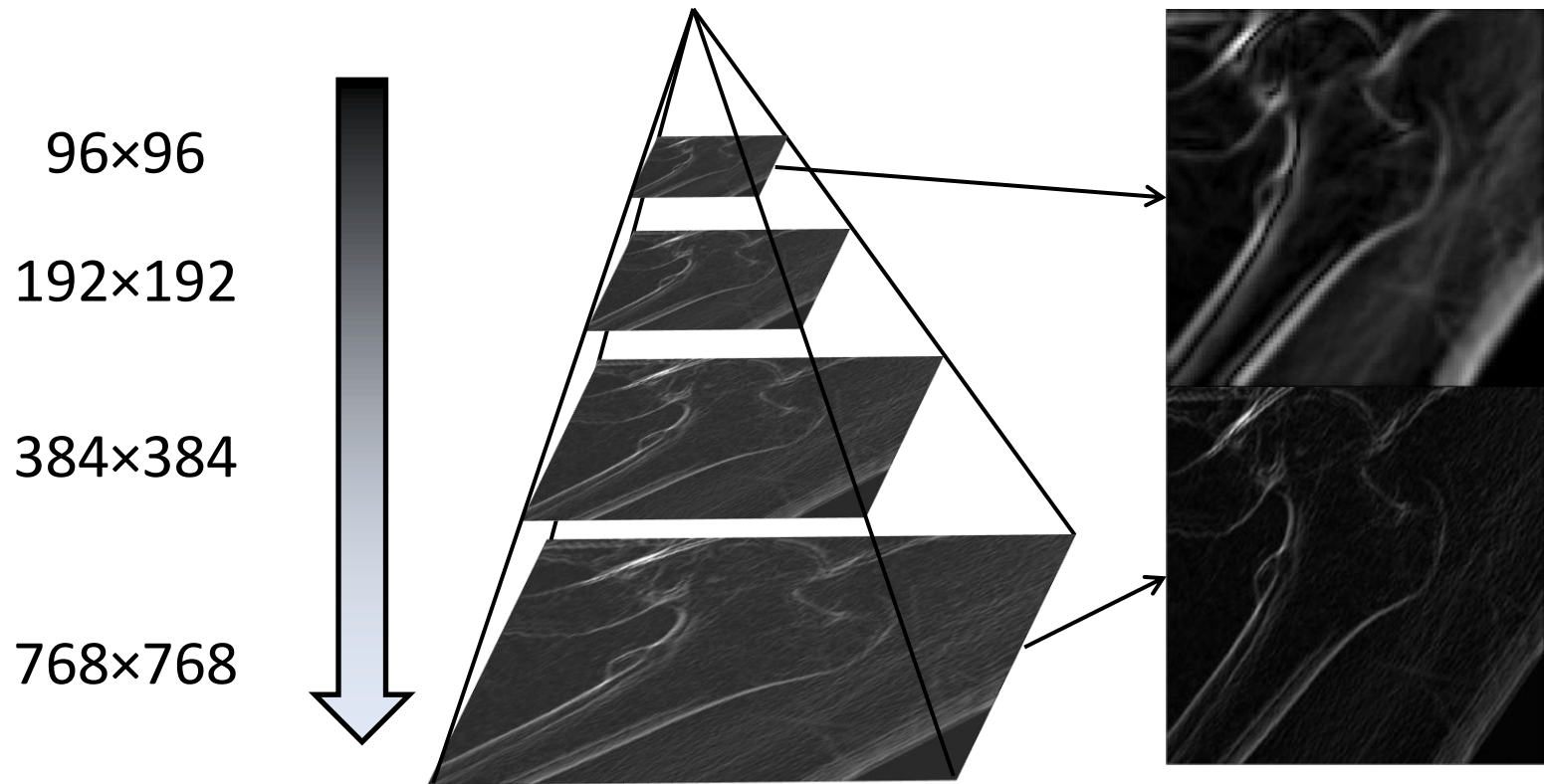
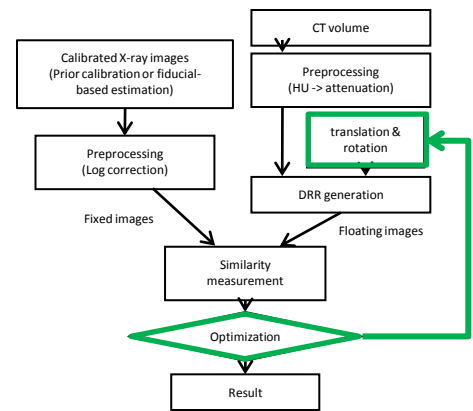
- No derivative computation
- Known for robustness and efficiency in a rugged search landscape
- Matlab implementation by Hansen<sup>\*1</sup>

\*1: Hansen N. The CMA evolution strategy: a comparing review. In: Lozano JA, Larranaga P, Inza I, Bengoetxea E, editors. Towards a new evolutionary computation. Advances on estimation of distribution algorithms: Springer; 2006. p. 75-102.



from Wikipedia

# Coarse-to-fine multi-resolution optimization strategy

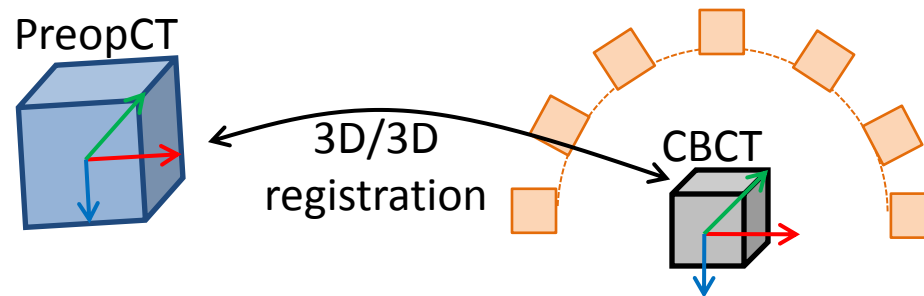


- Optimization was repeated 4 times using different resolution

# Ground truth registration

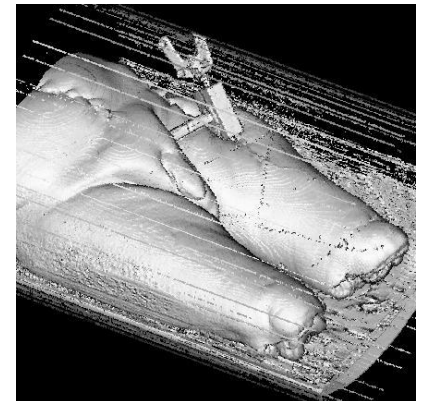
## 1. Flat-panel C-arm (Siemens C14)

- Geometric calibration using helix BB phantom
- 3D/3D registration between Preop CT and CBCT



## 2. Conventional C-arm

- Pose estimation using FTRAC
- Diagnostic CT of the cadaver with the FTRAC



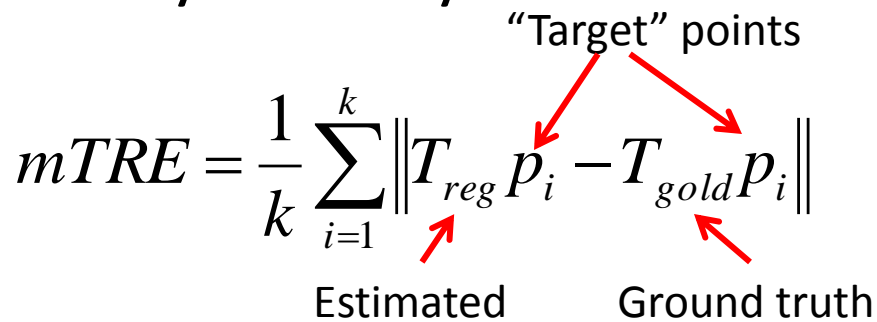
# Evaluation method: Error measure

- mTRE (mean TRE)
  - An error measure proposed in [1] to determine 3D error of a registration.
  - While it is widely used in literature, definition of the “target” points differ from study to study

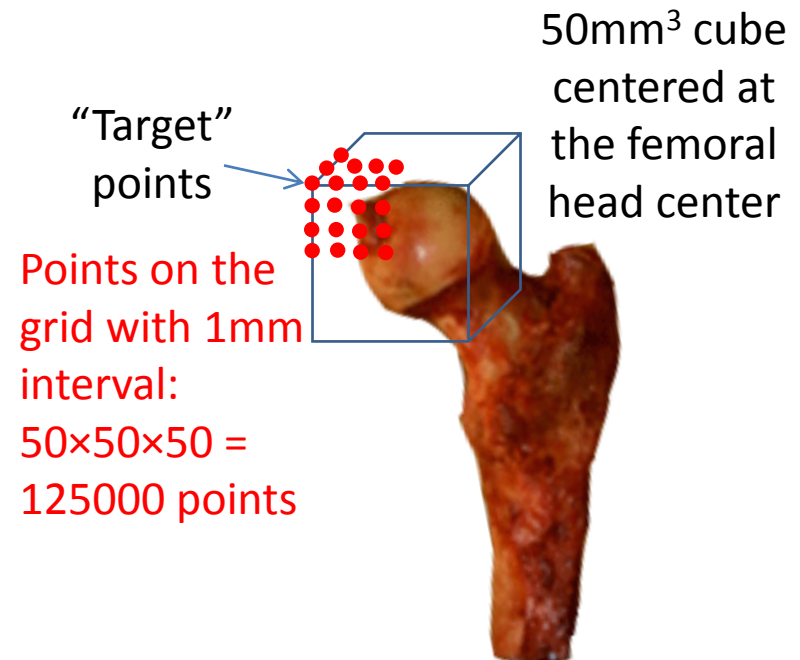
$$mTRE = \frac{1}{k} \sum_{i=1}^k \left\| T_{reg} p_i - T_{gold} p_i \right\|$$

Estimated                      Ground truth

“Target” points



[1] van de Kraats EB, Penney GP, Tomazevic D, van Walsum T, Niessen WJ. ,  
"Standardized evaluation methodology for 2-D-3-D registration," IEEE Trans.Med.Imaging Sep 24(9), 1177-1189 (2005).



# Evaluation method: Initial guesses

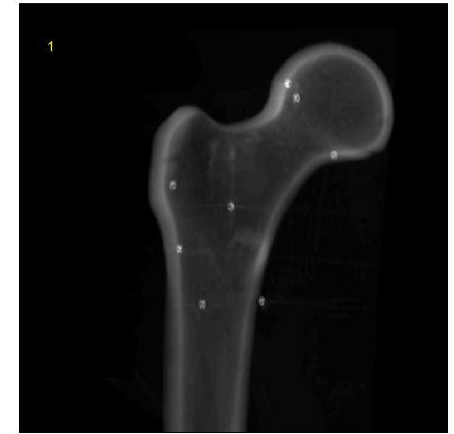
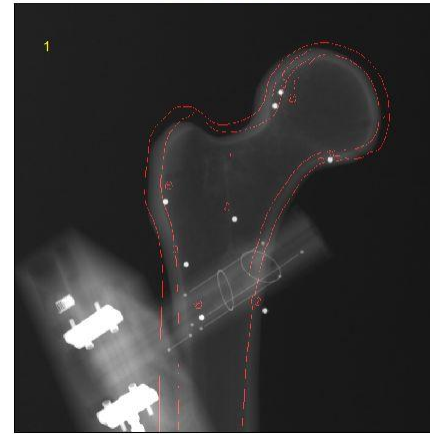
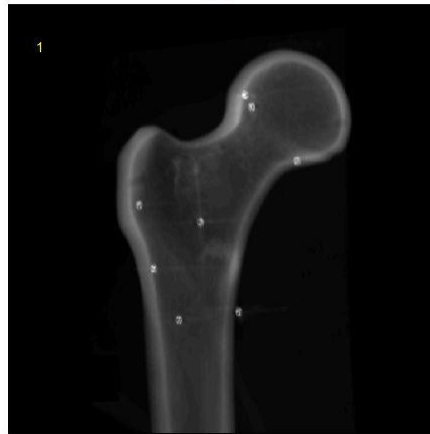
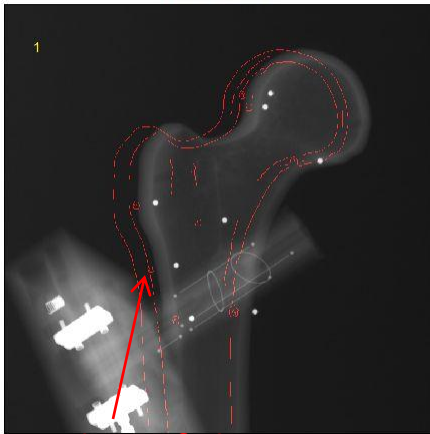
- 50 registration trials from different initial pose were conducted
- Initial poses were randomly selected by perturbing the ground truth registration by  $[-10 +10]$  mm,  $[-10 +10]$  degrees.
- The same initial poses were used for all experiments

Fixed image

Floating image

#1(768x768):(-0.59, 6.57, 1.21, -7.34, 0.47, -5.09) cost: -0.003633, elapsed: 0.236 sec  
Fixed + edge of DRR  
DRR

#1(768x768):(0.77, 7.53, -4.02, 3.37, 1.95, -0.30) cost: -0.005474, elapsed: 0.240 sec  
Fixed + edge of DRR  
DRR



Edge of the  
floating image

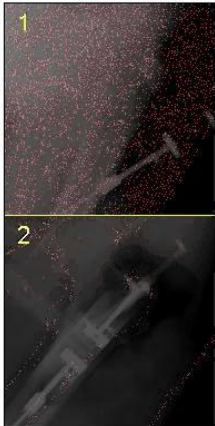
Randomly generated initial guess (2 examples out of 50)

# Results

# One typical trial

#4(768x768):(2.07, -2.72, 0.48, 4.51, 6.16, -6.46) cost: -0.017321, elapsed: 2.505 sec

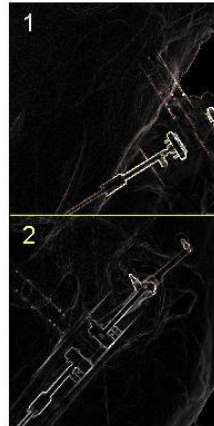
Fixed + edge of DRR



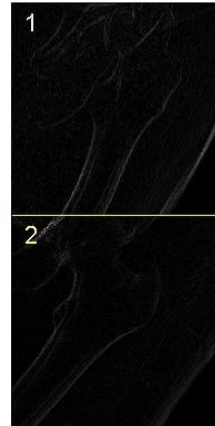
DRR



Gradient of fixed



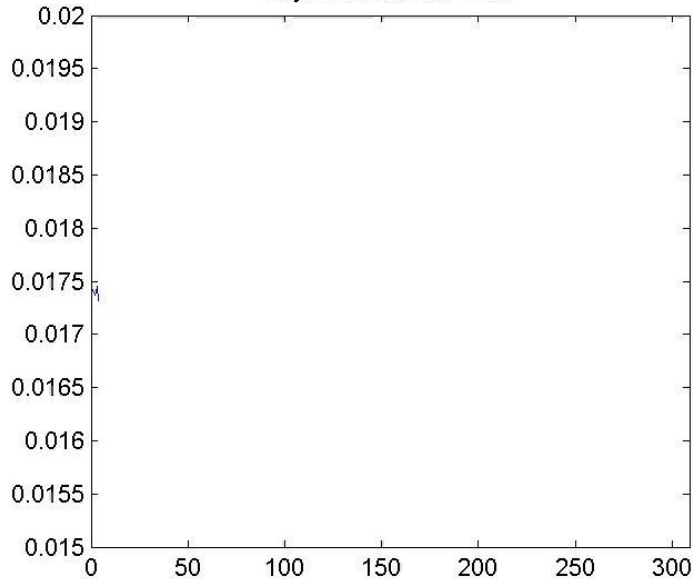
Gradient of DRR



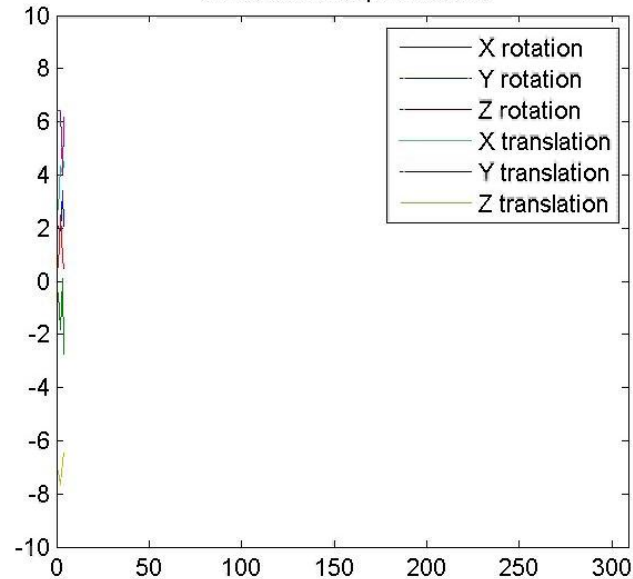
w



Objective function value

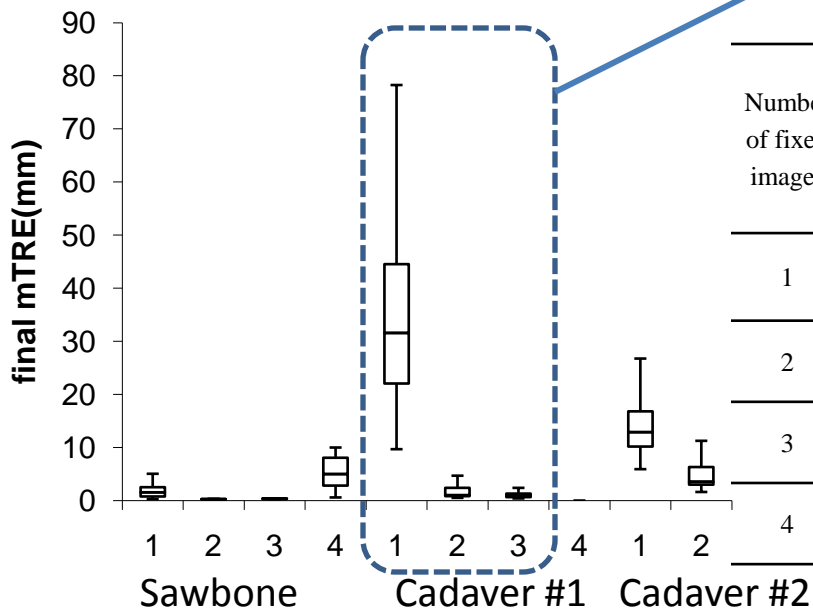
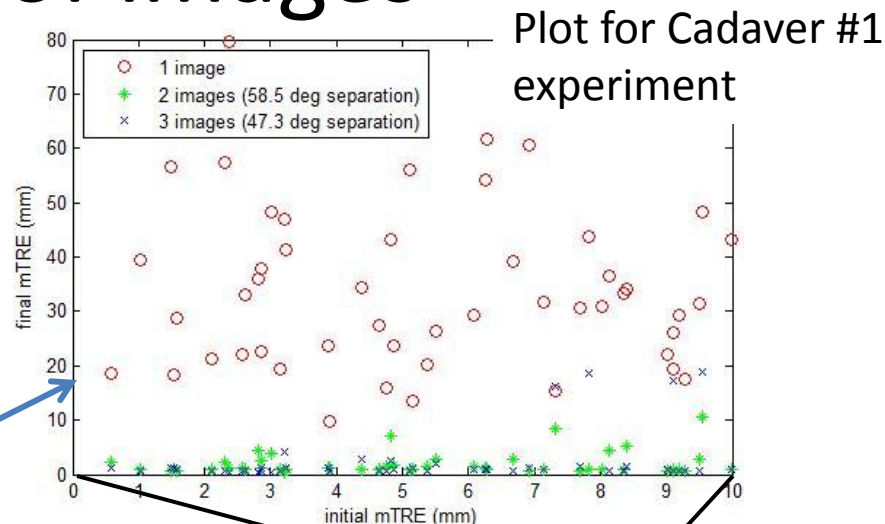
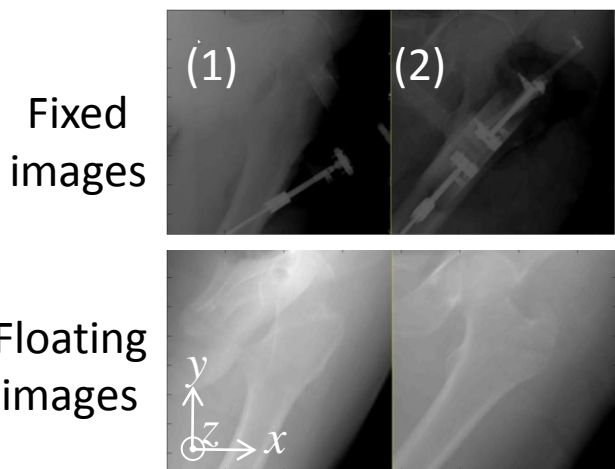


Transformation parameters



- GI similarity measure
- CMA-ES optimizer
- Siddon-based DRR

# Result of 50 trials: comparison of number of images

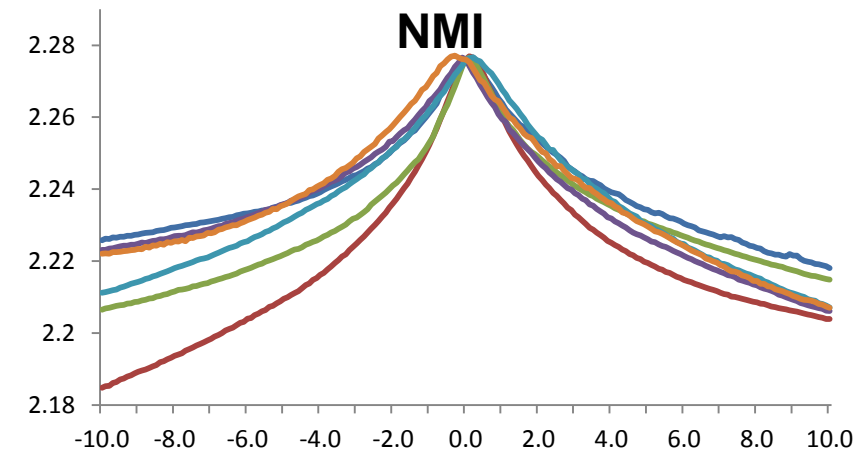
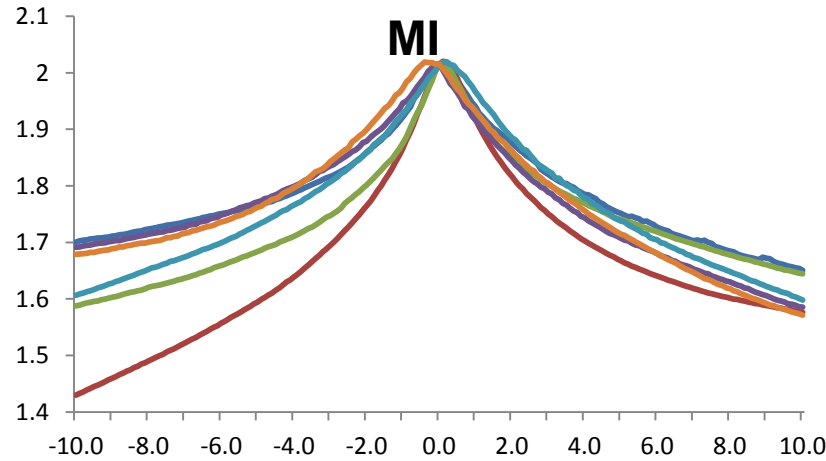
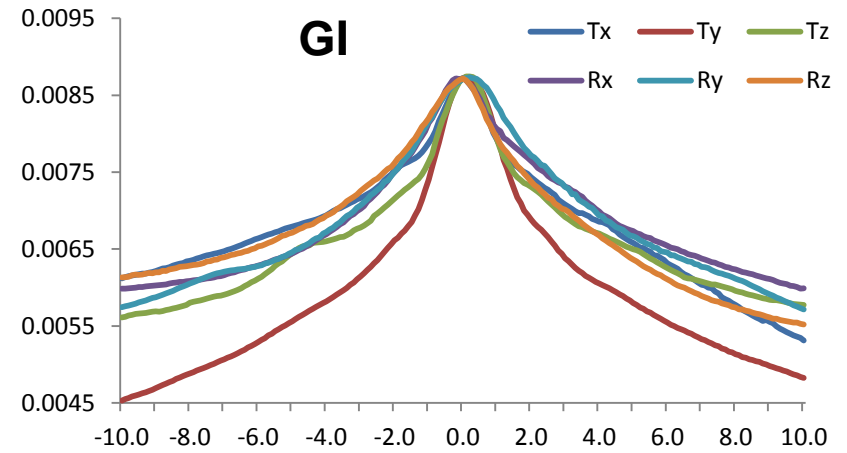
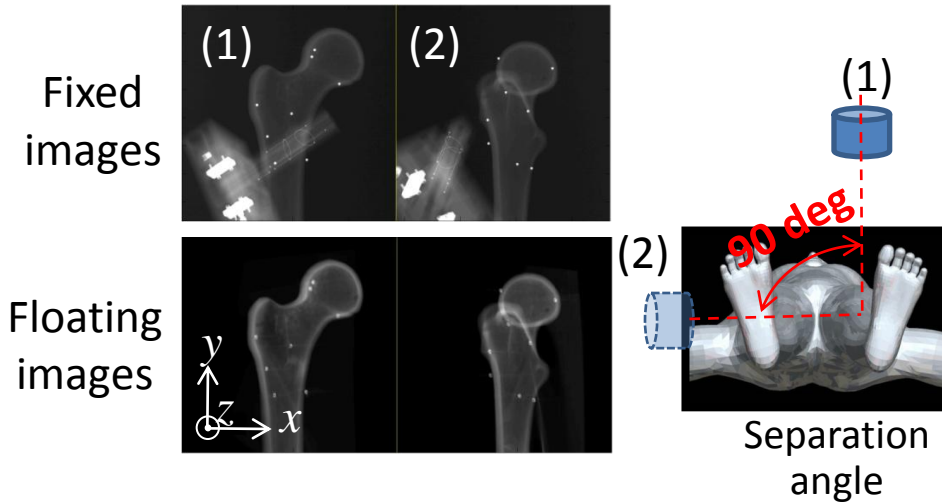


Number of fixed images	Sawbone				Cadaver #1				Cadaver #2			
	mTRE (mm) for success	T (s)	R (%)	$\Delta$ (deg)	mTRE (mm) for success	T (s)	R (%)	$\Delta$ (deg)	mTRE (mm) for success	T (s)	R (%)	$\Delta$ (deg)
1	1.560 $\pm$ 1.013	142.8 $\pm$ 3.5	94	n/a	* 159.3 $\pm$ 3.8	0	n/a	* 104.3 $\pm$ 8.0	0	n/a		
2	0.229 $\pm$ 0.042	280.1 $\pm$ 5.6	100	90	1.404 $\pm$ 0.967	323.5 $\pm$ 5.7	92	58.5	3.241 $\pm$ 0.756	184.5 $\pm$ 6.1	68	31.5
3	0.325 $\pm$ 0.027	410.6 $\pm$ 16.1	100	60	1.021 $\pm$ 0.682	450.5 $\pm$ 5.4	90	47.3	n/a	n/a	n/a	n/a
4	0.314 $\pm$ 0.025	684.9 $\pm$ 40.2	100	45	---	---	---	31.5	n/a	n/a	n/a	n/a

T - registration time, R - success rate, D - angle between consecutive images used in the experiment

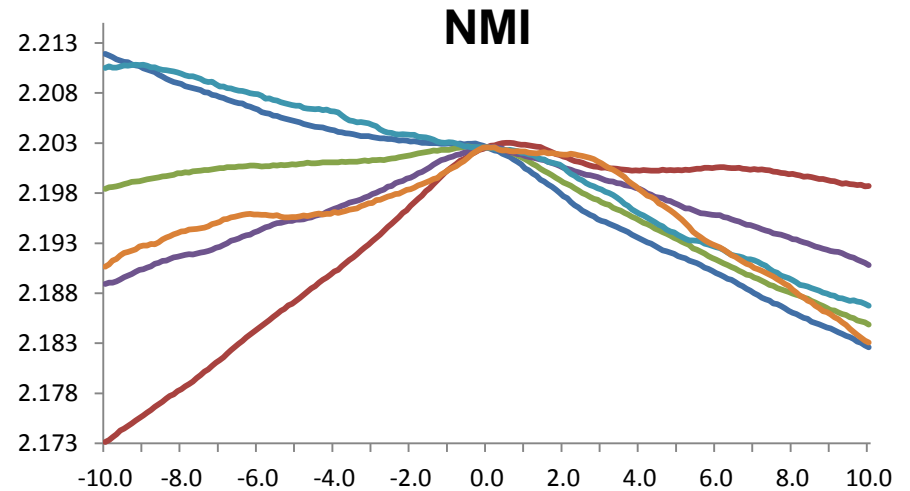
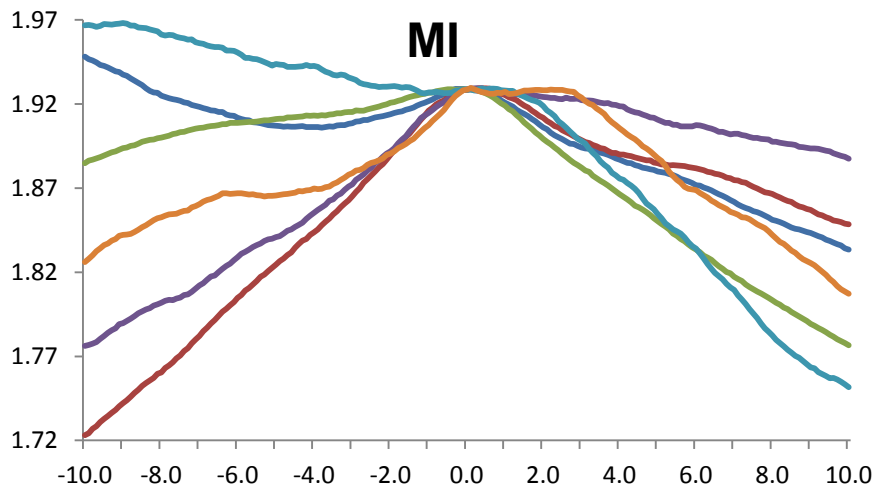
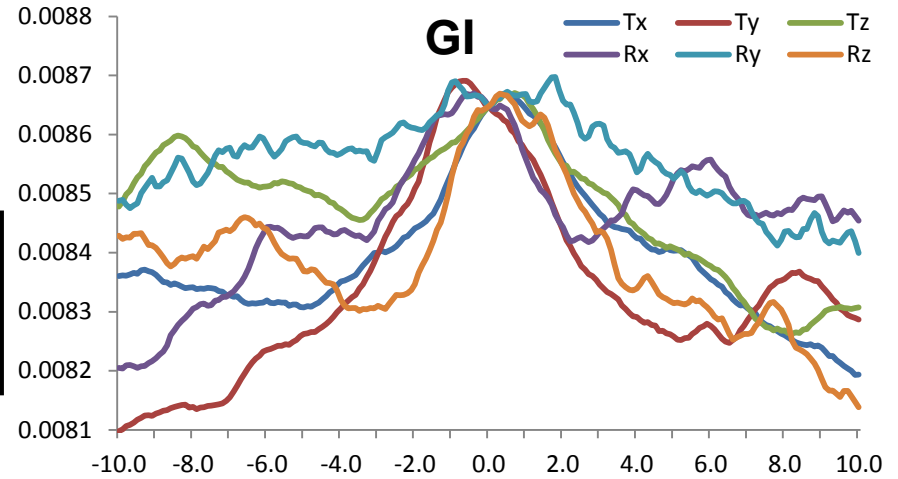
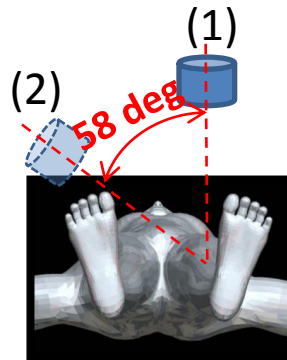
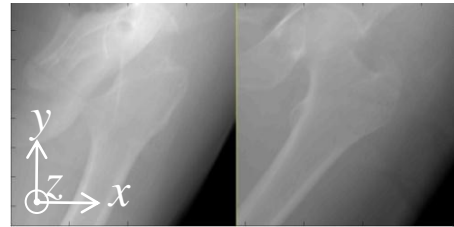
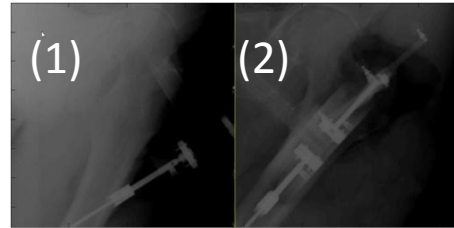


# Similarity Measures: Sawbone Images



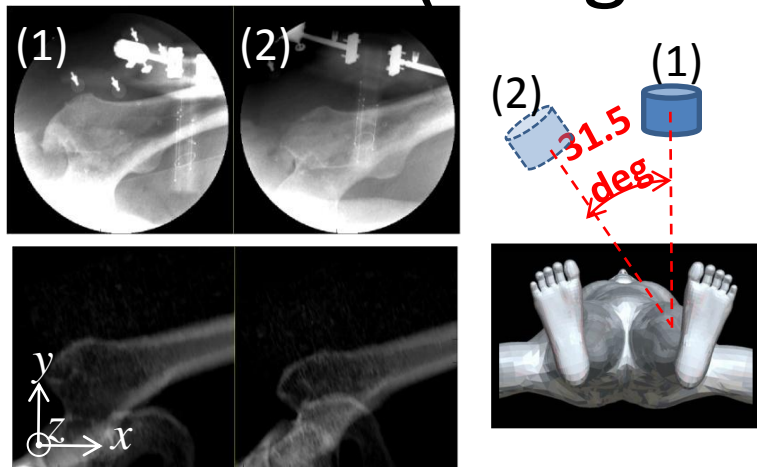
\*Sum of the similarity measures of the 2 image pairs

# Similarity Measures: Cadaver #1 (flat-panel)



Challenges: Soft tissue and metallic instruments

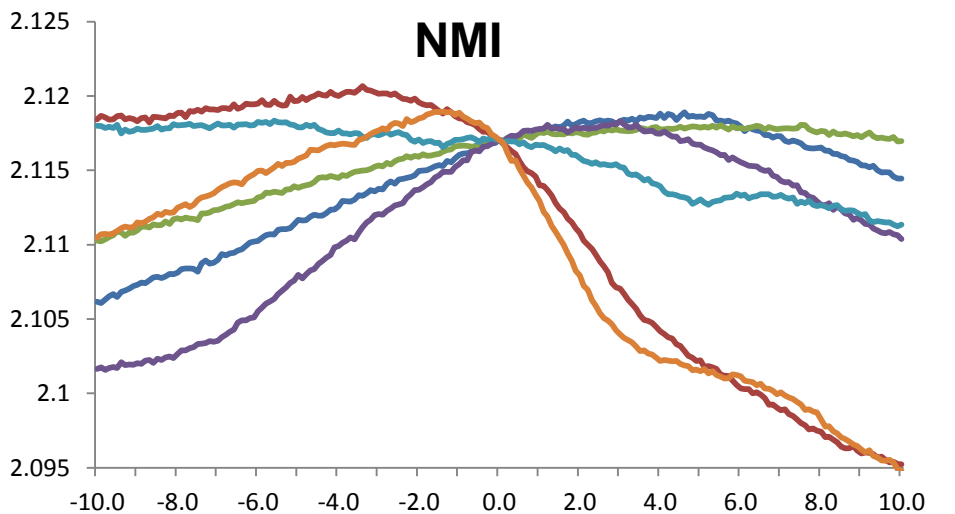
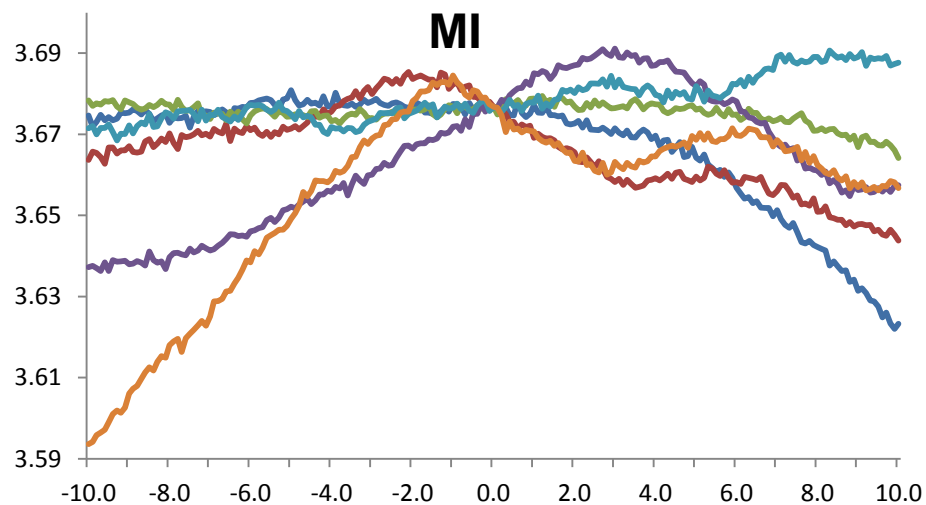
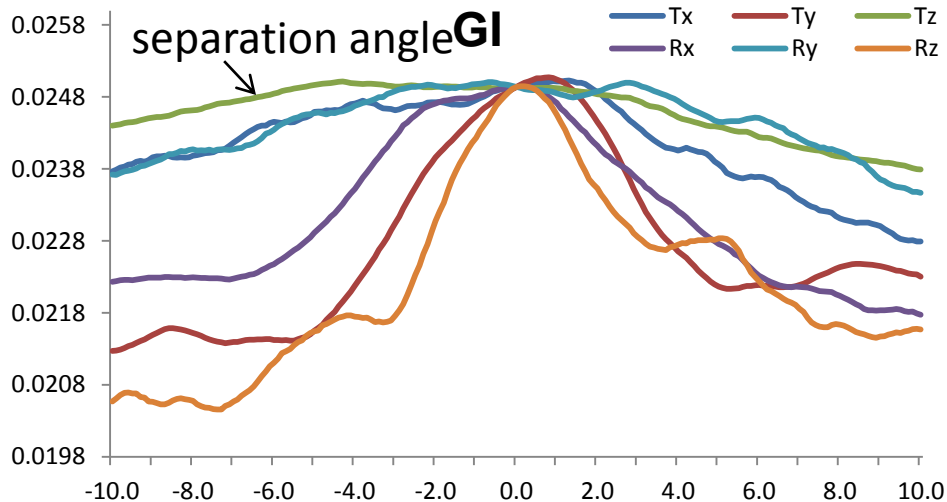
# Similarity Measures: Cadaver #2 (image intensifier)



Fixed images

Floating images

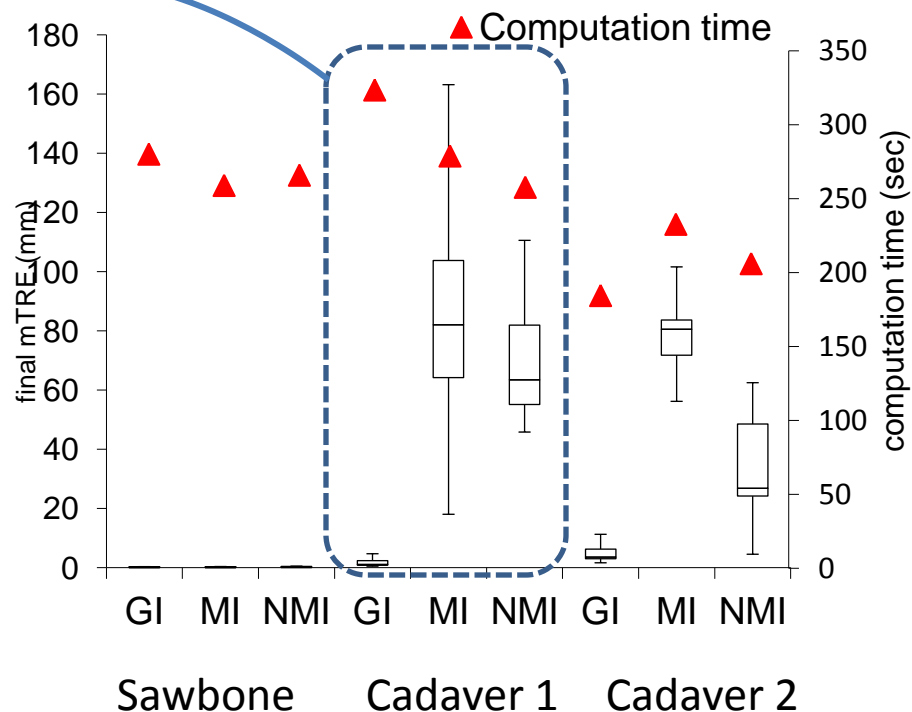
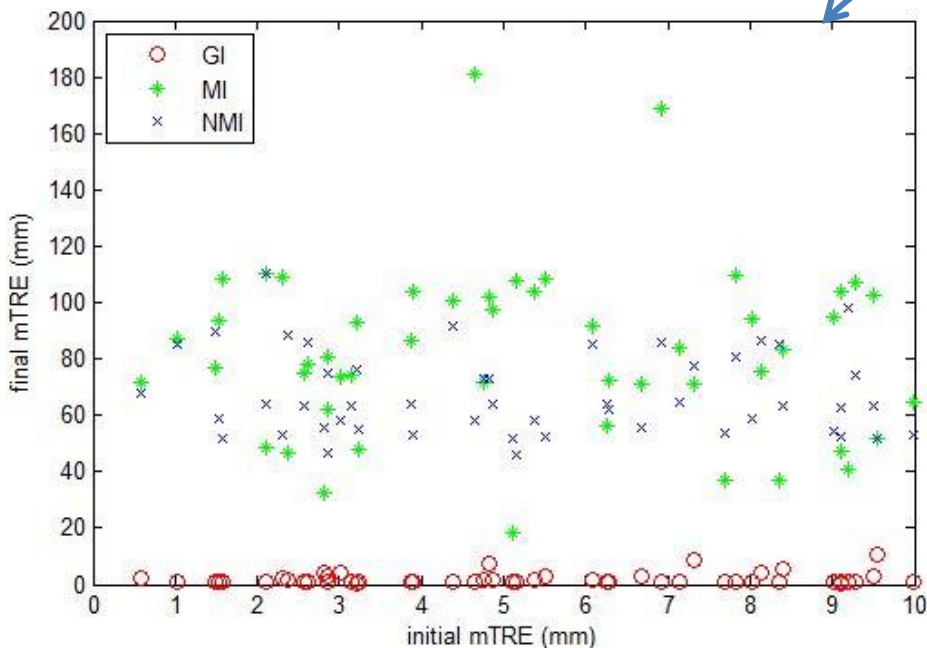
Due to small separation angle **GI**



Challenges: Soft tissue, metallic instruments, small separation angle

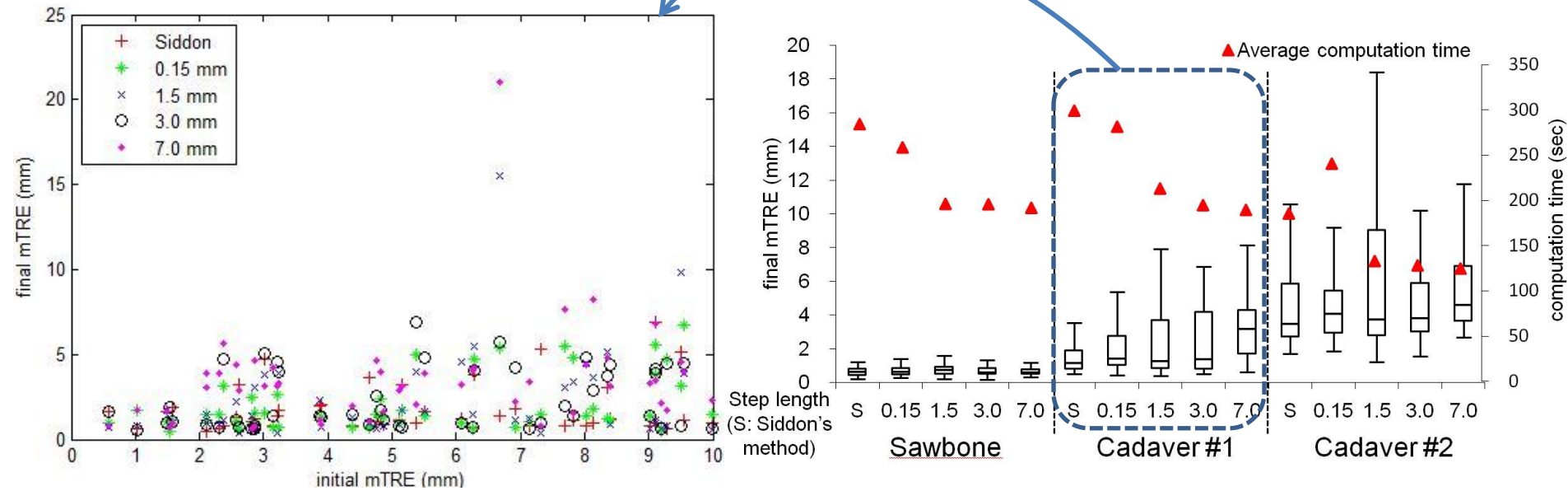
# Result of 50 trials: comparison of similarity measures

Cadaver #1 (2 images)



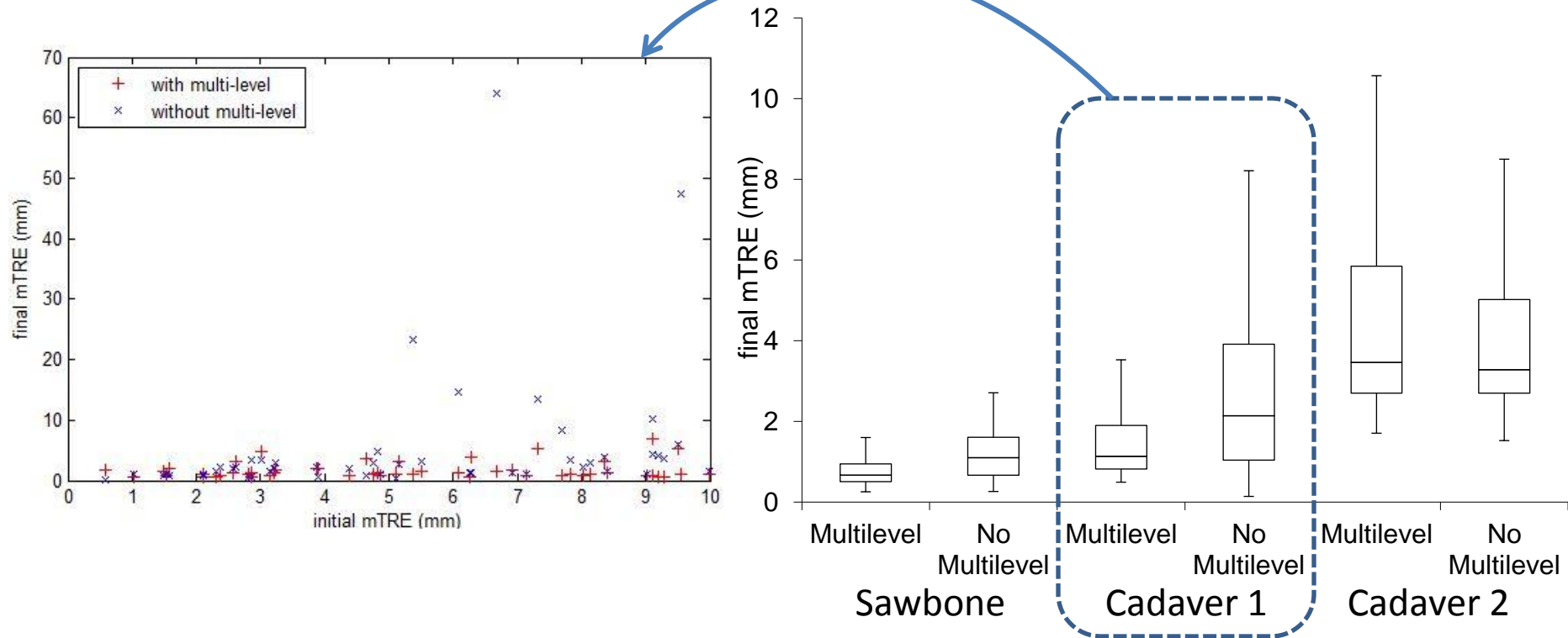
- All similarity measures showed almost the same performance in Sawbone images.
- GI worked significantly better than MI and NMI in cadaver images

# Comparison of DRR generator



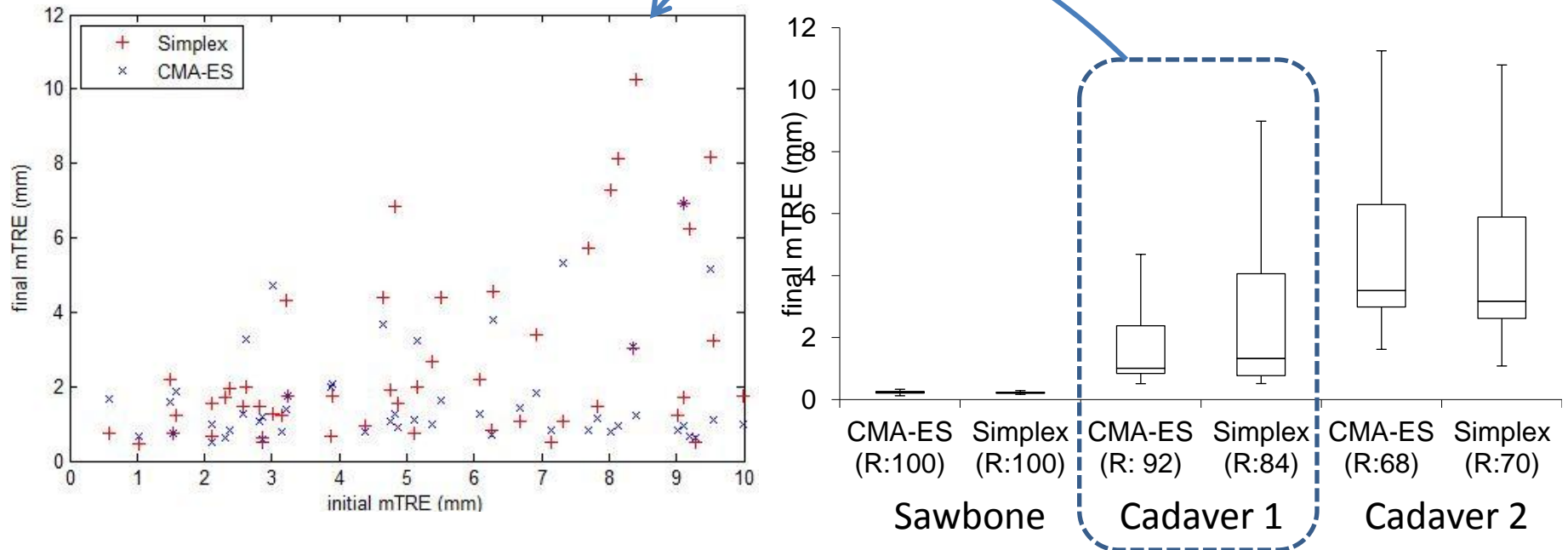
- Step length didn't affect registration result in Sawbone and Cadaver #2
- In Cadaver #1, increasing step length increased final mTRE

# Comparison of Optimization Strategy (coarse-to-fine multi-resolution optimization)



- The effect of coarse-to-fine multi-resolution strategy was statistically significant in Sawbone ( $P < 0.001$ ) and Cadaver 1 ( $P = 0.026$ )
- No significant difference was found in Cadaver 2 (because of the resolution of the original images?)

# Comparison of Optimizer



- In Cadaver #1 images, CMA-ES showed better precision than Downhill Simplex.
- Other two experiments showed no difference (To be confirmed by a statistical analysis)

# Summary

- In 3 experiments, mean TRE was  $0.229 \pm 0.042\text{mm}$ ,  $1.404 \pm 0.967\text{mm}$ ,  $3.241 \pm 0.756\text{mm}$ , respectively.
- GI worked significantly better than MI and NMI in presence of soft tissues.
- Coarse-to-fine multi-resolution strategy was significantly effective
- Registration accuracy may depend on the target anatomy, image quality as well as the geometries (separation angles) of each image.



# Next step

- Integration with navigation systems
  - Bone augmentation navigation system, TREK, etc.
- Further cadaver studies
- Integration with reconstruction algorithms that require registered prior CT
  - SxMAC, ROI recon, Hybrid recon, etc.