Medical Robots, **Constrained Robot Motion Control.** and "Virtual Fixtures"

(Part 1)

Russell H. Taylor 601.455/655

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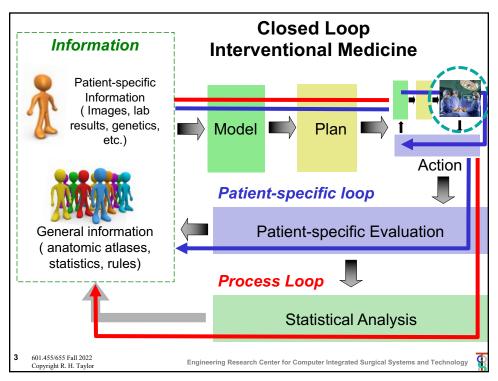
Disclosures & Acknowledgments

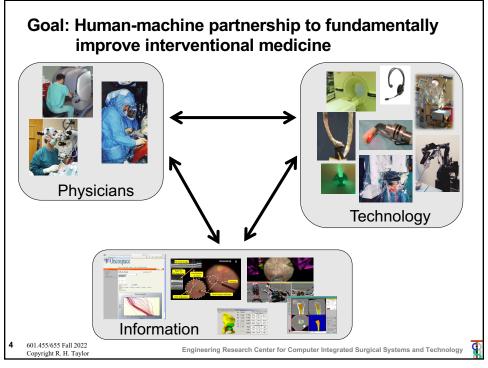
- This is the work of many people
- Some of the work reported in this presentation was supported by fellowship grants from Intuitive Surgical and Philips Research North America to Johns Hopkins graduate students and by equipment loans from Intuitive Surgical, Think Surgical, Philips, Kuka, and Carl Zeiss Meditec.
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Complementary Capabilities

Humans

- · Excellent judgment & reasoning
- Excellent optical vision
- Cannot see through tissue
- Do not tolerate ionizing radiation
- · Limited precision, hand tremor
- · No stereotactic accuracy
- · Moderately strong
- High dexterity ("human" scale)
- · Big hands and bodies
- Reasonable force sensitivity
- Must rely on memory of preoperative plans and data

Robots

- No judgment
- Limited vision processing
- · Can use x-rays, other sensors
- · Do not mind radiation
- · High precision
- High stereotactic accuracy
- · Variable strength
- · Dexterity at different scales
- · Variable sizes
- Can sense very small forces
- Can be programmed to use preoperative plans and data

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Common classes of medical robots

- Surgical "CAD/CAM" systems
 - Goal is accurate execution of surgical plans
 - Typically based on medical images
 - Planning may be "online" or "offline"
 - Execution is often at least semi-autonomous but may still involve interaction with humans
 - Examples: Orthopaedic robots, needle placement robots, radiation therapy robots
- Surgical "assistant" systems
 - Emphasis is on interactive control by human
 - Human input may be through hand controllers (e.g., da Vinci), hand-over-hand (e.g., Mako, JHU "steady hand" robots)
 - Typically augmenting or supplementing human ability
 - Common applications include MIS, microsurgery
- · Note that the distinction is really somewhat arbitrary
 - Most real systems have aspects of both.

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Image-guided needle placement

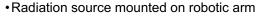
Steerable Needle Channel Rectal Sheath Imaging Coil She

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Image Guided Radiotherapy



- Automatic segmentation of targets
- Automated planning radiation beam path
- Image guide patient motion compensation for more accurate radiation targeting



Cyberknife





Slide credit: Howie Choset + RHT



http://www.varian.com/us/oncology/radiation_oncology/trilogy/

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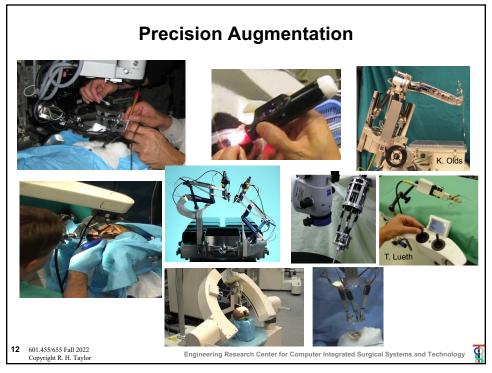
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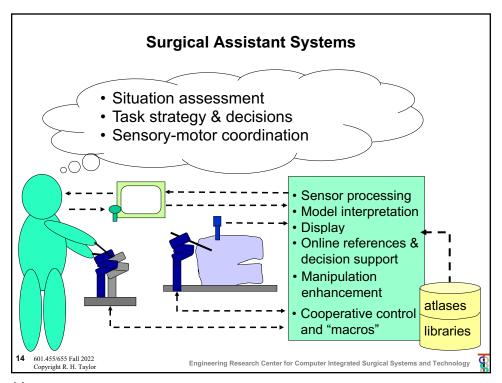
Common classes of medical robots

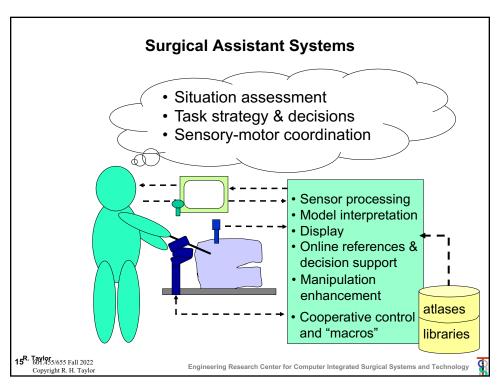
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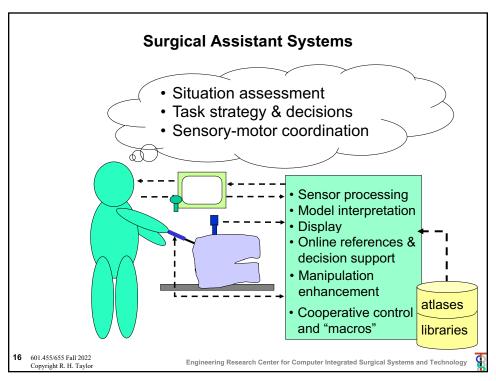
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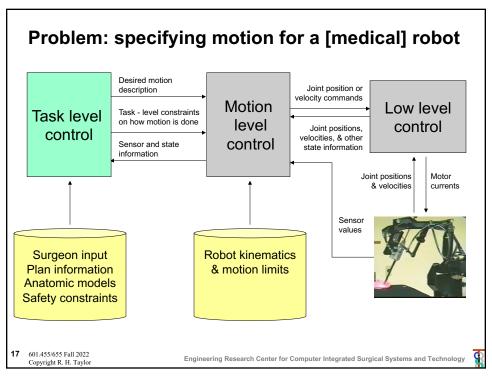
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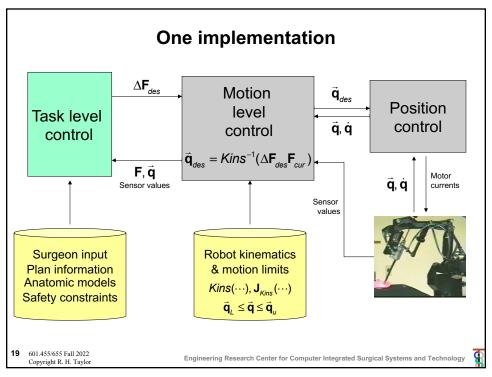
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Background: Jacobean Robot Motion Control

Let $\mathbf{F}=[\mathbf{R},\vec{\mathbf{p}}]$ be the current pose of a robot end effector and $\vec{\mathbf{q}}=[q_1,\cdots,q_N]$ be the current joint position values corresponding to \mathbf{F} . I.e., $\mathbf{F}=Kins(\vec{\mathbf{q}})$, where $Kins(\cdots)$ is a function computing the "forward kinematics" of the robot.



Pose
$$\mathbf{F}(\vec{\mathbf{q}} + \Delta \vec{\mathbf{q}}) = kins(\vec{\mathbf{q}} + \Delta \vec{\mathbf{q}})$$

$$\Delta \mathbf{F} \cdot \mathbf{F} = kins(\vec{\mathbf{q}} + \Delta \vec{\mathbf{q}})$$

$$\Delta \mathbf{F} = kins(\vec{\mathbf{q}} + \Delta \vec{\mathbf{q}})kins(\vec{\mathbf{q}})^{-1}$$

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For small $\Delta \vec{\mathbf{q}}$, we can write the following expression for $\Delta \mathbf{F} = [Rot(\vec{\alpha}), \vec{\epsilon}]$

$$\Delta \mathbf{F} = Kins(\mathbf{q} + \Delta \mathbf{q})Kins(\mathbf{q})^{-1}$$

which we typically linearize as

$$\Delta \vec{\mathbf{x}} = \begin{bmatrix} \vec{\alpha} \\ \vec{\varepsilon} \end{bmatrix} \approx \mathbf{J}_{\mathit{Kins}}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}}$$



Note that here we are computing ΔF in the base frame of the robot. If we want to compute ΔF in the end effector frame, so that $F \bullet \Delta F = Kins(\vec{q} + \Delta \vec{q})$, then we will get a slightly different expression for $J_{Kins}(\vec{q})$, though the flavor will be the same

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Background: Jacobean Robot Motion Control



Pose
$$\mathbf{F}(\vec{\mathbf{q}} + \Delta \vec{\mathbf{q}}) = kins(\vec{\mathbf{q}} + \Delta \vec{\mathbf{q}})$$

 $\Delta \mathbf{F} \cdot \mathbf{F} = kins(\vec{\mathbf{q}} + \Delta \vec{\mathbf{q}})$

$$\Delta \mathbf{F} = \mathit{kins} ig(\mathbf{\ddot{q}} + \Delta \mathbf{\ddot{q}} ig) \mathit{kins} ig(\mathbf{\ddot{q}} ig)^{\!-1}$$

$$\left[\begin{array}{c} \vec{\alpha} \\ \varepsilon \end{array}\right] \approx \mathbf{J} \Big(\vec{\mathbf{q}} \Big) \Delta \vec{\mathbf{q}}$$

$$\Delta ec{f q} pprox {f J} {\left(ec{f q}
ight)}^{\! -1} {\left[egin{array}{c} ec{lpha} \ arepsilon \end{array}
ight]}$$

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Background: Jacobean Robot Motion Control

Alternative way of solving:

$$\begin{bmatrix} \vec{\alpha} \\ \varepsilon \end{bmatrix} \approx \mathbf{J}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}}$$

$$\Delta \vec{\mathbf{q}} \approx \underset{\Delta \vec{\mathbf{q}}}{\operatorname{argmin}} \left\| \mathbf{J}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}} - \begin{bmatrix} \vec{\alpha} \\ \varepsilon \end{bmatrix} \right\|^2$$

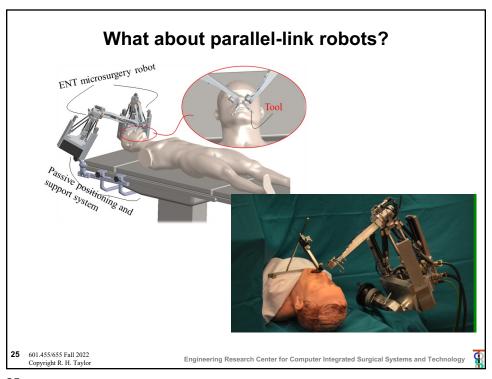
Advantages:

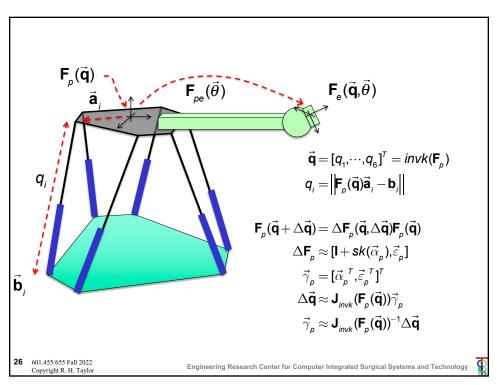
- · Produces solution even if kinematically redundant or kinematically deficient
- · Can add auxiliary constraints or objective function terms

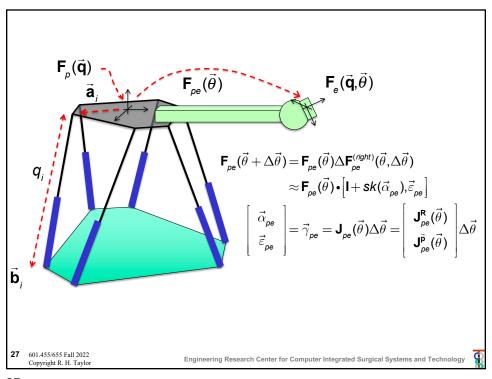
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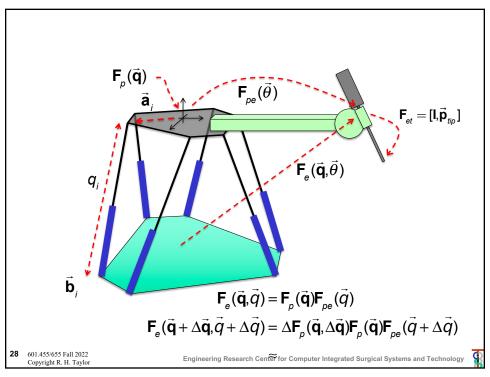
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Jacobean motion control implementation $\Delta \vec{\mathbf{X}}_{\underline{des}}$ Motion $\vec{\mathbf{q}}_{des}$ Position level Task level control q, q control control $\vec{\mathbf{q}}_{des} = \vec{\mathbf{q}} + \mathbf{J}^{-1}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{x}}_{des}$ F, q Motor Sensor values currents or values Surgeon input Robot kinematics Plan information & motion limits Anatomic models $Kins(\cdots), \mathbf{J}_{Kins}(\cdots)$ Safety constraints $\vec{q}_{i} \leq \vec{q} \leq \vec{q}_{ii}$ 601.455/655 Fall 2022 Copyright R. H. Taylor Engineering Research Center for Computer Integrated Surgical Systems and Technology









$$\begin{split} \mathbf{F}_{e}(\vec{\mathbf{q}},\vec{\theta}) &= \mathbf{F}_{\rho}(\vec{\mathbf{q}})\mathbf{F}_{\rho e}(\vec{\theta}) \\ \mathbf{F}_{e}(\vec{\mathbf{q}} + \Delta \vec{\mathbf{q}},\vec{\theta} + \Delta \vec{\theta}) &= \Delta \mathbf{F}_{\rho}(\vec{\mathbf{q}},\Delta \vec{\mathbf{q}})\mathbf{F}_{\rho}(\vec{\mathbf{q}})\mathbf{F}_{\rho e}(\vec{\theta} + \Delta \vec{\theta}) \\ \Delta \mathbf{F}_{e}(\vec{\mathbf{q}},\Delta \vec{\mathbf{q}},\vec{\theta},\Delta \vec{\theta})\mathbf{F}_{e}(\vec{\mathbf{q}},\vec{\theta}) &= \Delta \mathbf{F}_{\rho}(\vec{\mathbf{q}},\Delta \vec{\mathbf{q}})\mathbf{F}_{\rho}(\vec{\mathbf{q}})\mathbf{F}_{\rho e}(\vec{\theta})\Delta \mathbf{F}_{\rho e}(\vec{\theta},\Delta \vec{\theta}) \\ \Delta \mathbf{F}_{e}(\vec{\mathbf{q}},\Delta \vec{\mathbf{q}},\vec{\theta},\Delta \vec{\theta}) &= \Delta \mathbf{F}_{\rho}(\vec{\mathbf{q}},\Delta \vec{\mathbf{q}})\mathbf{F}_{\rho}(\vec{\mathbf{q}})\mathbf{F}_{\rho e}(\vec{\theta})\Delta \mathbf{F}_{\rho e}(\vec{\theta},\Delta \vec{\theta})\mathbf{F}_{e}(\vec{\mathbf{q}},\vec{\theta})^{-1} \\ &= \Delta \mathbf{F}_{\rho}(\vec{\mathbf{q}},\Delta \vec{\mathbf{q}})\mathbf{F}_{\rho}(\vec{\mathbf{q}})\mathbf{F}_{\rho e}(\vec{\theta})\Delta \mathbf{F}_{\rho e}(\vec{\theta},\Delta \vec{\theta})\mathbf{F}_{e}(\vec{\mathbf{q}},\vec{\theta})^{-1} \\ &= \Delta \mathbf{F}_{\rho}(\vec{\mathbf{q}},\Delta \vec{\mathbf{q}})\mathbf{F}_{e}(\vec{\mathbf{q}},\vec{\theta})\Delta \mathbf{F}_{\rho e}(\vec{\theta},\Delta \vec{\theta})\mathbf{F}_{e}(\vec{\mathbf{q}},\vec{\theta})^{-1} \\ \Delta \mathbf{R}_{e}(\vec{\mathbf{q}},\Delta \vec{\mathbf{q}},\Delta \vec{\theta}) &= \Delta \mathbf{R}_{\rho}(\vec{\mathbf{q}},\Delta \vec{\mathbf{q}})\mathbf{R}_{\rho}(\vec{\mathbf{q}})\mathbf{R}_{\rho e}(\vec{\theta})\Delta \mathbf{R}_{\rho e}(\vec{\theta},\Delta \vec{\theta})\Delta \mathbf{R}_{\rho e}(\vec{\mathbf{q}},\vec{\theta})^{-1} \mathbf{R}_{\rho e}(\vec{\mathbf{q}},\vec{\theta})^{-1} \\ \mathbf{I} + sk(\vec{\alpha}_{e}) \approx (\mathbf{I} + sk(\vec{\alpha}_{p}))\mathbf{R}_{e}(\vec{\mathbf{q}},\vec{\theta})(\mathbf{I} - sk(\vec{\alpha}_{pe}))\mathbf{R}_{e}(\vec{\mathbf{q}},\vec{\theta})^{-1} \end{split}$$

$$\begin{split} \mathbf{I} + sk(\vec{\alpha}_{e}) &\approx \left(\mathbf{I} + sk(\vec{\alpha}_{p})\right) \mathbf{R}_{e}(\vec{\mathbf{q}}, \vec{\theta}) (\mathbf{I} - sk(\vec{\alpha}_{pe})) \mathbf{R}_{e}(\vec{\mathbf{q}}, \vec{\theta})^{-1} \\ \mathbf{I} + sk(\vec{\alpha}_{e}) &\approx \left(\mathbf{I} + sk(\vec{\alpha}_{p})\right) \left(\mathbf{I} - \mathbf{R}_{e}(\vec{\mathbf{q}}, \vec{\theta}) sk(\vec{\alpha}_{pe}) \mathbf{R}_{e}(\vec{\mathbf{q}}, \vec{\theta})^{-1}\right) \\ \mathbf{I} + sk(\vec{\alpha}_{e}) &\approx \left(\mathbf{I} + sk(\vec{\alpha}_{p})\right) \left(\mathbf{I} - sk(\mathbf{R}_{e}(\vec{\mathbf{q}}, \vec{\theta}) \vec{\alpha}_{pe})\right) \\ \vec{\alpha}_{e} &\approx \vec{\alpha}_{p} - \mathbf{R}_{e}(\vec{\mathbf{q}}, \vec{\theta}) \vec{\alpha}_{pe} \\ \vec{\alpha}_{e} &\approx \mathbf{J}_{invk}^{\vec{\alpha}}(\mathbf{F}_{p}(\vec{\mathbf{q}}))^{-1} \Delta \vec{\mathbf{q}} - \mathbf{R}_{e}(\vec{\mathbf{q}}, \vec{\theta}) \vec{\alpha}_{pe} \end{split}$$

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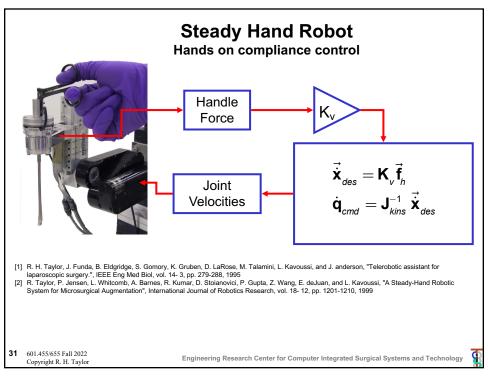
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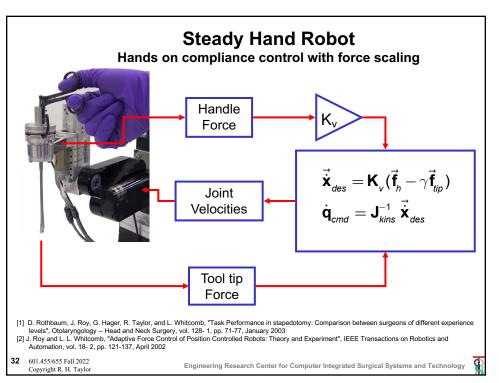
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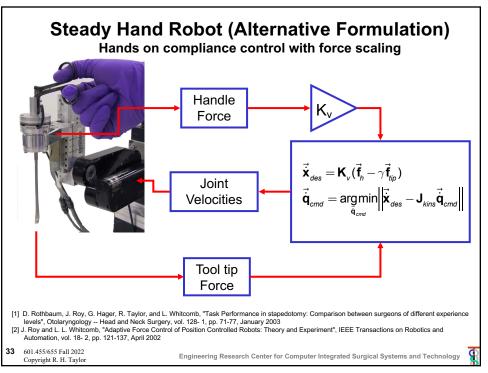
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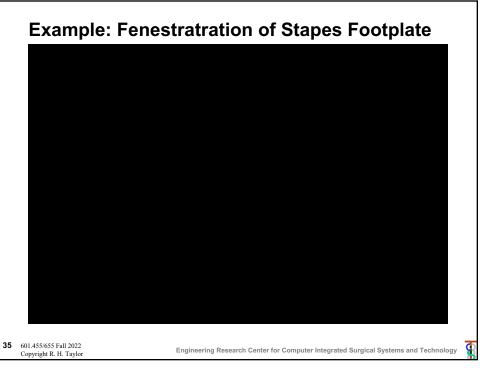
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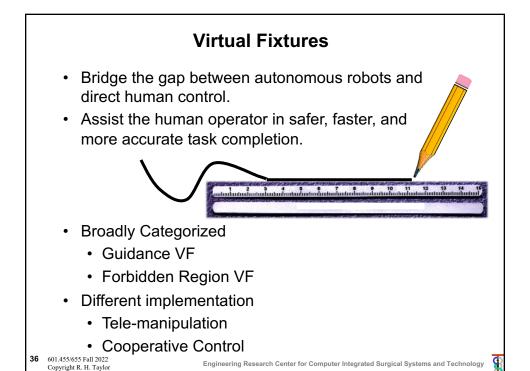












Background: Virtual Fixtures

- First proposed for complex telerobotic tasks, but draw upon rich prior research in robot assembly and other manufacturing automation applications
- Many authors, e.g.
 - L. B. Rosenberg, "Virtual Fixtures: Perceptual Tools for Telerobotic Manipulation," Proc. IEEE Virtual Reality International Symposium, 1993.
 - B. Davies, S. Harris, M. Jakopec, K. Fan, and J. cobb, "Intraoperative application of a robotic knee surgery system", MICCAI 1999.
 - S. Park, R. D. Howe, and D. F. Torchiana, "Virtual Fixtures for Robotic Cardiac Surgery", MICCAI 2001.
 - S. Payandeh and Z. Stanisic, "On Application of Virtual Fixtures as an Aid for Telemanipulation and Training," Symposium on Haptic Interfaces for Virtual Environment and Teleoperator Systems, 2002.
- Discussion that follows draws upon work at IBM Research and within the CISST ERC at JHU. E.a..
 - Funda, R. Taylor, B. Eldridge, S. Gomory, and K. Gruben, "Constrained Cartesian motion control for teleoperated surgical robots," *IEEE Transactions on Robotics and Automation*, vol. 12, pp. 453-466, 1996.
 - R. Kumar, An Augmented Steady Hand System for Precise Micromanipulation, Ph.D thesis in Computer Science, The Johns Hopkins University, Baltimore, 2001.
 - M. Li, M. Ishii, and R. H. Taylor, "Spatial Motion Constraints in Medical Robot Using Virtual Fixtures Generated by Anatomy," *IEEE Transactions on Robotics*, vol. 2, pp. 1270-1275, 2006.
 - A. Kapoor, M. Li, and R. H. Taylor "Constrained Control for Surgical Assistant Robots," in IEEE Int. Conference on Robotics and Automation, Orlando, 2006, pp. 231-236.
 - A. Kapoor and R. Taylor, "A Constrained Optimization Approach to Virtual Fixtures for Multi-Handed Tasks,"
 in IEEE International Conference on Polystics and Automation (ICPA). Pagadona, 2008, pp. 3401-3406.
 - in IEEE International Conference on Robotics and Automation (ICRA), Pasadena, 2008, pp. 3401-3406.
 M. Li, Intelligent Robotic Surgical Assistance for Sinus Surgery, PhD Thesis in Computer Science Baltimore, Maryland: The Johns Hopkins University, 2005.
 - Ankur Kapoor, Motion Constrained Control of Robots for Dexterous Surgical Tasks, Ph.D. Thesis in Computer Science, The Johns Hopkins University, Baltimore, September 2007

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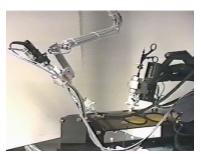
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Original Motivation for IBM Work

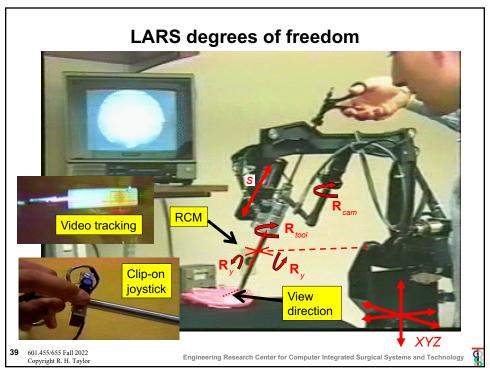
- · Kinematic control of robots for MIS
- · E.g., LARS and HISAR robots
- LARS and other IBM robots were kinematically redundant
 - Typically 7-9 actuated joints
- But tasks often imposed kinematic constraints
 - E.g., no lateral motion at trocar
- Some robots (e.g., IBM/JHU HISAR and CMI's AESOP) had passive joints
- · General goals
 - Exploit redundancy in best way possible
 - Come as close as possible to providing desired motion subject to robot and task limits
- Our approach: view this as a constrained optimization problem





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Motion Specification Problem

Requirements

- The tool shaft must pass within a specified distance of the entry port into the patient's body
- The individual joint limits may not be exceeded

Goals

- Aim the camera as close as possible at a target
 - or move view in direction indicated by clip-on pointing device
 - <u>or</u> move to track a video target on an instrument
 - or aim the working channel of the endoscope at a target
 - or something else (maybe a combination of goals)
- Keep the view as "upright" as possible
- Tool should pass as close as possible to entry port center
- Keep joints far away from their limits, to preserve options for future motion
- Minimize motion of XYZ joints
- Etc.

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Our approach: view as an optimization problem

- Currently formulate problem as constrained least squares problem
- · Express goals in the objective function
- If multiple goals, objective function is a weighted sum of individual elements
- · Add constraints for requirements
- Express constraints and objective function terms in whatever coordinate system is convenient
- · Use Jacobean formulation to transform to joint space
- · Solve for joint motion

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Example: keep tool tip near a point

$$\begin{split} \vec{D}(\Delta \vec{\mathbf{x}}) &= \Delta \mathbf{F}(\vec{\mathbf{q}}, \Delta \vec{\mathbf{q}}) \bullet \mathbf{F} \bullet \mathbf{p}_{tip} - \vec{\mathbf{p}}_{goal} \\ &= \vec{\alpha} \times \vec{\mathbf{t}} + \vec{\varepsilon} + \vec{\mathbf{t}} - \vec{\mathbf{p}}_{goal} \quad \text{where } \vec{\mathbf{t}} = \mathbf{F} \bullet \mathbf{p}_{tip} \\ \vec{\alpha} &= \mathbf{J}_{\vec{\alpha}}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}} \\ \vec{\varepsilon} &= \mathbf{J}_{\vec{\varepsilon}}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}} \end{split}$$

Suppose we want to stay as close as possible while never going beyond 3mm from goal and also obeying joint limits

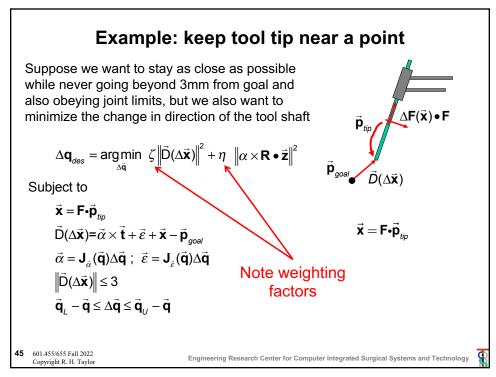
$$\Delta \mathbf{q}_{des} = \underset{\Delta \vec{\mathbf{p}}}{\text{argmin}} \ \left\| \vec{\mathbf{D}} (\Delta \vec{\mathbf{x}}) \right\|^2 = \left\| \vec{\alpha} \times \vec{\mathbf{t}} + \vec{\varepsilon} + \vec{\mathbf{t}} - \vec{\mathbf{p}}_{goal} \right\|^2$$

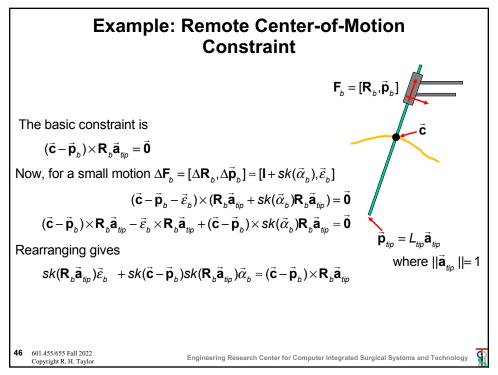
Subject to

$$\begin{split} \vec{\alpha} &= \mathbf{J}_{\vec{\alpha}}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}} \\ \vec{\varepsilon} &= \mathbf{J}_{\vec{\varepsilon}}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}} \\ \left\| \vec{\alpha} \times \vec{\mathbf{t}} + \vec{\varepsilon} + \vec{\mathbf{t}} - \vec{\mathbf{p}}_{goal} \right\| \leq 3 \\ \vec{\mathbf{q}}_{L} - \vec{\mathbf{q}} \leq \Delta \vec{\mathbf{q}} \leq \vec{\mathbf{q}}_{U} - \vec{\mathbf{q}} \end{split}$$

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Solving the optimization problem

- · Constrained linear least squares
 - Combine constraints and goals from task and robot control
 - Linearize and constrained least squares problem

$$\Delta \vec{\boldsymbol{q}}_{\textit{des}} = \underset{\Delta \vec{\boldsymbol{q}}}{\text{argmin}} \left\| \boldsymbol{\mathsf{E}}_{\textit{task}} \Delta \vec{\boldsymbol{x}} - \vec{\boldsymbol{\mathsf{f}}}_{\textit{task}} \right\|^2 + \left\| \boldsymbol{\mathsf{E}}_{\vec{\boldsymbol{q}}} \Delta \vec{\boldsymbol{x}} - \vec{\boldsymbol{\mathsf{f}}}_{\vec{\boldsymbol{q}}} \right\|^2$$

subject to

$$\Delta \vec{\mathbf{x}} = \mathbf{J} \Delta \vec{\mathbf{q}}; \ \mathbf{A}_{task} \Delta \vec{\mathbf{x}} \leq \vec{\mathbf{b}}_{task} \ ; \ \mathbf{A}_{\vec{\mathbf{q}}} \Delta \vec{\mathbf{q}} \leq \vec{\mathbf{b}}_{\vec{\mathbf{q}}}$$

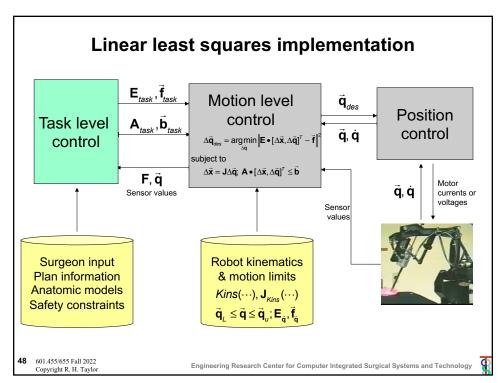
- E.g., using "non-negative least squares" methods developed by Lawson and Hanson
- Approach used in our IBM work and in Kumar, Li, Kapoor theses
- · Constrained nonlinear least squares
 - Approach explored by Kapoor (discuss later)
- Can also minimize other objective functions
 - E.g., minimize an L1 norm (linear programming problem)

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Typical Mid-Level Control Loop

- Step 1. Read robot state (q,q,etc.) and sensor values.
- Step 2. Perform safety checks and stop motion if needed.
- Step 3. Output $\Delta \vec{\mathbf{q}}/\Delta T$ values computed on previous clock tick (done now so commands to low level controller come at predictable times).
- Step 4. Interpret any commands from task level controller.
- Step 5. Compute $\mathbf{F}_{kins}(\mathbf{\vec{q}})$ and $\mathbf{J}_{kins}(\mathbf{\vec{q}})$.
- Step 6. Based on the current commanded behavior, robot state & kinematics, sensor values, and registered anatomic model, compute the desired incremental joint motion $\Delta \ddot{\mathbf{q}}$ for the next clock tick. Typically, this will involve formulating and solving an optimization problem, e.g.,

$$\begin{split} \Delta \vec{\mathbf{q}} &= \underset{\Delta \vec{\mathbf{q}}}{\operatorname{argmin}} \left| \left| \mathbf{A}_{\vec{\xi}} \vec{\xi} - \vec{\mathbf{b}}_{\vec{\xi}} \right| \right|^2 + \left| \left| \mathbf{A}_{\Delta \vec{\mathbf{q}}} \Delta \vec{\mathbf{q}} - \vec{\mathbf{b}}_{\Delta \vec{\mathbf{q}}} \right| \right|^2 \\ \vec{\xi} &= \mathbf{J}_{\text{kins}} (\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}} \\ \mathbf{C}_{\vec{\xi}} \vec{\xi} &\leq \vec{\mathbf{d}}_{\vec{\xi}} \\ \mathbf{C}_{\Delta \vec{\mathbf{q}}} \Delta \vec{\mathbf{q}} &\leq \vec{\mathbf{d}}_{\Delta \vec{\mathbf{q}}} \end{split}$$

Step 7. Go to sleep until the next clock tick.

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Some IBM Movies



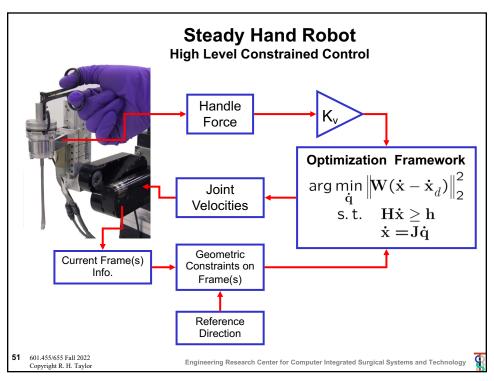
Early Constrained Motion System (LapSYS)

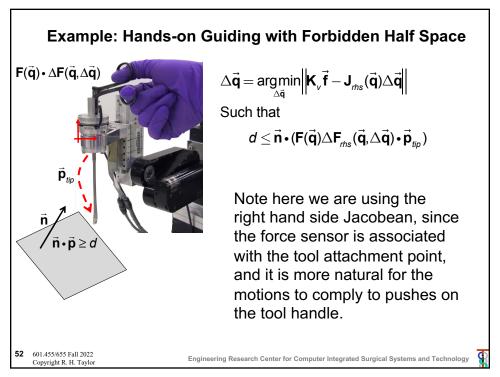


Vision-guided targeting

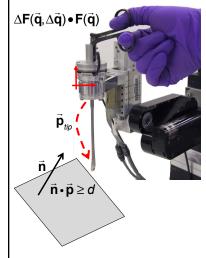
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$$\Delta \vec{\mathbf{q}} = \underset{\triangle \vec{\mathbf{q}}}{\operatorname{argmin}} \left| \left| \mathbf{K}_{_{V}} \vec{\mathbf{f}} - \mathbf{J}_{\mathit{ms}}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}} \right| \right|$$

Such that

$$\begin{bmatrix} \vec{\alpha} \\ \vec{\varepsilon} \end{bmatrix} = \mathbf{J}_{rhs}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}}$$
$$d \leq \vec{\mathbf{n}} \cdot \left(\mathbf{F}(\vec{\mathbf{q}}) \cdot (\vec{\alpha} \times \vec{\mathbf{p}}_{tip} + \vec{\varepsilon} + \vec{\mathbf{p}}_{tip}) \right)$$

I.e.,

$$\begin{bmatrix} \vec{\alpha} \\ \vec{\varepsilon} \end{bmatrix} = \mathbf{J}_{rhs}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}}$$
$$d \leq \vec{\mathbf{n}} \cdot (\mathbf{R}(\vec{\mathbf{q}}) \cdot (\vec{\alpha} \times \vec{\mathbf{p}}_{tip} + \vec{\varepsilon} + \vec{\mathbf{p}}_{tip}) + \vec{\mathbf{p}}_{kins})$$

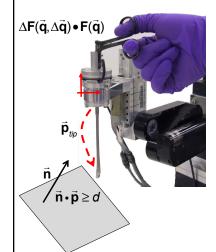
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Example: Hands-on Guiding with Forbidden Half Space



$$\Delta \vec{\mathbf{q}} = \underset{\Delta \vec{\mathbf{q}}}{\operatorname{argmin}} \left| \mathbf{K}_{_{V}} \vec{\mathbf{f}} - \mathbf{J}_{_{\mathit{rhs}}} (\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}} \right|^2$$

Such that

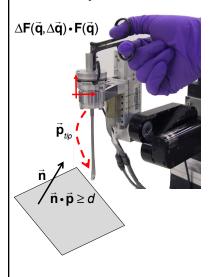
$$\begin{bmatrix} \vec{\alpha} \\ \vec{\varepsilon} \end{bmatrix} = \mathbf{J}_{ms}(\vec{\mathbf{q}}) \triangle \vec{\mathbf{q}}$$
$$d - \vec{\mathbf{n}} \cdot \vec{\mathbf{x}} \le \vec{\mathbf{n}} \cdot (\mathbf{R}(\vec{\mathbf{q}}) \cdot (\vec{\alpha} \times \vec{\mathbf{p}}_{tip} + \vec{\varepsilon}))$$
$$\vec{\mathbf{x}} = \mathbf{F}(\vec{\mathbf{q}}) \vec{\mathbf{p}}_{tip}$$

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Example: Hands-on Guiding with Forbidden Half Space



$$\Delta \vec{\mathbf{q}} = \underset{\Delta \vec{\mathbf{q}}}{\operatorname{argmin}} \left\| \mathbf{K}_{v} \vec{\mathbf{f}} - \mathbf{J}_{kins}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}} \right\|^{2}$$

Such that

$$d \leq \vec{n} \cdot (\Delta F(\vec{q}, \Delta \vec{q}) \cdot F(\vec{q}) \cdot \vec{p}_{tio})$$

If we use the LHS Jacobean, we get something similar. Note however that in this case the gain matrix will likely be pose dependent, since the it is more natural for the surgeon's hand to follow the tool. So it is useful to be able to make the conversion ...

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LHS versus RHS Jacobeans

$$\Delta F (J_{kins}(\vec{q}) \Delta \vec{q}) \cdot F(\vec{q}) = F(\vec{q}) \cdot \Delta F(J_{ms}(\vec{q}) \Delta \vec{q})$$

$$\Delta R (J_{kins}(\vec{q}) \Delta \vec{q}) \cdot R(\vec{q}) = R(\vec{q}) \cdot \Delta R(J_{ms}(\vec{q}) \Delta \vec{q})$$

Define

$$\mathbf{J}_{\mathit{kins}} = \left[\begin{array}{c} \mathbf{J}_{\mathit{kins}}^{\alpha} \\ \mathbf{J}_{\mathit{kins}}^{\varepsilon} \end{array} \right] \quad \vec{\alpha}_{\mathit{kins}} = \mathbf{J}_{\mathit{kins}}^{\alpha} \Delta \vec{\mathbf{q}} \quad \mathbf{J}_{\mathit{ths}} = \left[\begin{array}{c} \mathbf{J}_{\mathit{ths}}^{\alpha} \\ \mathbf{J}_{\mathit{ths}}^{\varepsilon} \end{array} \right] \quad \vec{\alpha}_{\mathit{ths}} = \mathbf{J}_{\mathit{ths}}^{\alpha} \Delta \vec{\mathbf{q}}$$

so

$$\begin{split} \Delta \mathbf{R}(\mathbf{J}_{\textit{rhs}}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}}) &= \mathbf{R}(\vec{\mathbf{q}})^{-1} \Delta \mathbf{R} \left(\mathbf{J}_{\textit{kins}} \Delta \vec{\mathbf{q}} \right) \bullet \mathbf{R}(\vec{\mathbf{q}}) \\ \mathbf{I} + sk(\alpha_{\textit{rhs}}) &= \mathbf{I} + \mathbf{R}^{-1} sk(\vec{\alpha}_{\textit{kins}}) \mathbf{R} \\ sk(\vec{\alpha}_{\textit{rhs}}) &= sk(\mathbf{R}^{-1} \vec{\alpha}_{\textit{kins}}) \\ \mathbf{J}_{\textit{rhs}}^{\alpha} &= \mathbf{R}^{-1} \mathbf{J}_{\textit{kins}}^{\alpha} \end{split}$$

and one can do something similar for the $\Delta \vec{p}$ parts.

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LHS versus RHS Jacobeans

$$\Delta F (J_{kins}(\vec{q}) \Delta \vec{q}) \cdot F(\vec{q}) = F(\vec{q}) \cdot \Delta F(J_{rhs}(\vec{q}) \Delta \vec{q})$$

Define

$$\mathbf{J}_{\mathrm{kins}} = \begin{bmatrix} \mathbf{J}_{\mathrm{kins}}^{\alpha} \\ \mathbf{J}_{\mathrm{kins}}^{\varepsilon} \end{bmatrix} \quad \vec{\alpha}_{\mathrm{kins}} = \mathbf{J}_{\mathrm{kins}}^{\alpha} \Delta \vec{\mathbf{q}} \quad \mathbf{J}_{\mathrm{rhs}} = \begin{bmatrix} \mathbf{J}_{\mathrm{rhs}}^{\alpha} \\ \mathbf{J}_{\mathrm{rhs}}^{\varepsilon} \end{bmatrix} \quad \vec{\alpha}_{\mathrm{rhs}} = \mathbf{J}_{\mathrm{rhs}}^{\alpha} \Delta \vec{\mathbf{q}}$$

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$$\begin{split} \mathbf{R}(\vec{\mathbf{q}}) \vec{\varepsilon}_{\textit{rhs}} + \vec{\mathbf{p}}(\vec{\mathbf{q}}) &= \Delta \mathbf{R}(\vec{\alpha}_{\textit{kins}}) \vec{\mathbf{p}}(\vec{\mathbf{q}}) + \vec{\varepsilon}_{\textit{kins}} \\ \mathbf{R}(\vec{\mathbf{q}}) \vec{\varepsilon}_{\textit{rhs}} &= \vec{\mathbf{p}}(\vec{\mathbf{q}}) + \vec{\alpha}_{\textit{kins}} \times \vec{\mathbf{p}}(\vec{\mathbf{q}}) + \vec{\varepsilon}_{\textit{kins}} - \vec{\mathbf{p}}(\vec{\mathbf{q}}) \\ \vec{\varepsilon}_{\textit{rhs}} &= \mathbf{R}(\vec{\mathbf{q}})^{-1} \Big(\vec{\alpha}_{\textit{kins}} \times \vec{\mathbf{p}}(\vec{\mathbf{q}}) + \vec{\varepsilon}_{\textit{kins}} \Big) \\ &= \mathbf{R}(\vec{\mathbf{q}})^{-1} \Big(\vec{\varepsilon}_{\textit{kins}} - sk \Big(\vec{\mathbf{p}}(\vec{\mathbf{q}}) \Big) \vec{\alpha}_{\textit{kins}} \Big) \\ &= \mathbf{R}(\vec{\mathbf{q}})^{-1} \vec{\varepsilon}_{\textit{kins}} - \mathbf{R}(\vec{\mathbf{q}})^{-1} sk \Big(\vec{\mathbf{p}}(\vec{\mathbf{q}}) \Big) \vec{\alpha}_{\textit{kins}} \end{split}$$

$$\mathbf{J}_{\textit{rhs}} = \left[\begin{array}{cc} \mathbf{R}^{-1} & \mathbf{0} \\ -\mathbf{R}^{-1} \mathbf{s} \textit{k}(\vec{\mathbf{p}}) & \mathbf{R}^{-1} \end{array} \right] \mathbf{J}_{\textit{kins}}$$

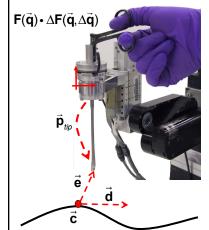
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Example: Hands-on Guiding to Follow a Path



$$\Delta \vec{\mathbf{q}} = \underset{\Delta \vec{\mathbf{q}}}{\operatorname{argmin}} \left| \left| \mathbf{K}_{_{V}} \vec{\mathbf{f}} - \mathbf{J}_{_{\mathit{fhS}}} (\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}} \right| \right|$$

Such that

$$\vec{\mathbf{e}} = (\mathbf{F}(\vec{\mathbf{q}}) \Delta \mathbf{F}_{ths}(\vec{\mathbf{q}}, \Delta \vec{\mathbf{q}}) \cdot \vec{\mathbf{p}}_{tip}) - \vec{\mathbf{c}}$$

$$\delta \geq \left| \vec{\mathbf{e}} - \left(\vec{\mathbf{d}} \cdot \vec{\mathbf{e}} \right) \vec{\mathbf{d}} \right|$$

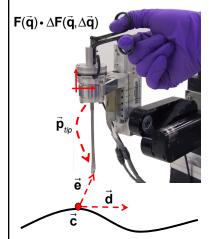
Note: δ is the maximum deviation allowed from the path

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Example: Hands-on Guiding to Follow a Path



$$\Delta \vec{\mathbf{q}} = \underset{\Delta \vec{\mathbf{q}}}{\operatorname{argmin}} \left| \left| \mathbf{K}_{\scriptscriptstyle V} \vec{\mathbf{f}} - \mathbf{J}_{\mathit{ms}}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}} \right| \right|^2$$

Such that

$$\vec{\mathbf{e}} = (\mathbf{F}(\vec{\mathbf{q}}) (\vec{\alpha} \times \vec{\mathbf{p}}_{tip} + \vec{\varepsilon} + \vec{\mathbf{p}}_{tip})) - \vec{\mathbf{c}}$$

$$\begin{bmatrix} \vec{\alpha} \\ \vec{\varepsilon} \end{bmatrix} = \mathbf{J}_{ms}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}}$$

$$\delta \geq \left| |\vec{\mathbf{e}} - (\vec{\mathbf{d}} \cdot \vec{\mathbf{e}}) \vec{\mathbf{d}}| \right|$$

Note: δ is the maximum deviation allowed from the path

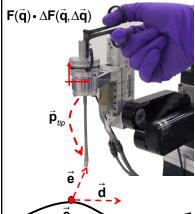
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Example: Hands-on Guiding to Follow a Path



$$\Delta \vec{\mathbf{q}} = \underset{\Delta \vec{\mathbf{q}}}{\operatorname{argmin}} \left\| \mathbf{K}_{_{V}} \vec{\mathbf{f}} - \mathbf{J}_{\textit{rhs}}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}} \right\|^{2}$$

Such that

$$\vec{\mathbf{e}} = \mathbf{R}(\vec{\mathbf{q}}) \left(\vec{\alpha} \times \vec{\mathbf{p}}_{tip} + \vec{\varepsilon} + \vec{\mathbf{p}}_{tip} \right) + \vec{\mathbf{p}}(\vec{\mathbf{q}}) - \vec{\mathbf{c}}$$

$$\begin{bmatrix} \vec{\alpha} \\ \vec{\varepsilon} \end{bmatrix} = \mathbf{J}_{ms}(\vec{\mathbf{q}}) \Delta \vec{\mathbf{q}}$$

$$\delta \ge \left| |\vec{\mathbf{e}} - (\vec{\mathbf{d}} \cdot \vec{\mathbf{e}}) \vec{\mathbf{d}} \right|$$

Note: δ is the maximum deviation allowed from the path

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