

Medical Robots, Constrained Robot Motion Control, and “Virtual Fixtures”

(Part 2)

Russell H. Taylor
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Disclosures & Acknowledgments

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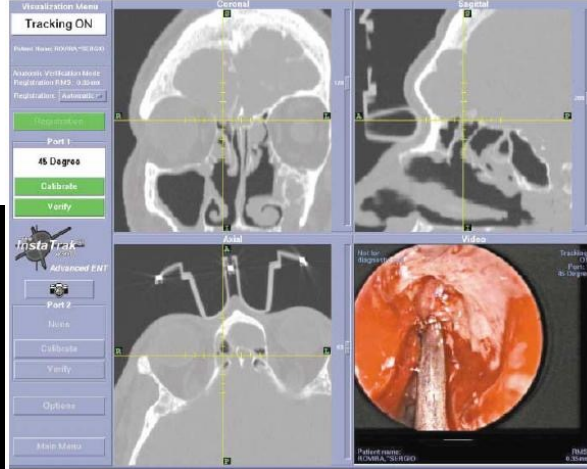
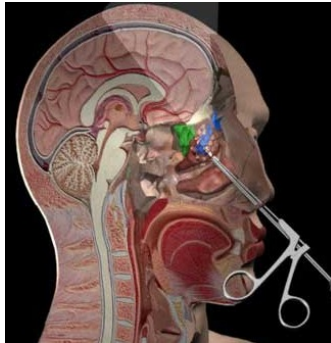
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Typical application domain: endoscopic sinus surgery



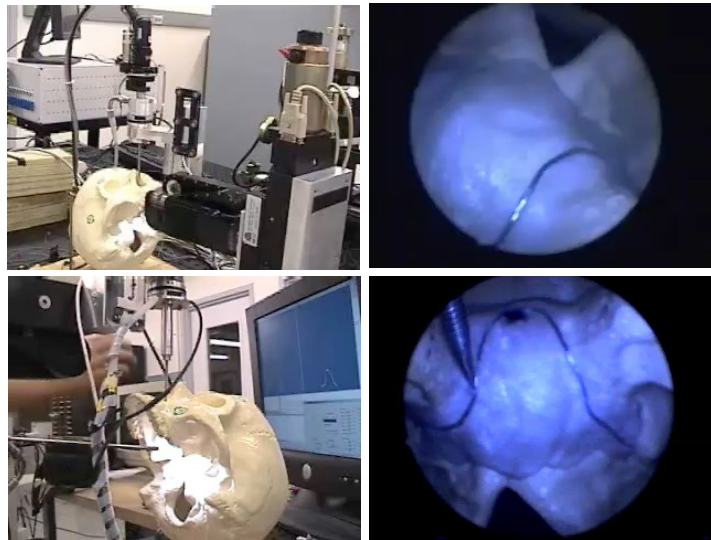
Kennedy, D.W., W.E. Bolger, S. J. Zinreich, J. Zinreich, *Diseases of the Sinuses: Diagnosis and Management*. 2001.

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Sample task: steady hand path tracing



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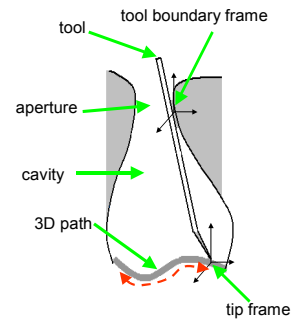
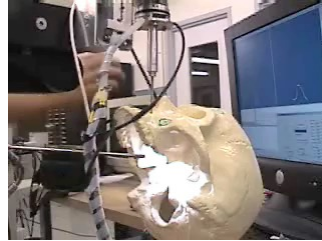
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Goal: robotically-assisted sinus surgery

- **Difficulties with conventional approach**
 - Complicated geometry
 - Safety-critical structures
 - Limited work space
 - Awkward tools
- **Our approach**
 - Cooperatively controlled “Steady hand” robot
 - Registered to CT models
 - “Virtual fixtures” automatically derived from models



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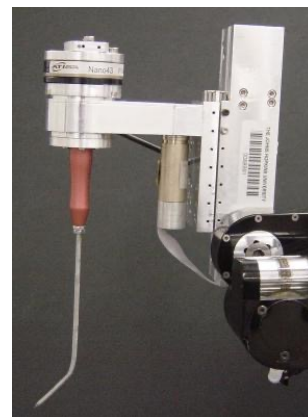
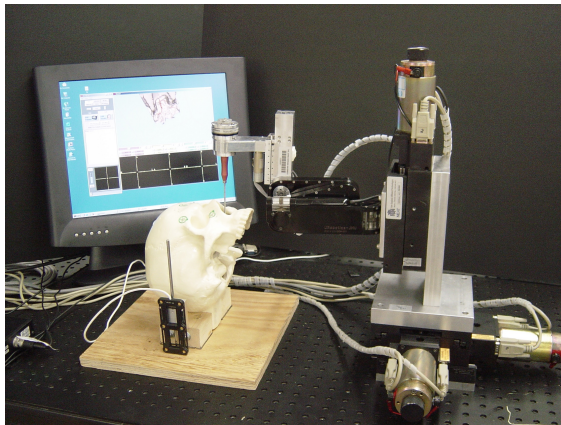
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Experiment Setup



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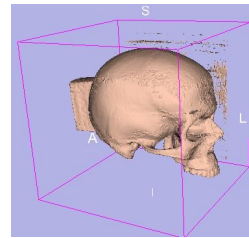
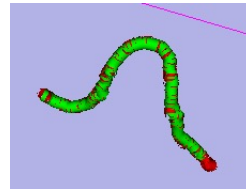
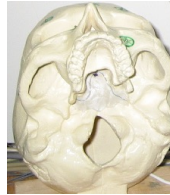
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Experimental setup

- Plastic Skull Phantom
 - Target path defined by embedded wire
 - Radioopaque fiducials implanted on skull for registration
- Computer model
 - Extracted from CT scan using standard software (Slicer)
- 3D tracking of tools, etc. using Northern Digital Optotrak®
- Co-register model, robot, and optical tracker using standard techniques



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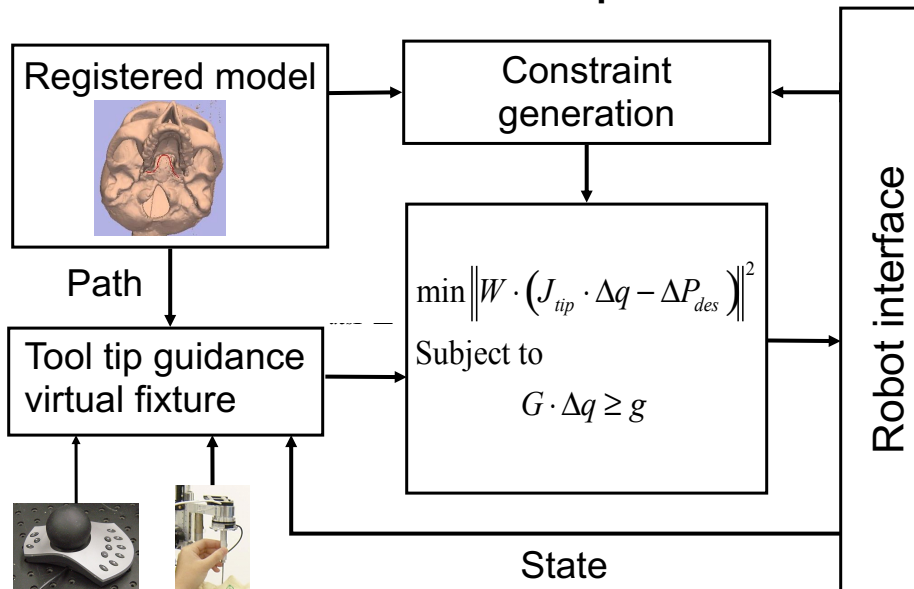
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Virtual Fixture Online Implementation



M. Li; R. Taylor; ICRA 2005

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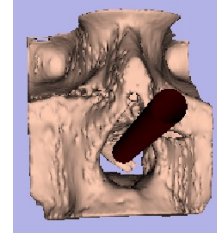
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Boundary Constraints Generation

- Anatomy – triangulated surface models
 - Patient-specific model of nose & sinus derived from CT
 - High complexity: 182,000 triangles & 99,000 vertices
- Tool shaft -- cylinder
- The boundary constraint generation requires us to find close-point pairs between boundary surface model & tool shaft



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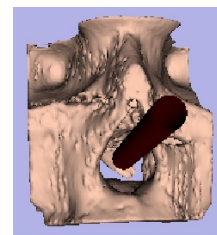
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 - Patient-specific model of nose & sinus derived from CT
 - High complexity: 182,000 triangles & 99,000 vertices
- Tool shaft -- cylinder
- The boundary constraint generation requires us to find close-point pairs between boundary surface model & tool shaft
- **Problem: How can we generate the right constraints in real time???**



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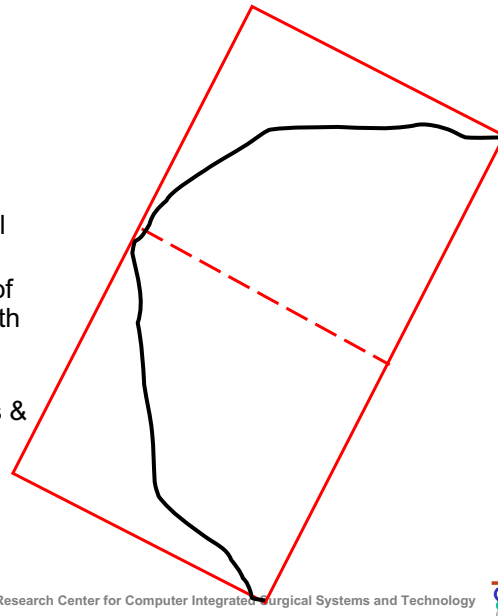


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Our solution: efficient search method using covariance tree representation of model

Covariance trees:

- Williams & Taylor, 1998; other authors
- Variation of k-d trees
- Basic idea:
 - Hierarchically split 3D model into sub-volumes
 - Realign coordinate system of each sub-volume to align with moments of inertia
- Produces bounding boxes that closely approximate boundaries & fast searches



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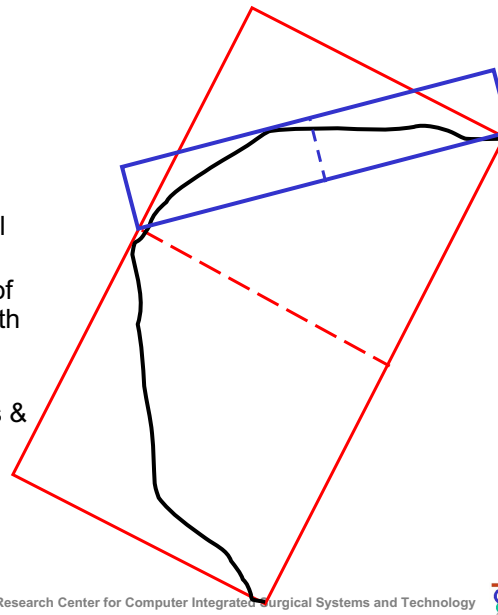


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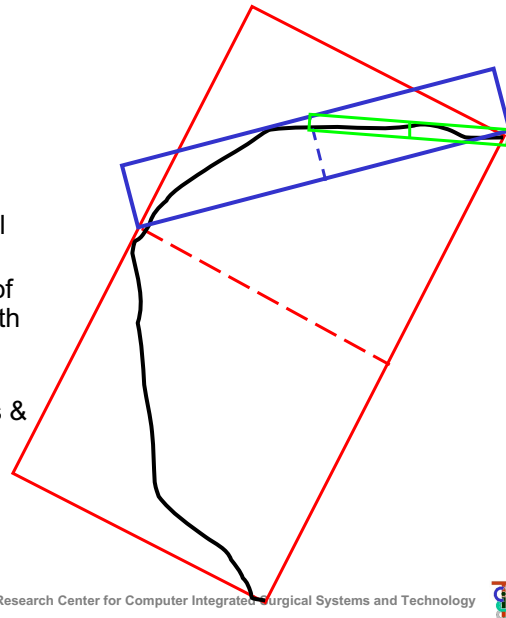


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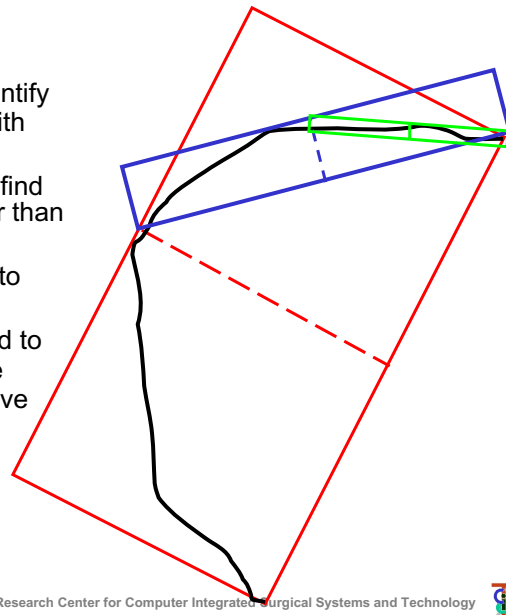


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One difference from ICP problem

One difference from ICP problem:

- Here we in principle need to identify all anatomy that can interfere with tool shaft
- Consequently modify search to find all triangle edges that are closer than some threshold to tool shaft
- Further modify to prune search to eliminate redundant constraints
- **NOTE:** Generally, you only need to consider surfaces that are close enough so that the tool may move there in one time step.



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Control Implementation

- Formulate constrained least squares problem
- Constraints & objective function include terms for desired tip motion, joint limits, boundary constraints

$$\zeta = \min_{\Delta q} \left\| \begin{bmatrix} W_{tip} & & \\ & W_k & \\ & & W_{joints} \end{bmatrix} \cdot \left(\begin{bmatrix} J_{tip}(q) \\ J_k(q) \\ I \end{bmatrix} \Delta q - \begin{bmatrix} \Delta P_{tip-des} \\ 0 \\ 0 \end{bmatrix} \right) \right\|$$

subject to $\begin{bmatrix} H_{tip} & & \\ & H_k & \\ & & H_{joints} \end{bmatrix} \cdot \begin{bmatrix} J_{tip}(q) \\ J_k(q) \\ I \end{bmatrix} (\Delta q) \geq \begin{bmatrix} h_{tip} \\ h_k \\ h_{joints} \end{bmatrix}$

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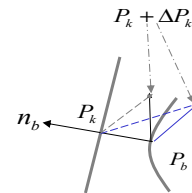
Control Implementation

- Tip frame $\Delta P_{tip} = J_{tip}(q) \cdot \Delta q$

$$\begin{aligned} & \|\Delta P_{tip} - \Delta P_{tip-des}\| \\ & \Delta P_{tip-d}^T \cdot \Delta P_{tip} \geq THD \end{aligned} \quad \begin{aligned} \min \quad & \zeta_{tip} = \|W_{tip} \cdot (J_{tip}(q) \Delta q - \Delta P_{tip-des})\| \\ \text{subject to} \quad & H_{tip-des} J_{tip}(q) \Delta q \geq h_{tip} \end{aligned}$$

- Boundary constraint $\Delta P_k = J_k(q) \cdot \Delta q$

$$\begin{aligned} & \|W_k \cdot \Delta P_k\| \\ & n_b^T \cdot (P_k + \Delta P_k - P_b) \geq d \end{aligned} \quad \begin{aligned} \min \quad & \zeta_k = \|W_k J_k(q) \Delta q\| \\ \text{subject to} \quad & H_k J_k(q) \Delta q \geq h_k \end{aligned}$$



- Joints limitation

$$\begin{aligned} & \|W_{joints} \cdot \Delta q\| \\ & q_{min} - q \leq \Delta q \leq q_{max} - q \end{aligned} \quad \begin{aligned} \min \quad & \zeta_{joints} = \|W_{joints} \Delta q\| \\ \text{subject to} \quad & H_{joints} \Delta q \geq h_{joints} \end{aligned}$$

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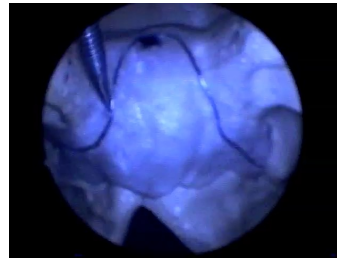
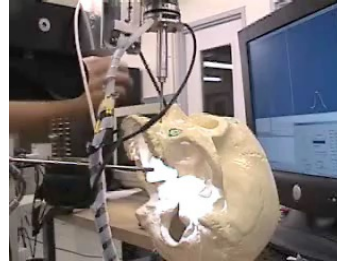
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Control implementation

- Solve problem numerically with standard methods (Lawson & Hanson, 1974)
- Performance:
 - 6 ms/iteration on 2GHz Pentium 4 PC
 - Typically 20 to 39 constraints



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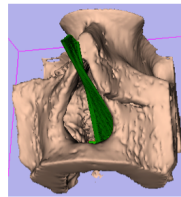
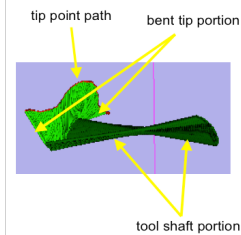
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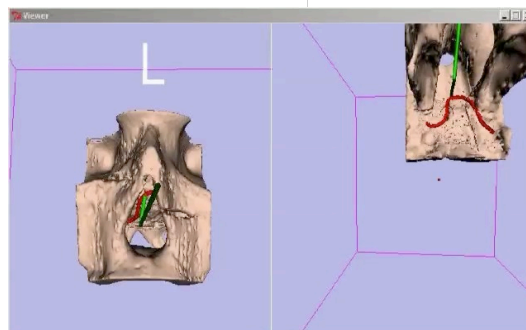


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Results



The average time in each control loop for the boundary searching is ~6ms



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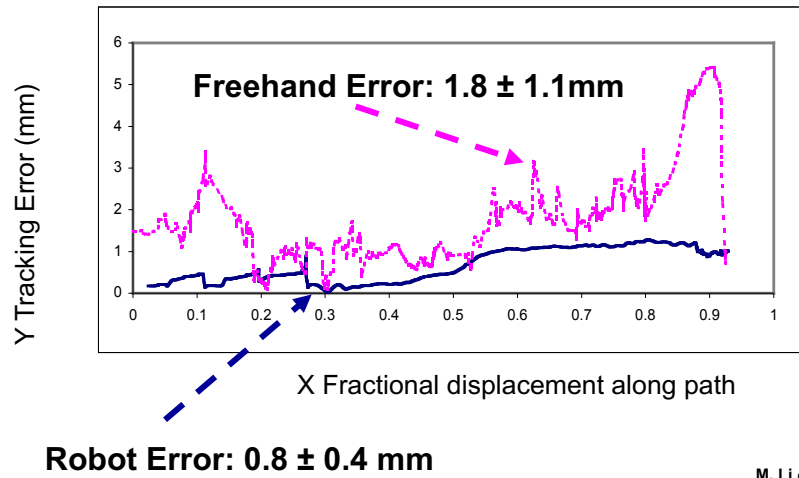
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Results: Robot vs Freehand



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Results: Robot vs Freehand

Trial#	Free hand		Robot Guidance	
	Average Error (mm)	Average Time (s)	Average Error (mm)	Average Time (s)
1	1.785	26.354	0.736	18.972
2	1.632	29.358	0.757	15.275
3	1.796	27.372	0.765	16.29
4	2.061	25.436	0.779	19.439
5	2.119	24.533	0.777	16.209
avg	1.819	26.611	0.763	17.237
std	1.126	1.863	0.395	1.848

Approx 1.5:1 improvement in time!

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Constraints when operating near to complex anatomy

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Anatomical Mesh-Based Virtual Fixtures for Surgical Robots

IROS 2020, Las Vegas

ZHAOSHUO (MAX) LI¹, ALEX GORDON², THOMAS LOOI², JAMES DRAKE², CHRISTOPHER FORREST², RUSSELL H. TAYLOR²

¹AUTHORS WITH LABORATORY FOR COMPUTATIONAL SENSING AND ROBOTICS, JOHNS HOPKINS UNIVERSITY, BALTIMORE, MARYLAND, USA

²AUTHORS WITH THE CENTER FOR IMAGE GUIDED INNOVATION AND THERAPEUTIC INTERVENTION LAB AT HOSPITAL FOR SICK CHILDREN, TORONTO, ONTARIO, CANADA

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Combine constraints

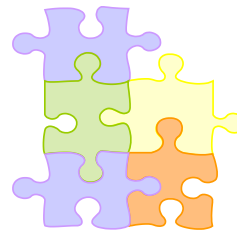
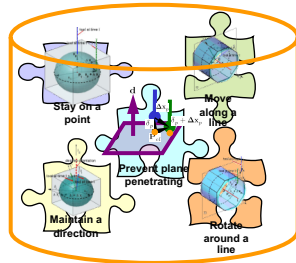
Single Frame

$$\begin{bmatrix} A_p \\ A_r \end{bmatrix} J(q) \cdot \Delta q \leq \begin{bmatrix} b_p \\ b_r \end{bmatrix}$$

Translational part (top), Rotational part (bottom)

Multiple Frame

$$\begin{bmatrix} A_1, 0 \\ \dots \\ 0, A_n \end{bmatrix} \begin{bmatrix} J_1(q) \\ \vdots \\ J_n(q) \end{bmatrix} \Delta q \leq \begin{bmatrix} b_1 \\ \vdots \\ b_n \end{bmatrix}$$



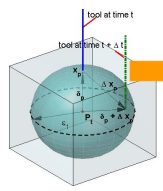
Customized virtual fixtures

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5 Basic Geometric Constraints (Virtual fixture library)



Stay on a point

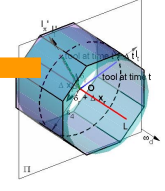
Optimization

$$\arg \min_{\Delta \vec{q}} C(\vec{x}(\vec{q} + \Delta \vec{q}), \vec{s}, \vec{x}^d)$$

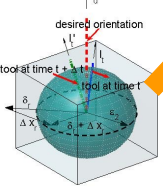
s. t. $A(\vec{x}(\vec{q} + \Delta \vec{q}), \vec{s}) \leq \vec{b}$,

$$\vec{s}_{up} \geq s \geq \vec{s}_{low} \geq 0,$$

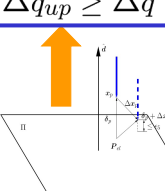
$$\Delta \vec{q}_{up} \geq \Delta \vec{q} \geq \Delta \vec{q}_{low}$$



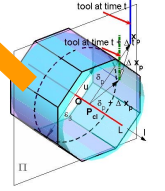
Move along a line



Maintain a direction



Prevent plane penetrating



Rotate around a line

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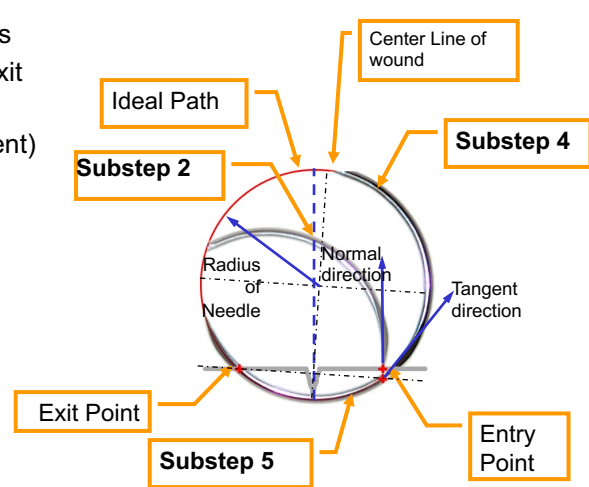
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Example: Suturing

The suturing task involves

- Select entry and exit points
- Align (Move & Orient) Needle
- Bite: Pass Needle
- Loop
- Knot



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Suturing: Align Step

0. Move Along a Line

1. Stay at a point + Rotate about a line

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Suturing: Align Step

2. Stay at a point + Rotate about a line

3. Puncture

4. Stay at a point + Rotate about a line

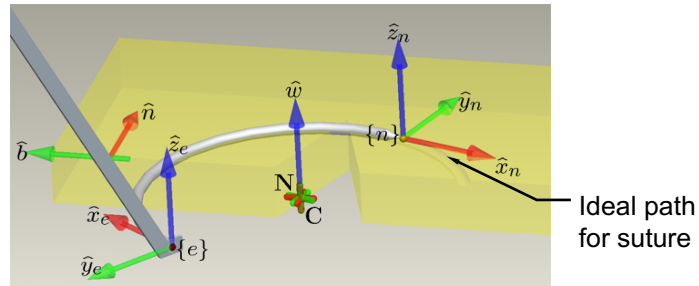
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Suturing: Bite Step



- Ideal trajectory is a circle with radius equal to needle radius.
- Needle plane is parallel to entry and exit points and surface normal.

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Suturing: Results

The average error (mm) in ideal and actual points as measured by OptoTrak[®]
Preliminary data collected from 4 users 5 trials each.

Error	Entry (mm)	Exit (mm)
Robot	0.6375; $\sigma = 0.12$	0.7742; $\sigma = 0.37$
Manual	--	2.1; $\sigma = 1.2$

- Suturing task using VF showed significant improvement in performance over freehand.
 - Can be performed at awkward angles
 - Avoids multiple trials and large undesirable movements inside tissue.

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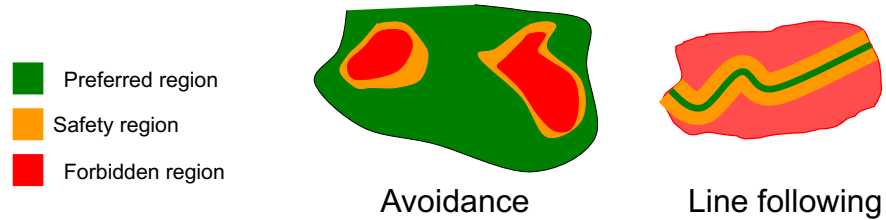
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Hard and soft constraints



- Constraints on the task can be “hard” or “soft”
- The relative sizes depend on the procedure, ranging from micros to tenths of millimeter.
- Soft constraints allow the controller to accommodate uncertainties inherent in surgical procedures.

Thanks: A. Kapoor

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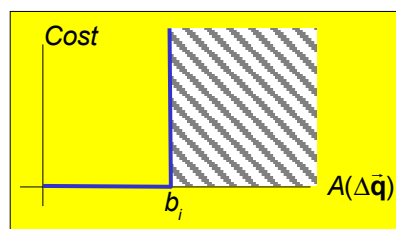
“Soft” constraint implementation

Suppose that we have a problem of the form

$$\Delta \vec{q}_{\text{des}} = \arg \min \|\mathbf{E}(\Delta \vec{q})\|^2$$

subject to a constraint of the form

$$A_i(\Delta \vec{q}) \leq b_i$$



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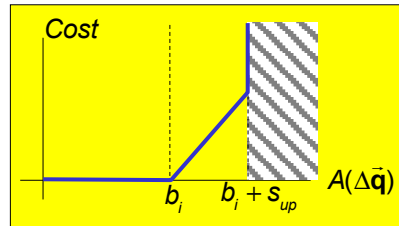
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“Soft” constraint implementation

But suppose we want to make the barrier “soft”. I.e., allow the robot to go beyond the barrier at increasing cost until it hits a harder barrier later



Add an explicit slack s_i and add a penalty term to the objective function

$$\Delta \bar{\mathbf{q}}_{\text{des}} = \arg \min \|\mathbf{E}(\Delta \bar{\mathbf{q}})\|^2 + \eta_i s_i^2$$

subject to a constraint of the form

$$A_i(\Delta \bar{\mathbf{q}}) - s_i \leq b_i$$

$$0 \leq s_i \leq s_{up,i}$$

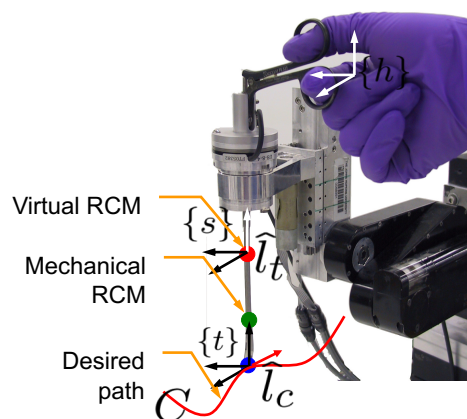
This process can be repeated several times to produce progressively steeper costs



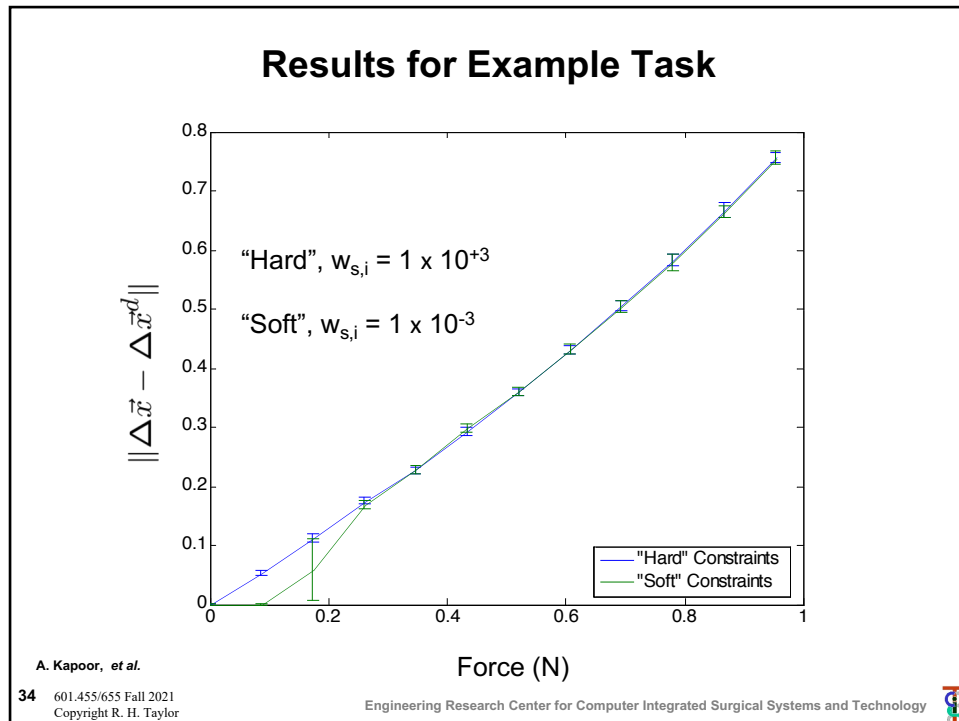
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Example Task

- Constraint 1: Tip to move along curve C
- Constraint 2: Origin of $\{s\}$ to move along
- Objective: Handle to follow user input



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Nonlinear Optimization

- One problem with linearized least squares is the proliferation of constraints to approximate the real constraints
- Consequently, it is worth considering alternatives that can handle more general formulas “directly”

$$\Delta \vec{q}_{des} = \underset{\Delta \vec{q}}{\operatorname{arg\,min}} C(\Delta \vec{x}, \Delta \vec{q}, \vec{s})$$

subject to

$$\Delta \vec{x} = \mathbf{J} \Delta \vec{q}$$

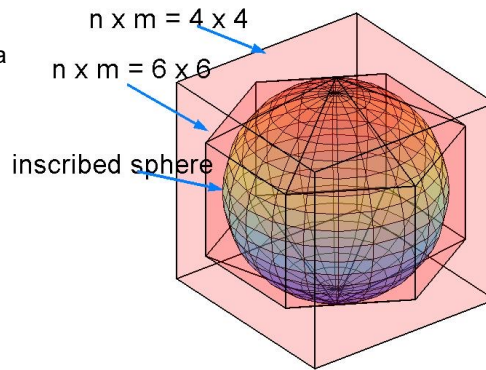
$$\mathbf{A}(\Delta \vec{x}, \Delta \vec{q}, \vec{s}) \leq \vec{b}$$

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Linear approximation for constraints

- $n \times m$ increase
 - Polyhedron approaches the inscribed sphere
 - Linearized conditions are a better approximation
 - More constraints require more time to solve the optimization problem
- Symmetrical polyhedron
 - $n \times m = 4 \times 4$
- Bounded polyhedron
 - $n \times m = 3 \times 3$



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Nonlinear Optimization

- One problem with linearized least squares is the proliferation of constraints to approximate the real constraints
- Consequently, it is worth considering alternatives that can handle more general formulas “directly”

$$\Delta \bar{\mathbf{q}}_{des} = \underset{\Delta \bar{\mathbf{q}}}{\operatorname{argmin}} C(\Delta \bar{\mathbf{x}}, \Delta \bar{\mathbf{q}}, \bar{\mathbf{s}})$$

subject to

$$\Delta \bar{\mathbf{x}} = \mathbf{J} \Delta \bar{\mathbf{q}}$$

$$\mathbf{A}(\Delta \bar{\mathbf{x}}, \Delta \bar{\mathbf{q}}, \bar{\mathbf{s}}) \leq \bar{\mathbf{b}}$$

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Using Non-Linear Constrained Optimization

- Use Sequential Quadratic Program* method
- SQP solves the following problem iteratively

$$\mathbf{d}^{(k)} = \arg \min_{\mathbf{d}^{(k)}} \nabla C(\mathbf{x}(\mathbf{q} + \Delta \mathbf{q}^{(k)}), \mathbf{s}^{(k)}, \mathbf{x}^d)^T \mathbf{d}^{(k)} + \frac{1}{2} \mathbf{d}^{(k)T} \mathbf{B}^{(k)} \mathbf{d}^{(k)}$$

$$\text{s. t. } \nabla A_j(\mathbf{x}(\mathbf{q} + \Delta \mathbf{q}^{(k)}), \mathbf{s}^{(k)})^T \mathbf{d}^{(k)} \leq b_j; \quad j \in \mathcal{A}_k$$

- Start with a solution $[\Delta \mathbf{q}^k, \mathbf{s}^k]^t$
- Descent direction along with step size determine next solution $[\Delta \mathbf{q}^{k+1}, \mathbf{s}^{k+1}]^t$

*P. Spellucci, *Math. Prog.*, '98

A. Kapoor, *et al.*

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Remarks: Non-Linear Constraints

- Current incremental motion can be used as starting guess for next motion
- Worst case number of constraints n times m , $n = \#$ variables, $m = \#$ nonlinear constraints
- Analytical gradient increases speed

A. Kapoor, *et al.*

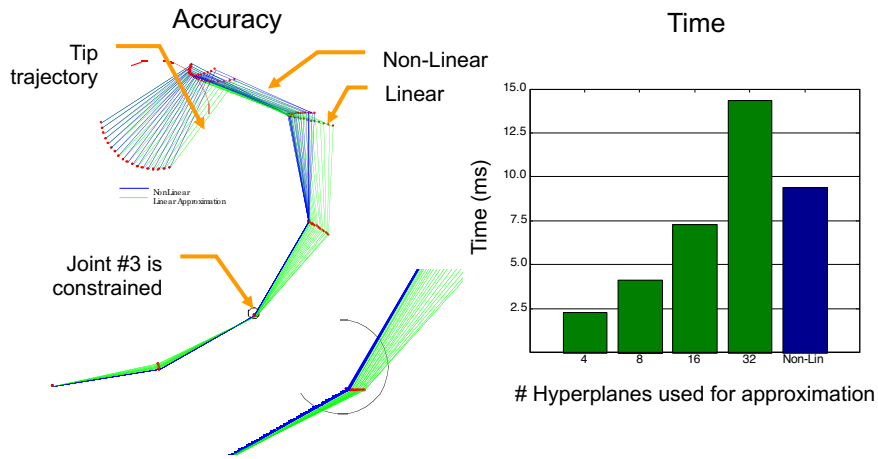
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Linear v. Non-Linear Constraints



A. Kapoor, et al.

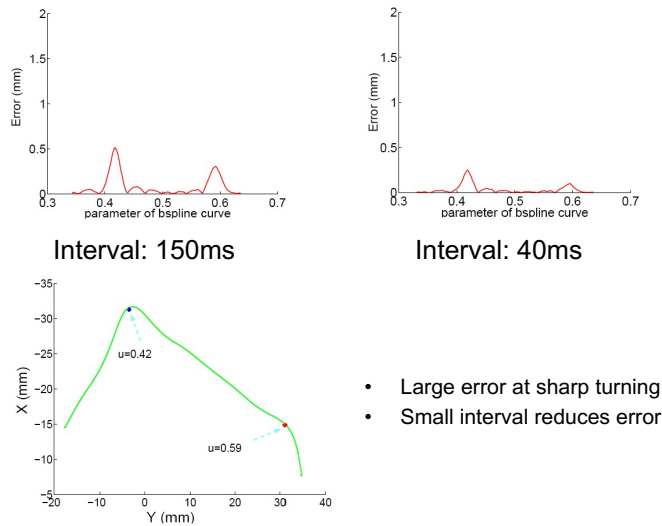
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Effect of increasing control-loop time



- Large error at sharp turning
- Small interval reduces error

Ming Li et al., IROS '05

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Longer Straight Line Motions

- In many cases, one wants to command a fairly long "straight line" motion from some initial pose to a final goal pose.
- This can be done fairly straightforwardly as follows:

\mathbf{F}_0 = initial pose; \mathbf{F}_G = goal pose;

$\dot{\theta}_{\max}$ = max angular velocity; v_{\max} = max linear speed

Define $\mathbf{F}_{G0} = [\mathbf{R}_{G0}, \vec{\mathbf{p}}_{G0}]$ such that $\mathbf{F}_G \mathbf{F}_{G0} = \mathbf{F}_0$

Compute axis-angle representation for $\mathbf{R}_{G0} = \text{Rot}(\vec{\mathbf{n}}_{G0}, \theta_{G0})$

Compute $T_{\text{move}} = \max(\theta_{G0} / \dot{\theta}_{\max}, \|\vec{\mathbf{p}}_{G0}\| / v_{\max})$; $T_{\text{left}} = T_{\text{move}}$

while $T_{\text{left}} > 0$ do

Wait for next time interval

Perform housekeeping; input state $(\vec{\mathbf{q}}, \dot{\vec{\mathbf{q}}}$, forces, etc.)

$T_{\text{left}} \leftarrow \max(T_{\text{left}} - \Delta T, 0)$; $\lambda \leftarrow T_{\text{left}} / T_{\text{max}}$; $\mathbf{F}_T \leftarrow \mathbf{F}_G \bullet [\mathbf{R}(\vec{\mathbf{n}}_{G0}, \lambda \theta_{G0}), \lambda \vec{\mathbf{p}}_{G0}]$

Set up optimization function to minimize $\|\mathbf{F}_T^{-1} \mathbf{F}(\vec{\mathbf{q}} + \Delta \vec{\mathbf{q}})\|^2$

Output velocity goal $\Delta \vec{\mathbf{q}} / \Delta T$

end

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Longer Straight-Line Motions

To minimize $\|\mathbf{F}_T^{-1} \mathbf{F}(\vec{\mathbf{q}} + \Delta \vec{\mathbf{q}})\|^2$ we actually want to try to make $\mathbf{F}_T \approx \mathbf{F}(\vec{\mathbf{q}} + \Delta \vec{\mathbf{q}}) = \mathbf{F}(\vec{\mathbf{q}}) \Delta \mathbf{F}(\vec{\xi})$

in a least-squares sense, where $\vec{\xi} = \mathbf{J}_{\text{kins}}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}}$ and $\vec{\xi} = [\vec{\alpha}^T, \vec{\epsilon}^T]^T$

$$\Delta \mathbf{R} \approx \mathbf{R}(\vec{\mathbf{q}})^{-1} \mathbf{R}_T = \text{Rot}(\vec{\mathbf{n}}_{RT}, \theta_{RT})$$

$$\vec{\mathbf{p}}_T \approx \mathbf{R}(\vec{\mathbf{q}}) \vec{\epsilon} + \mathbf{p}(\vec{\mathbf{q}})$$

This gives us the following minimization

$$\Delta \vec{\mathbf{q}} = \arg \min_{\Delta \vec{\mathbf{q}}} \nu_{\alpha} \|\vec{\alpha} - \vec{\theta}_{RT}\|^2 + \nu_{\epsilon} \|\mathbf{R}(\vec{\mathbf{q}}) \vec{\epsilon} + \mathbf{p}(\vec{\mathbf{q}}) - \vec{\mathbf{p}}_T\|^2$$

subject to

$$\vec{\alpha} = \mathbf{J}_{\text{kins}}^{\alpha}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}} \quad \vec{\epsilon} = \mathbf{J}_{\text{kins}}^{\epsilon}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}}$$

... other constraints such as joint limits, virtual fixture constraints, etc.

where ν_{α} and ν_{ϵ} can be used to control the relative importance of orientation and translation

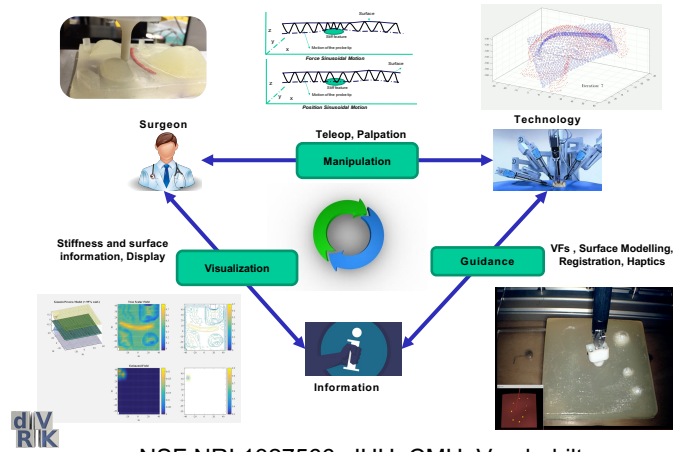
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Complementary Situational Awareness in a Robotic Surgical Assistant



NSF NRI 1327566: JHU, CMU, Vanderbilt

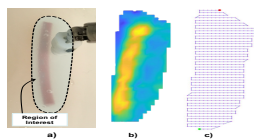
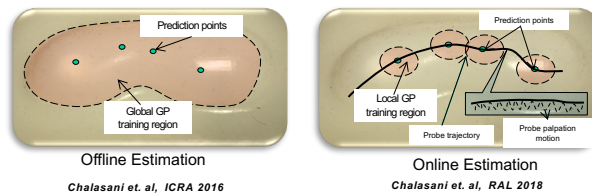
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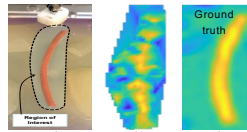
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CONTINUOUS STIFFNESS AND GEOMETRY UPDATE

Preetham Chalasani, Russell Taylor



Results from automated Sinusoidal palpation



Teleoperated palpation w. superimposed motion



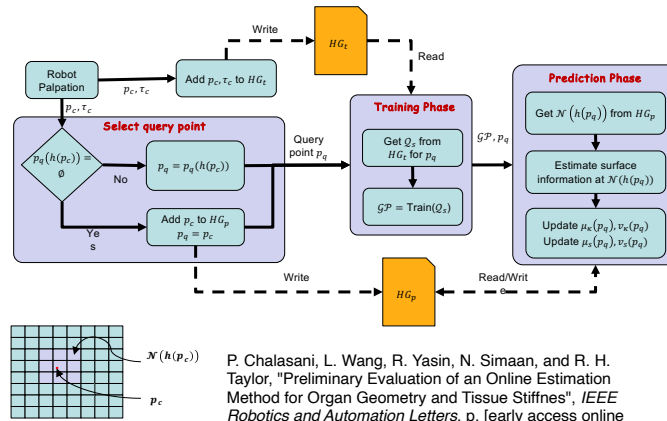
Automated Sinusoidal Palpation

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Online Geometry and Stiffness Update



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Hamlyn Demo

Constrained Semi-Autonomous Telemanipulated Palpation with Assistive Virtual Fixtures

Preetham Chalasani, Long Wang, Rashid Yasin,
Peter Kazanzides, Nabil Simaan and Russell H. Taylor

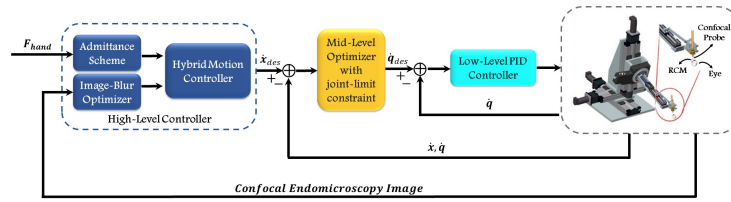


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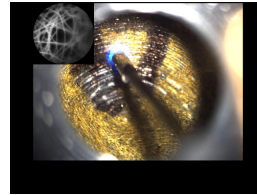
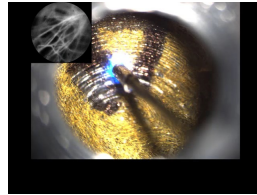
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Robot-assisted confocal endoscopic imaging for retinal surgery



Simple hand guiding with robot (5 DoF)



Hybrid control:

- Hand-guided lateral motion
- Image-based depth/focus control

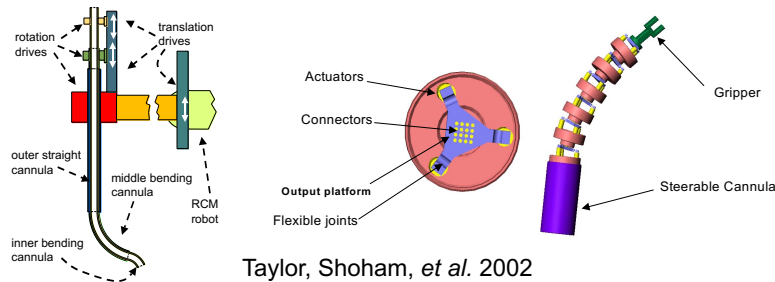
Z. Li, M. Shahbazi, M. Patel, P. Chalasani, E. O'Sullivan, H. Zhang, K. Vyas, A. Deguet, P. Gehlbach, I. Iordachita, G. Z. Yang, R. H. Taylor, "A Comparison of Cooperative vs. Teleoperated Robot-Assisted Frameworks for Confocal Endomicroscopy Scanning of the Retina", *IEEE TMRB*, in submission.

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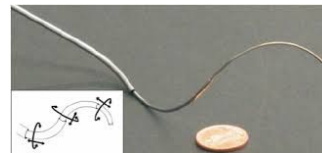
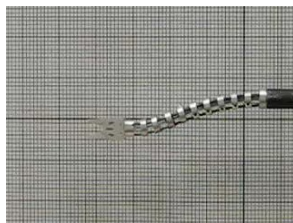
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High Dexterity in a Small Package



Taylor, Shoham, *et al.* 2002



Webster *et al.*, 2006

Simaan, Taylor *et al.* 2004, 2007

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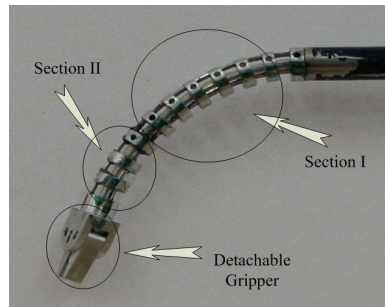
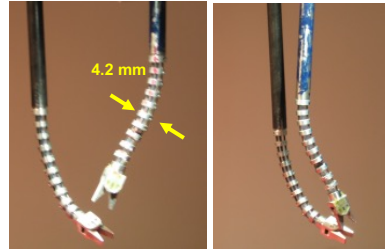
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Scalable Robot for Dexterous Surgery in Small Spaces (aka Snake Like Robot)



Team: A. Kapoor, Kai Xu, Wei Wei, N. Simaan,
P. Kazanzides, R. H. Taylor
Collaborator: P. Flint, MD

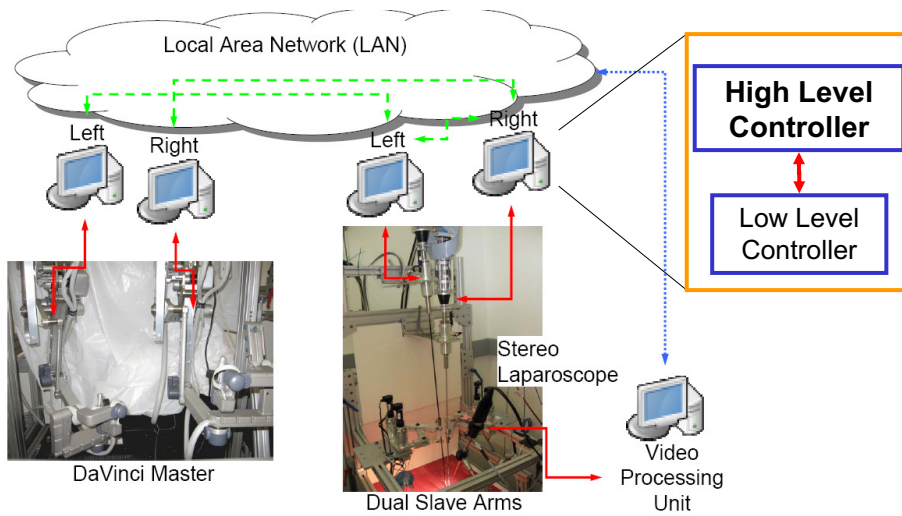


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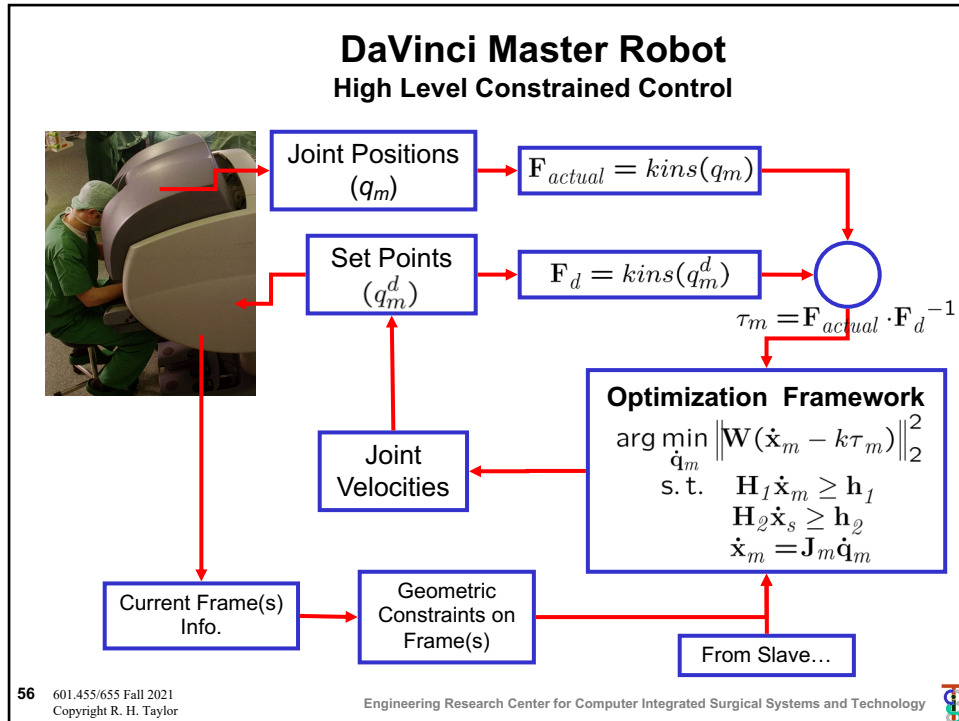
Snake Like Robot System Architecture



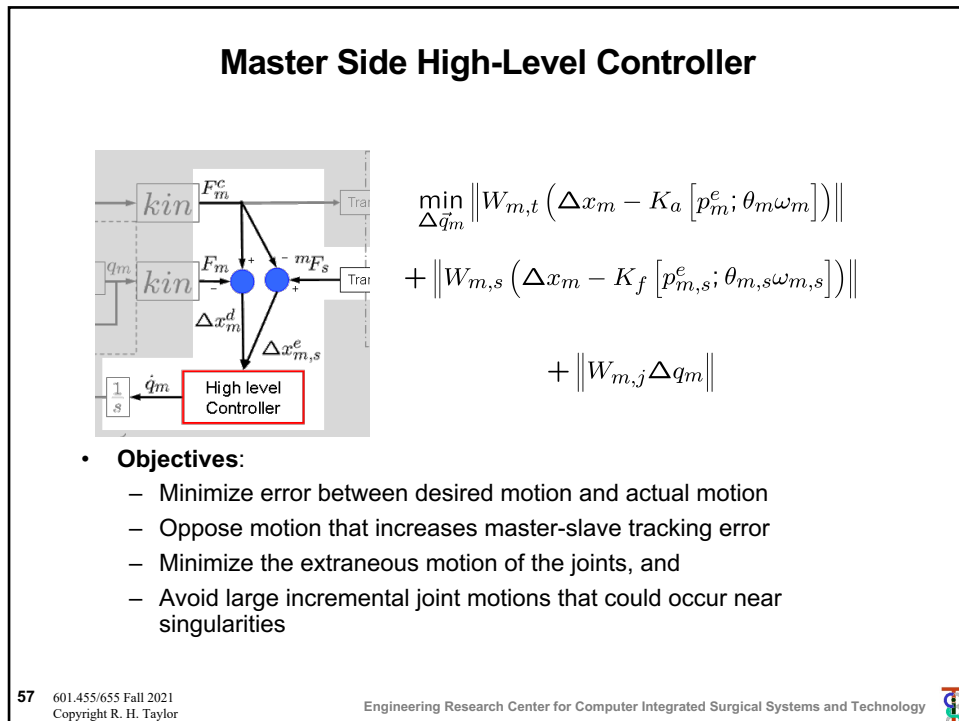
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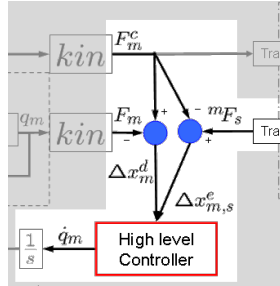


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Master Side High-Level Controller



that is
$$H_m \Delta q_m \geq h_m$$

$$\begin{bmatrix} I \\ -I \\ I \\ -I \end{bmatrix} \Delta q_m \geq \begin{bmatrix} q_{m,L} - q_m \\ q_m - q_{m,U} \\ \dot{q}_{m,U} \cdot \Delta t \\ \dot{q}_{m,U} \cdot \Delta t \end{bmatrix}$$

- **Constraints:**

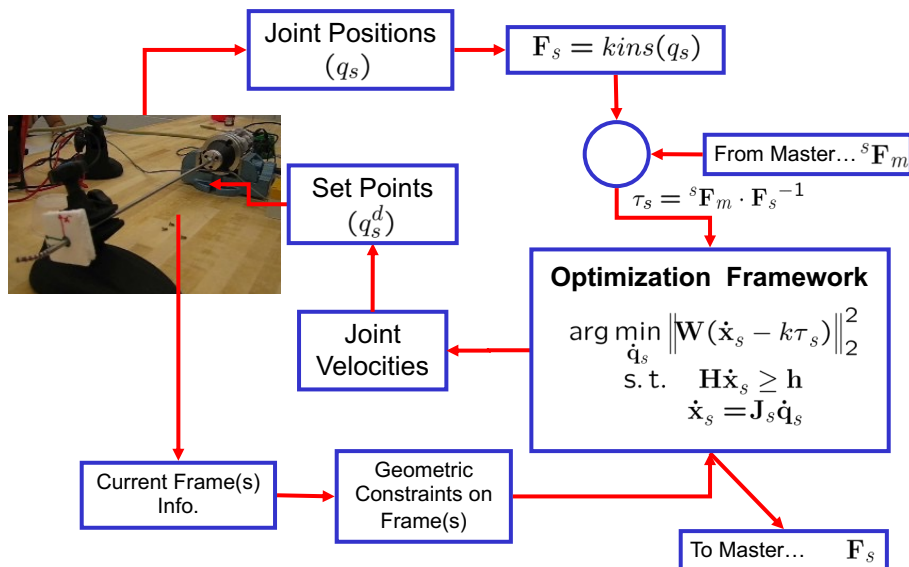
- General form: $H_{m,j} + \Delta q_m \geq h_{m,j}$
- Not allow motion outside joint range
- Not allow motion that exceeds joint velocity limits
- Additional constraints can be added from the VF Library

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DaVinci Slave Robot High Level Constrained Control



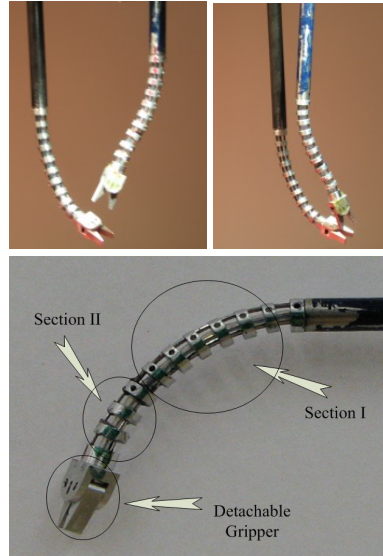
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Slave-Side Snakes

- Actual snake section bends are a fairly complicated function of the linear displacements of the individual tubes and wires in the bending parts. But these displacements can be computed from the desired bending angles.
- Therefore, create pseudo-"joints" q_{sec1} and q_{sec2} corresponding to the bending angles in the two bend sections.
- Solve the optimization problem for q_{sec1} and q_{sec2} and the other joint angles of the slave robot. Then compute linear displacements from q_{sec1} and q_{sec2} . This also involves some calculations for redundancy resolution that can be done with a similar optimization method or can be done analytically.



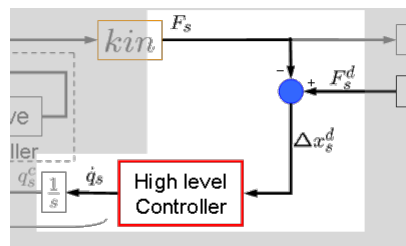
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Slave Side High-Level Controller



$$\min_{\Delta \vec{q}_s} \left\| W_{s,t} \left(\Delta x_s - K_a \left[p_s^e; \theta_s \omega_s \right] \right) \right\|$$

$$+ \left\| W_{s,j}(q) \Delta q_s \right\|$$

$$+ \left\| W_{s,s} \right\|$$

- Objectives:**
 - Minimize error between desired motion and actual motion
 - Minimize the extraneous motion of the joints, and
 - Avoid large incremental joint motions that could occur near singularities

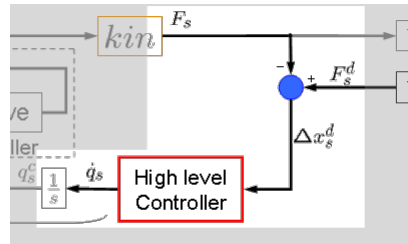
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Slave Side High-Level Controller



such that
$$\begin{bmatrix} I \\ -I \\ I \\ -I \end{bmatrix} \Delta q_s \geq \begin{bmatrix} q_{s,L} - q_s \\ q_s - q_{s,U} \\ \dot{q}_{s,U} \cdot \Delta t \\ \dot{q}_{s,U} \cdot \Delta t \end{bmatrix}$$

and
$$\begin{aligned} \|\vec{d}\| + \Delta x_b \cdot \hat{d} \\ + \vec{v} \cdot \hat{d} + s &\geq d_{safe} \\ 0 \leq s &\leq s_{lim} \end{aligned}$$

- **Constraints:**

- Not allow motion outside joint range
- Not allow motion that exceeds joint velocity limits
- **Collision avoidance between slaves**
- More constraints can be added from the VF Library

